

Package ‘xega’

February 17, 2026

Title Extended Evolutionary and Genetic Algorithms

Version 0.9.0.23

Description Implementation of a scalable, highly configurable, and e(x)tended architecture for (e)volutionary and (g)enetic (a)lgorithms. Multiple representations (binary, real-coded, permutation, and derivation-tree), a rich collection of genetic operators, as well as an extended processing pipeline are provided for genetic algorithms (Goldberg, D. E. (1989, ISBN:0-201-15767-5)), differential evolution (Price, Kenneth V., Storn, Rainer M. and Lampinen, Jouni A. (2005) <[doi:10.1007/3-540-31306-0](https://doi.org/10.1007/3-540-31306-0)>), simulated annealing (Aarts, E., and Korst, J. (1989, ISBN:0-471-92146-7)), grammar-based genetic programming (Geyer-Schulz (1997, ISBN:978-3-7908-0830-X)), grammatical evolution (Ryan, C., O'Neill, M., and Collins, J. J. (2018) <[doi:10.1007/978-3-319-78717-6](https://doi.org/10.1007/978-3-319-78717-6)>), and grammatical differential evolution (O'Neill, M. and Brabazon, A. (2006) in Arabinia, H. (2006, ISBN:978-193-241596-3). All algorithms reuse basic adaptive mechanisms for performance optimization. For 'xega's architecture, see Geyer-Schulz, A. (2025) <[doi:10.5445/IR/1000187255](https://doi.org/10.5445/IR/1000187255)>. Sequential or parallel execution (on multi-core machines, local clusters, and high-performance computing environments) is available for all algorithms. See <<https://github.com/ageyerschulz/xega/tree/main/examples/executionModel>>.

License MIT + file LICENSE

URL <https://github.com/ageyerschulz/xega>

Encoding UTF-8

RoxygenNote 7.3.3

Depends R (>= 3.5.0), parallelly, filelock

Imports xegaSelectGene, xegaBNF, xegaDerivationTrees, xegaGaGene, xegaGpGene, xegaGeGene, xegaDfGene, xegaPermGene, xegaPopulation (>= 1.0.0.12)

Suggests testthat (>= 3.0.0)

NeedsCompilation no

Author Andreas Geyer-Schulz [aut, cre] (ORCID: <<https://orcid.org/0009-0000-5237-3579>>)

Maintainer Andreas Geyer-Schulz <Andreas.Geyer-Schulz@kit.edu>

Repository CRAN

Date/Publication 2026-02-17 10:40:02 UTC

Contents

booleanGrammar	2
compileBNF	3
createExclusiveFile	4
lau15	5
NewEnvXOR	5
Parabola2D	6
Parabola2DEarly	7
sgXCrossoverFactory	8
sgXDecodeGeneFactory	9
sgXGeneMapFactory	10
sgXInitGeneFactory	11
sgXMutationFactory	11
sgXReplicationFactory	12
xega	13
xegaAnyTimeResult	16
xegaDebug	17
xegaReRun	18
xegaRun	19
xegaVersion	45
Index	46

booleanGrammar	<i>A constant function with a boolean grammar.</i>
----------------	--

Description

For the distribution of examples of BNF in grammars.

Usage

```
booleanGrammar()
```

Details

Imported from package xegaBNF for use in examples.

Value

A named list with \$filename and \$BNF, the grammar of a boolean grammar with two variables.

See Also

Other Grammar: [compileBNF\(\)](#)

Examples

```
booleanGrammar()
```

compileBNF

Compile a BNF.

Description

`compileBNF()` produces a context-free grammar from its specification in Backus-Naur form (BNF).
Warning: No error checking implemented.

Usage

```
compileBNF(g, verbose = FALSE)
```

Arguments

<code>g</code>	A character string with a BNF.
<code>verbose</code>	Boolean. TRUE: Show progress. Default: FALSE.

Details

A grammar consists of the symbol table `ST`, the production table `PT`, the start symbol `Start`, and the short production table `SPT`. An example BNF is provided by `booleanGrammar()`.

The function performs the following steps:

1. Make the symbol table.
2. Make the production table.
3. Extract the start symbol.
4. Compile a short production table.
5. Return the grammar.

For a full documentation, see <https://CRAN.R-project.org/package=xegaBNF>

Value

A grammar object (list) with the attributes `name` (the filename of the grammar), `ST` (symbol table), `PT` (production table), `Start` (the start symbol of the grammar), and `SPT` (the short production table).

See Also

Other Grammar: [booleanGrammar\(\)](#)

Examples

```
g<-compileBNF(booleanGrammar())
g$ST
g$PT
g$Start
g$SPT
```

createExclusiveFile *Create a unique filename.*

Description

Name conflicts in filenames are avoided by

- Including the time fractions below a second (tfrac).
- Padding the name with 6 random letters.
- Locking and retrying (as a last resort). The program stops after 10 unsuccessful attempts of finding a unique name.

Created by Jens Kleineheismann (2025).

Usage

```
createExclusiveFile(fpath = ".", prefix = "data", ext = ".dat")
```

Arguments

fpath	File path. Default: ".".
prefix	The filename. Default: "data".
ext	The file extension. Default: ".dat".

Value

A filename. Components: [prefix]_[year][month][day]_[h][min][sec]_[node]_[pid]_[pad]_[fracsec].[ext]

Examples

```
tmp<-tempdir()
fn<-createExclusiveFile(fpath=tmp, prefix="data", ext=".dat")
cat(fn)
```

`lau15`*The problem environment lau15*

Description

15 abstract cities for which a traveling salesman solution is sought. Solution: A path with a length of 291.

Usage

```
lau15
```

Format

An object of class `list` of length 14.

References

Lau, H. T. (1986): *Combinatorial Heuristic Algorithms in FORTRAN*. Springer, 1986. <doi:10.1007/978-3-642-61649-5>

See Also

Other Problem Environment: [NewEnvXOR\(\)](#), [Parabola2D](#), [Parabola2DEarly](#)

Examples

```
names(lau15)
lau15$genelength()
```

`NewEnvXOR`*Generate the problem environment EnvXOR*

Description

`NewEnvXOR()` generates the problem environment for the XOR-Problem.

The problem environment provides an abstract interface to the simple genetic programming algorithm. `ProblemEnv$f(perm)` defines the function we want to optimize.

A problem environment is a function factory with the following elements:

1. `name()`: A string with the name of the environment.
2. `ProblemEnv$f(word)`: Function with the word a word of the language (as a text string).

Should be provided by the user as a standard R-file.

Usage

```
NewEnvXOR()
```

Value

The problem environment:

- `$name`: The name of the problem environment.
- `$f`: The fitness function. For this environment, fitness is defined as the number of correct test cases (correct function) and the inverse of the number of terminal symbols. The second part means that a boolean function with a fewer number of variables and logical functions is fitter than one with more variables and logical functions if both solve the same number of test cases.

See Also

Other Problem Environment: [Parabola2D](#), [Parabola2DEarly](#), [lau15](#)

Examples

```
EnvXOR<-NewEnvXOR()
EnvXOR$name()
a2<-"OR(OR(D1, D2), (AND(NOT(D1), NOT(D2))))"
a3<-"OR(OR(D1, D2), AND(D1, D2))"
a4<-"AND(OR(D1,D2),NOT(AND(D1,D2)))"
gp4<-"(AND(AND(OR(D2,D1),NOT(AND(D1,D2))), (OR(D2,D1))))"
EnvXOR$f(a2)
EnvXOR$f(a3)
EnvXOR$f(a4)
EnvXOR$f(gp4)
```

Parabola2D

Problem environment for a 2-dimensional quadratic parabola

Description

Problem environment for finding maxima and minima of a 2-dimensional quadratic parabola.

Usage

```
Parabola2D
```

Format

An object of class `list` of length 8.

Value

A named list

- `$name()`: Returns the name of the problem environment.
- `$bitlength()`: The vector of the bitlengths of the parameters.
- `$genelength()`: The number of bits of a gene.
- `$lb()`: The vector of lower bounds of the parameters.
- `$ub()`: The vector of upper bounds of the parameters.
- `$f(parm)`: The implementation of the function of the quadratic parabola.
 - `parm`: A 2-element vector of reals.
 - Returns the value of the function.
- `$describe()`: Returns the description of the problem environment.
- `$solution()`: The solutions (maxima/minima) of the problem environment (if known).

See Also

Other Problem Environment: [NewEnvXOR\(\)](#), [Parabola2DEarly](#), [lau15](#)

Examples

```
names(Parabola2D)
Parabola2D$name()
Parabola2D$describe()
Parabola2D$bitlength()
Parabola2D$genelength()
Parabola2D$lb()
Parabola2D$ub()
Parabola2D$f
Parabola2D$f(c(2.2, -1.37))
Parabola2D$solution()
Parabola2D$solution()$minimum
Parabola2D$solution()$minpoints
Parabola2D$solution()$maximum
Parabola2D$solution()$maxpoints
```

Parabola2DEarly

Problem environment for a 2-dimensional quadratic parabola.

Description

An example of a problem environment with an early termination condition.

Usage

```
Parabola2DEarly
```

Format

An object of class `list` of length 9.

Value

A problem environment (see [Parabola2D](#)). `Parabola2DEarly$terminate(solution, lF)` is a test function which returns true if the solution is in an epsilon environment of a known solution. To invoke this function, use `xegaRun(..., early=TRUE, ...)`. The epsilon which determines the length of the interval as a fraction of the known optimal solution is configured by e.g. `xegaRun(..., terminationEps=0.001, ...)`.

See Also

Other Problem Environment: [NewEnvXOR\(\)](#), [Parabola2D](#), [lau15](#)

`sgXCrossoverFactory` *Factory for configuring a gene-dependent Crossover function.*

Description

`sgXCrossoverFactory()` selects

1. the algorithm-specific crossover factory and
2. the method in this factory.

Usage

```
sgXCrossoverFactory(algorithm = "sga", method = "CrossGene")
```

Arguments

<code>algorithm</code>	Specifies algorithm. Available: "sga", "sgde", "sgperm", "sge", "sgp". Default: "sga".
<code>method</code>	Crossover method. Algorithm (gene representation) dependent. Default: <code>CrossGene()</code> . Must be available in the gene-specific crossover factories.

Details

The available methods for each algorithm are:

- "sga": "Cross2Gene", "UCross2Gene", "UPCross2Gene", "CrossGene", "UCrossGene", "UPCrossGene".
- "sge": "Cross2Gene", "UCross2Gene", "UPCross2Gene", "CrossGene", "UCrossGene", "UPCrossGene".
- "sgede": "CrossGene", "UCrossGene", "UPCrossGene".
- "sgp": "Cross2Gene", "AllCrossGene", "AllCross2Gene", "FilterCrossGene", "FilterCross2Gene".
- "sgde": "CrossGene", "UCrossGene", "UPCrossGene".
- "sgperm": "CrossGene", "Cross2Gene".

Value

Crossover function from the crossover factory of the selected package.

See Also

Other Configuration: [sgXDecodeGeneFactory\(\)](#), [sgXGeneMapFactory\(\)](#), [sgXInitGeneFactory\(\)](#), [sgXMutationFactory\(\)](#), [sgXReplicationFactory\(\)](#)

Examples

```
sgXCrossoverFactory(algorithm="sga", method="CrossGene")
```

`sgXDecodeGeneFactory` *Factory for configuring a gene-dependent DecodeGene function.*

Description

A gene-specific decoder must be provided.

Usage

```
sgXDecodeGeneFactory(algorithm = "sga", method = "DecodeGene")
```

Arguments

algorithm	"sga", "sgde", "sgperm", "sge", "sgede", "sgp". Default: "sga".
method	Method. Default: "DecodeGene".

Value

Decode function for the selected algorithm from the correct package.

See Also

Other Configuration: [sgXCrossoverFactory\(\)](#), [sgXGeneMapFactory\(\)](#), [sgXInitGeneFactory\(\)](#), [sgXMutationFactory\(\)](#), [sgXReplicationFactory\(\)](#)

Examples

```
sgXDecodeGeneFactory(algorithm="sgperm", method="DecodeGene")
```

sgXGeneMapFactory *Factory for configuring a gene-dependent geneMap function.*

Description

The geneMap function depends on the gene representation and the algorithm selected.

Usage

```
sgXGeneMapFactory(algorithm = "sga", method = "Bin2Dec")
```

Arguments

algorithm Algorithm. Available: "sga", "sgde", "sgperm", "sge", "sgp". Default: "sga".
method The GeneMap method. The choices depend on the algorithm.

Details

Methods available for the different algorithms are:

- "sga": "Bin2Dec", "Gray2Dec", "Identity", "Permutation".
- "sgde": "Identity".
- "sgperm": "Identity". The gene map function is not used in the decoder.
- "sgp": "Identity". The gene map function is not used in the decoder.
- "sge": "Mod" or "Bucket".
- "sgede": "Identity".

Value

GeneMap function for the selected algorithm from the correct package.

See Also

Other Configuration: [sgXCrossoverFactory\(\)](#), [sgXDecodeGeneFactory\(\)](#), [sgXInitGeneFactory\(\)](#), [sgXMutationFactory\(\)](#), [sgXReplicationFactory\(\)](#)

Examples

```
sgXGeneMapFactory(algorithm="sga", method="Bin2Dec")
```

sgXInitGeneFactory *Factory for configuring a gene-dependent InitGene function.*

Description

Factory for configuring a gene-dependent InitGene function.

Usage

```
sgXInitGeneFactory(algorithm = "sga", method = "InitGene")
```

Arguments

algorithm Algorithm. Available: "sga", "sgde", "sgperm", "sge", "sgp". Default: "sga".
method Method. Default: "InitGene". For sgp, method = "InitGene" or "InitGeneGe".

Value

InitGene function from the correct package.

See Also

Other Configuration: [sgXCrossoverFactory\(\)](#), [sgXDecodeGeneFactory\(\)](#), [sgXGeneMapFactory\(\)](#), [sgXMutationFactory\(\)](#), [sgXReplicationFactory\(\)](#)

Examples

```
sgXInitGeneFactory(algorithm="sgperm")
```

sgXMutationFactory *Factory for configuring a gene-dependent Mutation function.*

Description

sgXMutationFactory() selects

1. the algorithm-specific mutation factory and
2. the method in this factory.

Usage

```
sgXMutationFactory(algorithm = "sga", method = "MutateGene")
```

Arguments

algorithm	Algorithm. Available: "sga", "sgde", "sgperm", "sge", sgp". Default: "sga".
method	Method. Available methods are package-dependent.

Details

The available methods for each factory are:

- "sga": "MutateGene", "IVM".
- "sge": "MutateGene", "IVM".
- "sgp": "MutateGene", "MutateAllGene", "MutateFilterGene".
- "sgede": "MutateGene", "MutateGeneDE".
- "sgde": "MutateGene", "MutateGeneDE".
- "sgperm": "MutateGene", "MutateGeneOrderBased", "MutateGenekInversion", "MutateGene2Opt", "MutateGenekOptLK", "MutateGeneGreedy", "MutateGeneBestGreedy", "MutateGeneMix".

Value

MutateGene function for the selected algorithm from the correct package.

See Also

Other Configuration: [sgXCrossoverFactory\(\)](#), [sgXDecodeGeneFactory\(\)](#), [sgXGeneMapFactory\(\)](#), [sgXInitGeneFactory\(\)](#), [sgXReplicationFactory\(\)](#)

Examples

```
sgXMutationFactory(algorithm="sga", method="MutateGene")
```

`sgXReplicationFactory` *Factory for configuring a gene-dependent Replication function.*

Description

Factory for configuring a gene-dependent Replication function.

Usage

```
sgXReplicationFactory(algorithm = "sga", method = "Kid1")
```

Arguments

algorithm	Algorithm. Available: "sga", "sgde", "sgperm", "sge", "sgede", "sgp". Default: "sga".
method	Method. Options are package-dependent: <ul style="list-style-type: none"> • "sga", "sgperm", "sge", "sgp": "Kid1", "KidPipeline", "Kid2". • "sgde", "sgede": "DE", "DEPipeline".

Value

A replication function for the algorithm from the correct package.

See Also

Other Configuration: [sgXCrossoverFactory\(\)](#), [sgXDecodeGeneFactory\(\)](#), [sgXGeneMapFactory\(\)](#), [sgXInitGeneFactory\(\)](#), [sgXMutationFactory\(\)](#)

Examples

```
sgXReplicationFactory(algorithm="sgp", method="Kid1")
```

xega

Package xega

Description

The main program of the e(x)tended (e)volutionary and (g)enetic (a)lgorithm (xega) package.

Layers (in top-down direction)

1. **Top-level main programs** (Package `xega` <<https://CRAN.R-project.org/package=xega>>): `xegaRun()`, `xegaReRun()`
2. **Population-level operations - independent of representation** (Package `xegaPopulation` <<https://CRAN.R-project.org/package=xegaPopulation>>): The population layer consists of functions for initializing, logging, observing, evaluating a population of genes, as well as computing the next population.
3. **Gene-level operations - representation-dependent.**
 - (a) **Binary representation** (Package `xegaGaGene` <<https://CRAN.R-project.org/package=xegaGaGene>>): Initialization of random binary genes, several gene maps for binary genes, several mutation operators, several crossover operators with 1 and 2 kids, replication pipelines for 1 and 2 kids, and, last but not least, function factories for configuration.
 - (b) **Real-coded genes** (Package `xegaDfGene` <<https://CRAN.R-project.org/package=xegaDfGene>>).
 - (c) **Permutation genes** (Package `xegaPermGene` <<https://CRAN.R-project.org/package=xegaPermGene>>).
 - (d) **Derivation-tree genes** (Package `xegaGpGene` <<https://CRAN.R-project.org/package=xegaGpGene>>).

- (e) **Binary genes with a grammar-driven decoder** (Package `xegaGeGene` <<https://CRAN.project.org/package=xegaC>>)
- 4. **Gene-level operations - independent of representation** (Package `xegaSelectGene` <<https://CRAN.project.org/package=xegaC>>)
Functions for static and adaptive fitness scaling, gene selection, gene evaluation, as well as measuring performance and configuration.

Early Termination

A problem environment may implement a function `terminate(solution)` which returns `TRUE` if the solution meets a condition for early termination.

Genetic Operator Pipelines

In `xega` the extended gene life-cycle is:

- (sequential) ... -> gene (data structure) -> select -> replicate(crossover -> mutate -> accept)
- (parallelizable) -> decode -> evaluate -> gene (data structure) -> ...

Only the `decode -> evaluate` phase can be parallelized. The `select -> crossover -> mutate -> accept` phases are executed sequentially. For algorithms which require e.g. evaluation during the `accept` phase (simulated annealing variants), this organization implies that the improvement by parallel or distributed execution models is negligible.

A genetic operator pipeline embeds the `crossover -> mutate -> accept -> decode -> evaluate` phases into a function closure per gene. The evaluation of a population of genes can be evaluated in parallel with potentially high reductions in total run-time.

The gene life-cycle with genetic operator pipelines in `xega` is:

- (sequential) ... -> gene (data structure) -> select -> replicate pipeline -> gene (function closure)
- (parallelizable) -> evaluate -> gene (data structure) ...

This shifts the execution of the `crossover -> mutate -> accept -> decode -> evaluate` phases to the parallelizable evaluation of a function closure.

Parallel and Distributed Execution

Several implementations of a parallel `lapply()` function are provided. They support the parallel and distributed execution of fitness functions on several combinations of hard- and software architectures. A parallel `lapply()`-function must have the following abstract interface:

```
parallelApply(pop, EvalGene, lF)
```

where `pop` is a list of genes, `EvalGene` the evaluation function for the fitness of a gene, and `lF` the local function configuration of the algorithm.

The several implementations of a `parallelApply()` function are provided. The implementations use

- the function `parallel::mclapply()` for multi-core parallelization by the fork mechanism of Unix-based operating systems on a single machine.
- the function `parallel::parLapply()` for socket connections on a single or multiple machines on the Internet.

- the function `future.apply::future_lapply()` for asynchronous parallelization based on future packages.

In addition, user-defined parallel apply functions can be provided. Example scripts for using the `Rmpi::mpi.parLapply()` function of the `Rmpi` package are provided for an HPC environment with Slurm as well as on a notebook.

The Architecture of the xegaX-Packages

The xegaX-packages are a family of R-packages which implement e(x)tended (e)volutionary and (g)enetic (a)lgorithms (xega). The architecture has 3 layers, namely the user interface layer, the population layer, and the gene layer:

- The user interface layer (package `xega` <<https://CRAN.R-project.org/package=xega>>) provides a function call interface and configuration support for several algorithms: genetic algorithms (`sga`), permutation-based genetic algorithms (`sgPerm`), derivation-free algorithms as e.g. differential evolution (`sgde`), grammar-based genetic programming (`sgp`), and grammatical evolution (`sge`).
- The population layer (package `xegaPopulation` <<https://CRAN.R-project.org/package=xegaPopulation>>) contains population-related functionality as well as support for population statistics dependent adaptive mechanisms and for parallelization.
- The gene layer is split into a representation-independent and a representation-dependent part:
 1. The representation-independent part (package `xegaSelectGene` <<https://CRAN.R-project.org/package=xegaSelectGene>>) is responsible for variants of selection operators, evaluation strategies for genes, as well as profiling and timing capabilities.
 2. The representation-dependent part consists of the following packages:
 - `xegaGaGene` <<https://CRAN.R-project.org/package=xegaGaGene>> for binary-coded genetic algorithms.
 - `xegaPermGene` <<https://CRAN.R-project.org/package=xegaPermGene>> for permutation-based genetic algorithms.
 - `xegaDfGene` <<https://CRAN.R-project.org/package=xegaDfGene>> for derivation-free algorithms e.g. differential evolution.
 - `xegaGpGene` <<https://CRAN.R-project.org/package=xegaGpGene>> for grammar-based genetic algorithms.
 - `xegaGeGene` <<https://CRAN.R-project.org/package=xegaGeGene>> for grammatical evolution algorithms.

The packages `xegaDerivationTrees` and `xegaBNF` support the packages `xegaGpGene` and `xegaGeGene`:

- `xegaBNF` <<https://CRAN.R-project.org/package=xegaBNF>> essentially provides a grammar compiler and
- `xegaDerivationTrees` <<https://CRAN.R-project.org/package=xegaDerivationTrees>> an abstract data type for derivation trees.

Copyright

(c) 2023 Andreas Geyer-Schulz

License

MIT

URL<https://github.com/ageyerschulz/xega>**Installation**From CRAN by `install.packages('xega')`**Author(s)**

Andreas Geyer-Schulz

See Also

Useful links:

- <https://github.com/ageyerschulz/xega>

`xegaAnyTimeResult`*Writes xega results after each iteration to a rds file.*

Description

Writes xega results after each iteration to a rds file.

Usage

```
xegaAnyTimeResult(  
  mIT,  
  pp,  
  ft,  
  lF,  
  allsolutions,  
  popStat,  
  evalFail,  
  GAconfiguration,  
  path  
)
```

Arguments

m1T	Main loop timer function.
pp	Population.
ft	Fitness vector.
lF	Local function configuration.
allsolutions	Boolean.
popStat	Population statistics (mean, min, Q1, median, Q3, max, var, mad).
evalFail	Number of evaluation failures.
GAconfiguration	Configuration of the genetic algorithm.
path	File path.

Details

The file `xegaAnyTimeResult.rds` is overwritten after each generation. The function is intended to be used with the defaults (`xegaAnyTimeResult()`).

Value

Invisible 0.

xegaDebug	<i>Debug (show) progress in xegaRun main loop.</i>
-----------	--

Description

Debug (show) progress in xegaRun main loop.

Usage

```
xegaDebug(debug, msg = "debug message", obj = NULL)
```

Arguments

debug	Boolean. Default: FALSE. If TRUE, show msg and obj.
msg	Text message.
obj	R object.

Value

0 (invisible)

Examples

```
xegaDebug(debug=FALSE, msg="nothing is shown")
xegaDebug(debug=TRUE, msg="nothing is shown")
xegaDebug(debug=TRUE, msg="xegaDebug:", obj=xegaDebug)
```

xegaReRun	<i>Run an evolutionary or genetic algorithm with the same configuration as in the previous run.</i>
-----------	---

Description

xegaReRun() runs a simple genetic algorithm with the same configuration as in the run specified by the list element \$GAconfig of the solution of a simple genetic algorithm. The problem environment and the the grammar are extracted from the solution object.

If script==TRUE, the solution object and a R script to rerun xega are written to the current directory.

Usage

```
xegaReRun(solution, script = FALSE, fn = "xegaRunScript", ...)
```

Arguments

solution	The solution of a previous run of xegaRun().
script	Boolean. Default: FALSE. If TRUE, write an R script to repeat the xega run with the command in the solution object.
fn	Filename of R script. Default: xegaRunScript.R
...	List of named arguments of xega, you want to override.

Details

xegaReRun() does not capture the configuration for parallel/distributed processing for the execution model "FutureApply", because the user defines the configuration before calling xegaRun().

If executionModel matches neither "Sequential" nor "MultiCore" or !is.null(uParApply)==TRUE, a warning is printed, and xegaReRun() attempts the execution, but may fail, because the set up of the parallel environment has not been performed before xegaReRun.

Value

A list of

1. \$popStat: A matrix with mean, min, Q1, median, Q3, max, var, mad of population fitness as columns: i-th row for i-th each generation.
2. \$fit: Fitness vector if generations<=1 else: NULL.
3. \$solution: With fields \$solution\$name, \$solution\$fitness, \$solution\$value, \$numberOfSolutions, \$solution\$genotype, \$solution\$phenotype, \$solution\$phenotypeValue,
4. \$evalFail: Number of failures of fitness evaluations.
5. \$GAconfig: The configuration of the GA used by xegaReRun().
6. \$GAenv: Attribute value list of GAconfig.
7. \$timer: An attribute value list with the time used (in seconds) in the main blocks of the GA: tUsed, tInit, tNext, tEval, tObserve, and tSummary.

See Also

Other Main Program: [xegaRun\(\)](#)

Examples

```
a<-xegaRun(Parabola2D, max=FALSE, algorithm="sga", generations=10, popsize=20, verbose=1)
b<-xegaReRun(a)
seqApply<-function(pop, EvalGene, lF) {lapply(pop, EvalGene, lF)}
c<-xegaRun(Parabola2D, max=FALSE, algorithm="sga", uParApply=seqApply)
b<-xegaReRun(c)
```

xegaRun	<i>Run an evolutionary or genetic algorithm for a problem environment which contains a function to optimize.</i>
---------	--

Description

xegaRun() runs an evolutionary or genetic algorithm whose type is selected by algorithm. Available algorithms are:

1. "sga": Genetic algorithm with binary genes.
2. "sgde": Differential evolution with real genes.
3. "sgperm": Genetic algorithm with permutation genes.
4. "sgp": Grammar-based genetic programming with derivation-tree genes.
5. "sge": Grammatical evolution (genetic algorithm with binary genes and a grammar-driven decoder).
6. "sgede": Grammatical evolution (genetic algorithm with real genes, genetic operators from differential evolution and a grammar-driven decoder).

The choice of the algorithm determines the gene-dependent configuration options.

Usage

```
xegaRun(
  penv,
  grammar = NULL,
  max = TRUE,
  algorithm = "sga",
  popsize = 100,
  generations = 20,
  crossrate = 0.2,
  mutrate = 1,
  elitist = TRUE,
  replay = 0,
  maxdepth = 7,
```

```
maxtrials = 5,  
codons = 25,  
codonBits = 0,  
codonPrecision = "LCM",  
maxPBias = 0.01,  
evalmethod = "EvalGeneU",  
evalrep = 1,  
reportEvalErrors = TRUE,  
genemap = "Bin2Dec",  
decoder = "DecodeGene",  
crossrate2 = 0.3,  
ivcrossrate = "Const",  
crossover = "Cross2Gene",  
uCrossSwap = 0.2,  
mincrossdepth = 1,  
maxcrossdepth = 7,  
ivmutrate = "Const",  
mutrate2 = 1,  
bitmutrate = 0.005,  
bitmutrate2 = 0.01,  
maxmutdepth = 3,  
minmutinsertiondepth = 1,  
maxmutinsertiondepth = 7,  
lambda = 0.05,  
max2opt = 100,  
scalefactor1 = 0.9,  
scalefactor2 = 0.3,  
scalefactor = "Const",  
cutoffFit = 0.5,  
mutation = "MutateGene",  
replication = "Kid2",  
initgene = "InitGene",  
offset = 1,  
eps = 0.01,  
tournamentSize = 2,  
selectionBias = 1.5,  
maxTSR = 1.5,  
topK = 1,  
selection = "SUS",  
mateselection = "SUS",  
selectionContinuation = TRUE,  
scaling = "NoScaling",  
scalingThreshold = 0,  
scalingExp = 1,  
scalingExp2 = 1,  
rdmWeight = 1,  
drMax = 2,  
drMin = 0.5,
```

```

dispersionMeasure = "var",
scalingDelay = 1,
accept = "All",
alpha = 0.99,
beta = 2,
cooling = "ExponentialMultiplicative",
coolingPower = 1,
temp0 = 40,
tempN = 0.01,
verbose = 1,
logevals = FALSE,
allsolutions = FALSE,
early = FALSE,
terminationCondition = "NoTermination",
terminationEps = 0.01,
terminationThreshold = 0,
worstFitness = 0,
PACdelta = 0.01,
fSpace = "Hilbert",
cores = NA,
pipeline = "NoPipe",
executionModel = "Sequential",
uParApply = NULL,
Cluster = NULL,
profile = FALSE,
batch = FALSE,
anytime = FALSE,
path = ".",
semantics = "byValue",
debug = FALSE,
comment = NULL,
lastArgument = 0
)

```

Arguments

penv	Problem environment.
grammar	A compiled grammar object. Default: NULL. Example: <code>compileBNF(booleanGrammar())</code>
max	If TRUE then Maximize! Default: TRUE. Used in functions <code>EvalGeneDet</code> , <code>EvalGeneStoch</code> , <code>EvalGeneU</code> , and <code>EvalGeneR</code> of package <code>xegaSelectGene</code> .
algorithm	Specifies the algorithm class dependent on gene representation: <ul style="list-style-type: none"> • "sga": Binary representation (Default). • "sgde": Real representation. E.g. Differential evolution. • "sgperm": Permutation representation. • "sge": Binary representation. Grammatical evolution. (Not yet variable length.)

	<ul style="list-style-type: none"> • "sgede": Real representation. Genetic operators from differential evolution. Grammatical evolution. (Not yet variable length.) • "sgp": Derivation tree representation. Grammar Based Genetic Programming.
popsiz	Population size. Default: 100.
generations	Number of generations. Default: 20.
crossrate	Probability of applying crossover operator. Default: 0.20. (Global parameter)
mutrate	Probability of applying mutation operator. Default: 1.0. (Global parameter)
elitist	Boolean. If TRUE, then keep the best solution in the population. Default: TRUE.
replay	Integer. If replay>0, then use replay as the seed of the random number generator and store it for the exact repetition of this run. Default: 0.
maxdepth	The maximal depth of a derivation tree. Default: 7. ("sgp").
maxtrials	Maximal number of trials for finding subtrees with the same root symbol. Default: 5. (sgp).
codons	The maximal number of codons of derivations on a gene. Default: 25. ("sge").
codonBits	The number of bits of a codon. Default: 0. ("sge").
codonPrecision	Specify the method to set the number of bits of a codon ("sge"): <ul style="list-style-type: none"> • "Min": Sufficient to code the maximal number of choices of production rules for a non-terminal. • "LCM": Contains the least common multiple of the prime factors of the number of choices of production rules for all non-terminals. • "MaxPBias": The computed precision guarantees that the choice rule bias for a non-terminal is below maxPBias. Argument of function factory xegaGePrecisionFactory in package xegaGeGene.
maxPBias	The threshold of the choice rule bias. Default: 0.01. ("sge").
evalmethod	Specifies the method of function evaluation: <ul style="list-style-type: none"> • "EvalGeneU": The function is always evaluated. (Default) • "EvalGeneR": The function is always evaluated. Repairs of the gene by the decoder are possible. • "Deterministic": The function is evaluated only once. • "Stochastic": The expected function value and its variance are incrementally updated. Argument of function factory EvalGeneFactory in package xegaSelectGene.
evalrep	Specifies the number of repeated fitness evaluations of a (stochastic) function.
reportEvalErrors	Report errors in the evaluation of fitness functions. Default: TRUE.
genemap	Gene map for decoding. Default: "Bin2Dec". The default value works only for algorithm "sga". Used as method argument of the function factory sgXGeneMapFactory of package xega. <p>Available options determined by algorithm:</p> <ul style="list-style-type: none"> • "sga": Binary representation (Default).

- "Bin2Dec": For real parameter vectors.
- "Gray2Dec": For real parameter vectors.
- "Identity": For 0/1 parameter vectors.
- "Permutation": For permutations.

See the function factory `xegaGaGeneMapFactory` in package `xegaGaGene`.

- "sgp": Derivation tree. Gene map is not used, but must be specified. We use `xegaGaGene::xegaGaGeneMapFactory` with `method="Identity"`.
- "sge": Binary representation (Default). How are genes decoded?
 - "Mod": The modulo rule.
 - "Bucket": The bucket rule (with the mLCM). Problem: Mapping $1:2^k$ to $1:mLCMG$.

See the function factory `xegaGeGeneMapFactory` in package `xegaGeGene`.

- "sgde": Real coded gene. We use `xegaDfGene::xegaDfGeneMapFactory` with `method="Identity"`. Function used: `xegaDfGene::xegaDfGeneMapIdentity`
- "sgperm": Permutation gene. Gene map is not used, but must be specified. We use `xegaDfGene::xegaDfGeneMapFactory` with `method="Identity"`. Function used: `xegaDfGene::xegaDfGeneMapIdentity`

decoder	Specifies a decoder for a gene, Default: "DecodeGene". For algorithm <code>sge</code> , a second decoder is available: <code>DecodeGeneDT</code> . This decoder is faster, but it may generate code which still contains non-terminal symbols and which does not work.
crossrate2	Crossover rate for genes with below "average" fitness. Probability of applying crossover operator for genes with a "below average" fitness. Default: 0.30. (Global parameter)
ivcrossrate	Specifies the method of determining the crossover rate. <ul style="list-style-type: none"> • "Const" Constant crossover rate. The probability of applying the crossover operator is constant for the whole run of the algorithm. Default: "Const". • "IV" Individually variable crossover rate. The <code>crossrate</code> of a gene is determined by the following threshold rule: If the fitness of the gene is higher than $1F\\$CutoffFit() * 1F\\$CBestFitness()$, then $1F\\$CrossRate1()$ else $1F\\$CrossRate2()$ is used. Argument of function factory <code>CrossRateFactory</code> in package <code>xegaPopulation</code> .
crossover	Crossover method. Default: "Cross2Gene". The choice of crossover methods depends on the setting of the argument <code>algorithm</code> . Used as the method argument in function factory <code>sgXCrossoverFactory</code> of package <code>xega</code> . <ul style="list-style-type: none"> • <code>algorithm="sga"</code>: crossover is an argument of function factory <code>xegaGaCrossoverFactory</code> in package <code>xegaGaGene</code>. <ul style="list-style-type: none"> - Crossover operators with 1 kid: <ul style="list-style-type: none"> * "CrossGene" one-point crossover. * "UCrossGene" uniform crossover. * "UPCrossgene" parameterized uniform crossover. Local parameter: <code>uCrossSwap</code>. - Crossover operators with 2 kids: <ul style="list-style-type: none"> * "Cross2Gene" one-point crossover.

- * "UCross2Gene" uniform crossover.
 - * "UPCross2gene" parameterized uniform crossover. Local parameter: uCrossSwap.
 - algorithm="sgp": crossover is an argument of function factory xegaGpCrossoverFactory in package xegaGpGene.
 - Crossover operators with 1 kid:
 - * "AllCrossGene" position-based one-point crossover.
 - Crossover operators with 2 kids:
 - * "Cross2Gene" position-based one-point crossover.
 - algorithm="sge": We use the factory xegaGaCrossoverFactory. (Adaptation needed for variable-length binary representation.)
 - algorithm="sgde": crossover is an argument of function factory xegaDfCrossoverFactory in package xegaDfGene.
 - Crossover operators with 1 kid:
 - * "CrossGene" one-point crossover (of reals)
 - * "UCrossGene" uniform crossover (of reals)
 - * "UPCrossGene" parametrized uniform crossover (of reals). Local parameter: uCrossSwap.
 - Crossover operators with 2 kids: Not implemented.
 - algorithm="sgperm": crossover is an argument of function factory xegaPermCrossoverFactory in package xegaPermGene.
 - Crossover operators with 1 kid:
 - * "CrossGene" position-based one-point crossover.
 - Crossover operators with 2 kids:
 - * "Cross2Gene" position-based one-point crossover.
- uCrossSwap The fraction of positions swapped in the parametrized uniform crossover operator. A local crossover parameter. Default: 0.2. ("sga" and "sgde"). Used in packages xegaGaGene and xegaDfGene for functions xegaGaUPCross2Gene, xegaDfUPCross2Gene, xegaGaUPCrossGene, and xegaDfUPCrossGene.
- mincrossdepth minimal depth of exchange nodes (roots of subtrees swapped by crossover). ("sgp").
- maxcrossdepth Maximal depth of exchange nodes (roots of subtrees swapped by crossover). ("sgp"). Used in package xegaGpGene functions xegaGpCrossGene and xegaGpCross2Gene in package xegaGpGene.
- ivmutrate "Const" or "IV" (individually variable). Default: "Const".
- mutrate2 Mutation rate. Default: 1.0. (Global parameter).
- bitmutrate Bit mutation rate. Default: 0.005. A local mutation parameter. ("sga" and "sge"). Used in package xegaGaGene functions MutateGene IVAdaptiveMutateGene
- bitmutrate2 Bit mutation rate for genes with "below average" fitness. Default: 0.01. A local mutation parameter. ("sga" and "sge"). Used in package xegaGaGene functions IVAdaptiveMutateGene
- maxmutdepth Maximal depth of a derivation tree inserted by a mutation operation. Default: 3. ("sgp").

minmutinsertiondepth	Minimal depth at which an insertion tree is inserted. Default: 1. ("sgp").
maxmutinsertiondepth	Maximal depth at which an insertion tree is inserted. Default: 7. ("sgp"). Used in package xegaGpGene function xegaGpMutateGene.
lambda	Decay rate. Default: 0.05. A local mutation parameter. ("sgperm"). Used in package xegaPermGene function xegaPermMutateGeneKInversion.
max2opt	Maximal number of trials to find an improvement by a random edge exchange in a permutation. Default: 100. ("sgperm"). Used in package xegaPermGene function xegaPermMutateGene20pt and xegaPermMutateGeneOptLK.
scalefactor1	Scale factor for differential mutation operator (Default: 0.9). ("sgde").
scalefactor2	Scale factor for differential mutation operator (Default: 0.2). ("sgde").
scalefactor	Method for setting scale factor ("sgde"): <ul style="list-style-type: none"> • "Const": Constant scale factor configured by scalefactor1. • "Uniform": A random scale factor in the interval from 0.000001 to 1.0. • "DERSF": A random scale factor in the interval from 0.5 to 1.0. • "DETVSF": The scale factor is linear decaying from an upper bound (scalefactor1==0.9) to a lower bound (scalefactor2==0.2) with the number of generations. • "CauchySF": Bounded Cauchy distributed scale factor with a scale parameter which increases with the number of generations. • "FBSASF": Fitness based self adaptive scale factor. • "RGSF": Random Gaussian scale factor (Random pick of a random number from either $\text{abs}(\text{rnorm}(1, 0.3, 0.3))$ or $\text{abs}(\text{rnorm}(1, 0.7, 0.3))$).
cutoffFit	Cutoff for fitness. Default: 0.5. ("sga" and "sge"). Used in package xegaGaGene function IVAdaptiveMutateGene.
mutation	Label specifies the mutation method dependent on algorithm. Default: "MutateGene". The (global) probability of calling a mutation method is specified by mutrate and mutrate2. Used as method argument of the function factory sgXMutationFactory in package xega. <ul style="list-style-type: none"> • algorithm="sga": mutation is an argument of function factory xegaGaMutationFactory in package xegaGaGene. <ul style="list-style-type: none"> – "MutateGene": Bitwise mutation. Local parameter: bitmutrate. Function used: xegaGaGene::xegaGaMutateGene. – "IVM": Individually variable mutation. Intuitively, we know that bad genes need higher mutation rates. Good genes have a fitness which is above a threshold fitness. The threshold is determined as a percentage of the current best fitness in the population. The percentage is set by the parameter cutoffFit. Local parameters: bitmutrate for good genes. bitmutrate2 for bad genes. bitmutrate2 should be higher than bitmutrate. • algorithm="sgp": mutation is an argument of function factory xegaGpMutationFactory in package xegaGpGene. <ul style="list-style-type: none"> – "MutateGene": Random insertion of a random derivation tree. Local parameter: maxmutdepth. Function used: xegaGpGene::xegaGpMutateGene.

- `algorithm="sge"`: mutation is an argument of function factory `xegaGaMutationFactory`. Nothing specific to grammatical evolution has been implemented.
- `algorithm="sgde"`: mutation is an argument of function factory `xegaDfMutationFactory` in package `xegaDfGene`.
 - `"MutateGene"`: Add the scaled difference of the parameters of two randomly selected to a gene. Local parameters: Choice of function for `scalefactor` as well as `scalefactor1` and `scalefactor2`. Function used: `xegaDfGene::xegaDfMutateGeneDE`.
- `algorithm="sgperm"`: mutation is an argument of function factory `xegaPermMutationFactory` in package `xegaPermGene`.
 - `"MutateGene"`: Function used: `xegaPermGene::xegaPermMutateGeneOrderBased`.
 - `"MutateGeneOrderBased"`: See `"MutateGene"`.
 - `"MutateGenekInversion"`: Function used: `xegaPermGene::xegaPermMutateGenekInversion`.
 - `"MutateGene2Opt"`: Function used: `xegaPermGene::xegaPermMutateGene2Opt`.
 - `"MutateGenekOptLK"`: Function used: `xegaPermGene::xegaPermMutateGenekOptLK`.
 - `"MutateGeneGreedy"`: Function used: `xegaPermGene::xegaPermMutateGeneGreedy`.
 - `"MutateGeneBestGreedy"`: Function used: `xegaPermGene::xegaPermMutateGeneBestGreedy`.
 - `"MutateGeneMix"`: Function used: `xegaPermGene::xegaPermMutateMix`.

`replication` "Kid1", "Kid1Pipeline", "Kid1PipelineG", "Kid2", "Kid2Pipeline" or "Kid2PipelineG".

Default: "Kid1". For algorithms "sga", "sgPerm", "sgp", and "sge": "Kid1" means a crossover operator with one kid. "Kid1Pipeline" means a function closure with a genetic operator pipeline is returned. "Kid1PipelineG" means a gene with a genetic operator pipeline embedded is returned. "Kid2" means a crossover operator with two kids. "Kid2Pipeline" means a function closure with a genetic operator pipeline is returned. "Kid2PipelineG" means a gene with a genetic operator pipeline embedded is returned.

For algorithms "sgde" and "sgede", replication must be set to "DE", "DEPipeline", or "DEPipelineG".

The pipeline versions of replication requires to set `pipeline="PipeC"` or `pipeline="PipeG"` too.

The pipeline versions of replication generate either a genetic operator pipeline as a function closure or a genetic operator pipeline embedded in a gene. We call this transformation pipeline compilation. The execution of the function closures or of the gene embedded pipelines is shifted to the evaluation step and, thus, can be parallelized.

When genetic operator pipelines are used, the gene representation of the population vector cycles

- either between function closures and named lists as elements (`pipeline="PipeC"`)
- or between genes extended with a list element `$Pipeline()` with the genetic operator pipeline and the needed additional genes (1 for crossover, 3 for differential evolution) and a normal gene without these elements (`pipeline="PipeG"`).

Used as the method argument of the function factory `sgXReplicationFactory` of package `xega`.

`initgene` Default: "InitGene". For algorithm "sgp",

	<ol style="list-style-type: none"> 1. "InitGene": Random derivation tree. 2. "InitGeneGe": Random derivation tree from random integer vector.
offset	Offset used in proportional selection. Default: 1. Used in the following functions of package xegaSelectGene: ScaleFitness, PropFitOnLn, PropFit, PropFitM, PropFitDiffOnLn, PropFitDiff, SUS.
eps	Epsilon in proportional fitness difference selection. Default: 0.01. Used in package xegaSelectGene function PropFitDiffM.
tournamentSize	Tournament size. Default: 2. Used in package xegaSelectGene functions SelectTournament, SelectSTournament.
selectionBias	(> 1.0). Controls selection pressure for Whitley's linear rank selection with selective pressure. Default: 1.5. Near 1.0: almost uniform selection. Used in package xegaSelectGene function SelectLRSelective,
maxTSR	Controls selection pressure for Grefenstette and Baker's linear rank selection method. Should be higher than 1.0 and lower equal 2.0. Default: 1.5. Used in package xegaSelectGene function SelectLinearRankTSR.
topK	Controls the number of the best genes selected.
selection	Selection method for the first parent of crossover. Default: "SUS".
mateselection	Selection method for the second parent of crossover. Default: "SUS". Available selection methods for the selection method of a parent: <ul style="list-style-type: none"> • Uniform random selection: "Uniform". • Uniform random selection without replacement: "UniformP". • Proportional to fitness: "ProportionalOnln" (fastest), "Proportional", "ProportionalM", • Proportional to fitness differences: "PropFitDiffOnln" (fastest), "PropfitDiff", "PropfitDiffM", • Stochastic universal sampling: "SUS", • Tournament selection: "Duel" (fastest), "Tournament", "STournament", • Rank selection: "LRSelective" (fastest), "LRTSR". • Best k genes: "TopK".
selectionContinuation	Argument of function factory SelectGeneFactory in package xegaSelectGene. Boolean. If TRUE, precomputes selection indices for next generation once and transforms selection function to index lookup continuation. Default: TRUE. Used in package xegaPopulation function xegaNextPopulation.
scaling	Scaling method. Default: "NoScaling". Available scaling methods: <ul style="list-style-type: none"> • "NoScaling", • "ConstantScaling" (Static), • "ThresholdScaling" (Dynamic), • "ContinuousScaling" (Dynamic).
scalingThreshold	Argument of function factory ScalingFactory in package xegaSelectGene. Numerical constant. Default: 0.0. If the ratio of dispersion measures is in [(1-scalingThreshold), 1+scalingThreshold], fitness is not scaled. Used in package xegaSelectGene function ThresholdScaleFitness.

scalingExp	Scaling exponent k in fit^k . With "ConstantScaling": $0 \leq k$. With "ThresholdScaling": $1 < k$. (Default: 1) Used in package xegaSelectGene, functions ScalingFitness, ThresholdScaleFitness.
scalingExp2	Scaling exponent for "ThresholdScaling": $0 \leq k < 1$. (Default: 1) Used in package xegaSelectGene function ThresholdScaleFitness.
rdmWeight	Numerical constant. Default: 1.0. Weight of ratio of dispersion measures in continuous scaling. Used in package xegaSelectGene function ContinuousScaleFitness.
drMax	Maximal allowable dispersion ratio. Default: 2.0. Used in package xegaSelectGene function DispersionRatio.
drMin	Minimal allowable dispersion ratio. Default: 0.5. Used in package xegaSelectGene function DispersionRatio.
dispersionMeasure	Dispersion measure specifies a concrete dispersion measure of the population's fitness vector at generation k . (e.g. the variance of the population fitness). In dynamic scaling methods the ratio of dispersion measures at k and $k-j$ is often used to adapt the selection pressure. Default: "var". Available dispersion measures: "var", "std", "mad", "cv", "range", "iqr". Argument of function factory DispersionMeasureFactory in package xegaSelectGene.
scalingDelay	The ratio of dispersion measures compares the current population dispersion at t with the population dispersion at t -scalingdelay. Default: 1. Used in package xegaSelectGene function DispersionRatio.
accept	Acceptance rule for a new gene. Default: "All". <ul style="list-style-type: none"> • "All" function AcceptNewGene • "Best" function AcceptBest • "Metropolis" function AcceptMetropolis. The behavior of this acceptance rule depends on: <ol style="list-style-type: none"> 1. The distance between the fitness values. The larger the distance, the larger the drop in acceptance probability. 2. α is 1 minus the discount rate of the cooling schedule. α is in $[0, 1]$. The smaller the α, the faster the drop in temperature and thus acceptance probability. 3. β a constant. The larger the β, the faster the drop in acceptance probability. 4. temperature the starting value of the temperature. Must be higher than the number of generations. • "IVMetropolis" function AcceptIVMetropolis. The behavior of this acceptance rule is qualitatively the same as that of the Metropolis acceptance rule above. The acceptance rule is adaptive by a correction of the temperature in proportion to the difference between the fitness of the current best and the fitness of the gene considered. <p>Argument of function factory AcceptFactory in package xegaPopulation.</p>
alpha	1 minus the discount rate for temperature. (Default: 0.99). (Used in the cooling schedule at the end of main GA-loop.)
beta	Constant in the Metropolis acceptance rule. (Default: 2.0). (Used in the Metropolis acceptance rule.)

cooling	<p>Cooling schedule for temperature. (Default: "ExponentialMultiplicative")</p> <ul style="list-style-type: none"> • "ExponentialMultiplicative" calls ExponentialMultiplicativeCooling • "LogarithmicMultiplicative" calls LogarithmicMultiplicativeCooling • "PowerMultiplicative" calls PowerMultiplicativeCooling • "PowerAdditive" calls PowerAdditiveCooling • "ExponentialAdditive" calls ExponentialAdditiveCooling • "TrigonometricAdditive" calls TrigonometricAdditiveCooling <p>Argument of function factory CoolingFactory in package xegaPopulation.</p>
coolingPower	Exponent for PowerMultiplicative cooling schedule. (Default: 1. This is called linear multiplicative cooling.)
temp0	Starting value of temperature (Default: 40). (Used in the Metropolis acceptance rule. Updated in the cooling schedule.)
tempN	Final value of temperature (Default: 0.01). (Used in the Metropolis acceptance rule. Updated in the cooling schedule.)
verbose	<p>The value of verbose (Default: 1) controls the information displayed:</p> <ol style="list-style-type: none"> 1. == 0: Nothing is displayed. 2. == 1: 1 point per generation. 3. > 1: Max(fit), number of solutions, indices. 4. > 2: and population fitness statistics. 5. > 3: and fitness, value of phenotype, and phenotype. 6. > 4: and str(genotype).
logevals	<p>Boolean. If TRUE then log all evaluations and their parameters in the file xegaEvalLog<exclusive pattern>.rds. Default: FALSE.</p> <p>log<-readRDS(xegaEvalLog<exclusive pattern>.rds) reads the log. The log is a list of named lists with the following elements:</p> <ul style="list-style-type: none"> • \$generation: The generation. • \$fit: The fitness value. • \$sigma: The standard deviation of the fitness value, if it exists. Default: 0. • \$obs: The number of observations for computing the fitness value, if it exists. Default: 0. • \$phenotype: The phenotype of the gene.
allsolutions	Boolean. If TRUE, then return all the best solutions. Default: FALSE.
early	Boolean. If FALSE (Default), ignore the code for early termination. See Parabola2DEarly .
terminationCondition	<p>Termination condition. Available:</p> <ul style="list-style-type: none"> • "NoTermination" (Default). • "AbsoluteError": Algorithm ends if current optimum is in optimum +/- terminationEps. • "RelativeError": Algorithm ends if current optimum is in optimum +/- terminationEps*optimum. If the optimum is 0, the interval has length 0.

- "RelativeErrorZero": Algorithm ends if current optimum is in optimum +/- terminationEps*optimum. If the optimum is 0, the interval is from -terminationEps to terminationEps.
- "PAC": Algorithm ends if current optimum is in ub +/- terminationEps*optimum. If ub is 0, the interval is from -terminationEps to terminationEps. ub is an estimated upper PAC bound for the global optimum. The probability that the optimum is above ub is set by PACdelta. The epsilon environment by terminationEps.
- "GEQ": Algorithm ends if the current optimal phenotype value is greater or equal than terminationThreshold.
- "LEQ": Algorithm ends if the current optimal phenotype value is less or equal than terminationThreshold.

terminationEps Fraction of the known optimal solution for computing termination interval. Default: 0.01. See [Parabola2DEarly](#).

terminationThreshold A threshold for terminating the algorithm. Default: 0.0.

worstFitness Set the worst fitness. Default: 0.0. Used e.g. in evalgeneU() for giving genes whose evaluation failed a very low fitness value to decrease their survival rate into the next generation.

PACdelta $P(\text{ub} < \text{opt}) < \text{PACdelta}$. Default: 0.01.

fSpace Function space of fitness function. Default: "Hilbert".

cores Number of cores used for multi-core parallel execution. (Default: NA. NA means that the number of cores is set by `parallelly:availableCores()` if the execution model is "MultiCore" or "MultiCoreHet".

pipeline Method of pipeline compilation. Default: "NoPipe".

- "NoPipe": No pipeline compilation.
- "PipeC": Pipeline compilation generates a population of function closures of genetic operator pipelines which can be executed in parallel.
- "PipeG": Pipeline compilation generates a population of genes with embedded genetic operator pipelines which can be executed in parallel.

executionModel Execution model of fitness function evaluation. Available:

- "Sequential": `base::lapply` is used.
- "MultiCore": `parallel::mclapply` is used.
- "MultiCoreHet": `parallel::mclapply` is used. For tasks with a high variance in execution time.
- "FutureApply": `future.apply::future_lapply` is used. Requires the specification of a plan.
- "FutureApplyHet": `future.apply::future_lapply` is used. For tasks with a high variance in execution time. Requires the specification of a plan.
- "Cluster": `parallel::parLapply` is used. Requires a proper configuration of the cluster and the specification of an exit handler to shutdown the cluster.
- "ClusterHet": `parallel::parLapplyLB` is used. Requires a proper configuration of the cluster and the specification of an exit handler to shutdown the cluster. For tasks with a high variance in execution time.

	Default: "Sequential".
uParApply	A user-defined parallel apply function (e.g. for Rmpi). If specified, overrides settings for executionModel. Default: NULL.
Cluster	A cluster object generated by parallel::makeCluster() or parallelly::makeCluster(). Default: NULL.
profile	Boolean. If TRUE measures execution time and counts the number of executions of the main components of genetic algorithms. Default: FALSE.
batch	Boolean. If TRUE, then save the result in the file path/xegaResult<exclusive pattern>.rds. Default: FALSE.
anytime	Boolean. If TRUE, then save the current best result in the file path/xegaAnyTimeResult.rds. Default: FALSE.
path	Path. Default: ".".
semantics	Determines the representation of the local function list lF. Default: "byValue". <ul style="list-style-type: none"> • "byValue": lF is a named list object. • "byReference": lF is an environment.
debug	Boolean. Default: FALSE. Debug (show) progress in xegaRun main loop.
comment	A text. Default: NULL. Comments may document e.g. hardware configurations for xega in external scripts.
lastArgument	Not used. Default: 0.

Details

The algorithm expects a problem environment env which is a named list with at least the following functions:

- \$name(): The name of the problem environment.
- \$f(parm, gene=0, lF=0): The function to optimize. The parameters gene and lF are provided for future extensions.

Additional parameters needed depend on the algorithm and the problem environment. For example, for binary genes for function optimization, additional elements must be provided:

- \$bitlength(): The vector of the bitlengths of the parameters.
- \$genelength(): The number of bits of a gene.
- \$lb(): The vector of lower bounds of the parameters.
- \$ub(): The vector of upper bounds of the parameters.

Value

Result object. A named list of

1. \$popStat: A matrix with mean, min, Q1, median, Q3, max, variance, and median absolute deviation of population fitness as columns: i-th row for the measures of the i-th generation.
2. \$fit: Fitness vector if generations<=1 else: NULL.
3. \$solution: Named list with fields

- `$solution$name`: Name of problem environment.
 - `$solution$fitness`: Fitness value of the best solution.
 - `$solution$value`: The evaluated best gene.
 - `$solution$numberofsolutions`: Number of solutions with the same fitness.
 - `$solution$genotype`: The gene is a genetic code.
 - `$solution$phenotype`: The decoded gene.
 - `$solution$phenotypeValue`: The value of the function of the parameters of the solution.
 - `$solution$evalFail`: Number of failures or fitness evaluations
 - and, if configured, `$solution$allgenotypes`, as well as `$solution$allphenotypes`.
4. `$GAconfig`: For rerun with `xegaReRun()`.
 5. `$GAenv`: Attribute value list of `GAconfig`.
 6. `$timer`: An attribute value list with the time used (in seconds) in the main blocks of the GA: `tUsed`, `tInit`, `tNext`, `tEval`, `tObserve`, and `tSummary`.
 7. `$logfn`: File name of logfile. Default: NA.
 8. `$resfn`: File name of RDS-file with result. Default: NA.
 9. `$xegaVersion`: xega version used.

Problem Specification

The problem specification consists of

- `penv`: The problem environment.
- `max`: Maximize? Boolean. Default: TRUE.
- `grammar`: A grammar object. For the algorithms "sgp" and "sge".

Basic Parameters

The main parameters of a "standard" genetic algorithm are:

- `popsize`: Population size.
- `generations`: Number of generations.
- `crossrate`: Constant probability of one-point crossover.
- `mutrate`: Constant probability of mutation.

`crossrate` and `mutrate` specify the probability of applying the genetic operators crossover and mutation to a gene.

Two more parameters are important:

- `elitist`: Boolean. If TRUE (default), the fittest gene always survives.
- `replay`: Integer. If 0 (default), a random seed of the random number generator is chosen. For exact replications of a run of a genetic algorithm, set `replay` to a positive integer.

Global and Local Parameters

However, when using uniform crossover instead of one-point crossover, an additional parameter which specifies the probability of taking a bit from the first parent becomes necessary. Therefore, we distinguish between global and local operator parameters:

1. Global operator parameters: The probabilities of applying a crossover (`crossrate`) or a mutation operator (`mutrate`) to a gene.
2. Local operator parameters: E.g. the per-bit probability of mutation or the probability of taking a bit from parent 1 for the uniform crossover operator. Local operator parameters affect only the genetic operator which needs them.

There exist several advantages of this classification of parameters:

- For the formal analysis of the behavior of the algorithms, we achieve a division in two parts: The equations of the global parameters with operator-specific expressions as plug-ins.
- For empirically finding parameterizations for problem classes, we propose to fix local parameters at reasonable values (e.g. based on biological evidence) and conditional on this optimize the (few) remaining global parameters.
- For parallelization, specialized gene processing pipelines can be built and more efficiently executed, because the global parameters `crossrate` and `mutrate` decide which genes survive
 1. unchanged,
 2. mutated,
 3. crossed, and
 4. crossed as well as mutated.

To mimic a classic genetic algorithm with crossover and bit mutation rate, the probability of applying the mutation operator to a gene should be set to `mutrate=1`.

Global Adaptive Mechanisms

The adaptive mechanisms described in the following are based on threshold rules which determine how a parameter of the genetic operator is adapted. The threshold conditions are based on population statistics:

Adaptive Scaling. For adaptive scaling, select a dynamic scaling method, e.g. `scaling="ThresholdScaling"`. A high selection pressure decreases the dispersion in the population. The parameter `scalingThreshold` is a numerical parameter which defines an interval from $1 - \text{scalingThreshold}$ to $1 + \text{scalingThreshold}$:

1. If the RDM is in this interval, the fitness function is not scaled.
2. If the RDM is larger than the upper bound of the interval, the constant `scalingExp` which is higher than 1 is chosen for the scaling function. This implements the rule: If the dispersion has increased, increase the selection pressure.
3. If the RDM is smaller than the lower bound of the interval, the constant `scalingExp2` which is smaller than 1 is chosen for the scaling function. This implements the rule: If the dispersion has decreased, increase the selection pressure.

The dispersion measure is computed as the ratio of the dispersion measure at t relative to the dispersion measure at $t - \text{scalingDelay}$. The default dispersion measure is the variance of the population

fitness (dispersionMeasure="var"). However, other dispersion measures ("std", "mad", "cv", "range", "iqr") can be configured.

Another adaptive scaling method is continuous scaling (scaling="ContinuousScaling"). The scaling exponent is adapted by a weighted ratio of dispersion measures. The weight of the exponent is set by `rdmWeight=1.1`, its default is `1.0`. Since the ratio of dispersion measures may be quite unstable, the default limits for the ratio are `drMin=0.5` and `drMax=2.0`.

Individually Variable Mutation and Crossover Probabilities

The rationale of individually variable mutation and crossover rates is that selected genes with a low fitness should be changed by a genetic operator with a higher probability. This increases the chance of survival of the gene because of the chance of a fitness increase through crossover or mutation.

Select an adaptive genetic operator rate: For the crossover rate, `ivcrossrate="IV"`. For the mutation rate, `ivmutrate="IV"`.

If the fitness of a gene is higher than `cutoffFit` times the current best fitness, the crossover rate is `crossrate` else the crossover rate is `crossrate2`.

If the fitness of a gene is higher than `cutoffFit` times the current best fitness, the mutation rate is `mutrate` else the mutation rate is `mutrate2`.

The Initialization of a Population

For the algorithms "sga", "sgde", and "sgperm" the information needed for initialization is the length of the gene in bits, in parameters, and in the number of symbols of a permutation. For "sgp", the depth bound gives an upper limit for the program which can be represented by a derivation tree. For "sge", a codon is an integer for selecting a production rule. The number of bits of a gene is `codons*codonBits`.

Algorithm		Parameters
"sga"	Number of bits.	<code>penv\$genelength()</code>
"sgde"	Number of parameters.	<code>length(penv\$bitlength(), penv\$lb(), penv\$sub())</code>
"sgede"	Number of Codons.	<code>codons, codonPrecision</code>
"sgperm"	Number of symbols.	<code>penv\$genelength()</code>
"sgp"	Depth bound of derivation tree.	<code>maxdepth</code>
"sge"	Number of codons and number of bits of a codon.	<code>codons, codonBits, codonPrecision, maxPBias</code>

The Pipeline of Genetic Operators

The pipeline of genetic operators merges the pipeline of a genetic algorithm with the pipeline of evolutionary algorithms and simulated annealing by adding an acceptance step:

- For evolutionary algorithms, the acceptance rule `accept="Best"` means that the fitter gene out of a parent and its kid survives (is copied into the next generation).
- For genetic algorithms the acceptance rule `accept="All"` means that always the kid survives.
- For simulated annealing the acceptance rule `accept="Metropolis"` means that the survival probability of a kid with a fitness worse than its parent decreases as the number of generations executed increases.
- The evaluation of the operator pipeline can be shifted to the evaluation phase by pipeline compilation:

- pipeline="PipeC": (population of function closures of genetic operator pipelines) or
- pipeline="PipeG": (population of genes with embedded genetic operator pipelines).

Proper configuration of the pipeline allows the configuration of new algorithm variants which mix elements of genetic, evolutionary, and simulated annealing algorithms.

The following table gives a working standard configuration of the pipeline of the genetic operators for each of the five algorithms:

Step/Algorithm	"sga"	"sgde"	"sgperm"
(next) Scaling	NoScaling	NoScaling	NoScaling
(next) Selection	SUS	UniformP	SUS
(next) Replication	Kid2	DE	Kid2
(next) Crossover	Cross2Gene	UCrossGene	Cross2Gene
(next) Mutation	MutateGene	MutateGeneDE	MutateGene
(next) Acceptance	All	Best	All
(eval) Decoder	Bin2Dec	Identity	Identity
(eval) Evaluation	EvalGeneU	EvalGeneU	EvalGeneU

Step/Algorithm	"sgp"	"sge"	"sgede"
(next) Scaling	NoScaling	NoScaling	NoScaling
(next) Selection	SUS	SUS	UniformP
(next) Replication	Kid2	Kid2	DE
(next) Crossover	Cross2Gene	Cross2Gene	UCrossGene
(next) Mutation	MutateGene	MutateGene	MutateGeneDE
(next) Acceptance	All	All	Best
(eval) Decoder	-	Mod	Identity
(eval) Evaluation	EvalGeneU	EvalGeneU	EvalGeneU

Scaling

In genetic algorithms, scaling of the fitness functions has the purpose of increasing or decreasing the selection pressure. Two classes of scaling methods are available:

- Constant scaling methods.
 - No scaling (configured by scaling="NoScaling").
 - Constant scaling (configured by scaling="ConstantScaling"). Depends on the scaling exponent scalingExp.
- Adaptive scaling methods.
 - Threshold scaling (configured by scaling="ThresholdScaling"). It is configured with the scaling exponents scalingExp and scalingExp2, and the scaling threshold scalingThreshold. It uses a threshold rule about the change of a dispersion measure of the population fitness $1F\$RDM()$ to choose the scaling exponent:
 - * $1F\$RDM() > 1 + \text{scalingThreshold}$: The scaling exponent is scalingExp which should be greater than 1. Rationale: Increase selection pressure to reduce the dispersion of fitness.

- * $1F\$RDM() < 1 - \text{scalingThreshold}$: The scaling exponent is scalingExp2 which should be lower than 1. Rationale: Decrease selection pressure to increase the dispersion of fitness.
- * Else: Scaling exponent is 1. Fitness is not scaled.
- Continuous scaling (configured by $\text{scaling} = \text{"ContinuousScaling"}$). The ratio of the dispersion measures $1F\$RDM()$ is greater than 1 if the dispersion increased in the last generation and less than 1 if the dispersion decreased in the last generation. The scaling exponent is the product of the ratio of the dispersion measures $1F\$RDM()$ with the weight rdmWeight .

The change of the dispersion measure of the population fitness is measured by the function $1F\$RDM()$ (RDM means (R)atio of (D)ispersion (M)easure). This function depends on

- the choice of a dispersion measure of the population fitness dispersionMeasure . The variance is the default ($\text{dispersionMeasure} = \text{"var"}$). The following dispersion measures of the population fitness are available: Variance ("var"), standard deviation ("std"), median absolute deviation ("mad"), coefficient of variation ("cv"), range ("range"), interquartile range ("iqr").
- the scaling delay scalingDelay . The default is $\text{scalingDelay} = 1$. This means the ratio of the variance of the fitness of the population at time t and the variance of the fitness of the population at time $t-1$ is computed.
- the upper and lower bounds of the ratio of dispersion measures.
- Dispersion ratios may have extreme fluctuations: The parameters drMax and drMin define upper and lower bounds of the ratio of dispersion measures. The defaults are $\text{drMax} = 2$ and $\text{drMin} = 1$.

See package `xegaSelectGene` <<https://CRAN.R-project.org/package=xegaSelectGene>>

Selection

Selection operators determine which genes are chosen for the replication process for the next generation. Selection operators are configured by selection and mateselection (the 2nd parent for crossover). The default operator is stochastic universal selection for both parents (configured by $\text{selection} = \text{"SUS"}$ and $\text{mateselection} = \text{"SUS"}$). The following operators are implemented:

- Uniform random selection with replacement (configured by "Uniform"). Needed for simulating uniform random mating behavior, for computer experiments without selection pressure, and for computing random search solutions as naive benchmarks.
- Uniform random selection without replacement (configured by "UniformP"). Needed for differential evolution.
- Selection proportional to fitness (in $O(n)$ by "SelectPropFit" , in $O(n \cdot \log(n))$ by $\text{"SelectPropFitOnln"}$, and in $O(n^2)$ by "SelectPropFitM"). offset configures the shift of the fitness vector if $\text{min(fit)} = < 0$.
- Selection proportional to fitness differences (in $O(n)$ by $\text{"SelectPropFitDiff"}$, in $O(n \cdot \log(n))$ by $\text{"SelectPropFitDiffOnln"}$, and in $O(n^2)$ by $\text{"SelectPropFitDiffM"}$). Even the worst gene should have a minimal chance of survival: eps is added to the fitness difference vector. This also guarantees numerical stability for populations in which all genes have the same fitness.

- Deterministic tournament selection of k genes (configured by "Tournament"). The tournament size is configured by tournamentSize. Selection pressure increases with tournament size. The worst k-1 genes of a population never survive.
- Deterministic tournament selection of 2 genes (configured by "Duel").
- Stochastic tournament selection of k genes (configured by "STournament"). The tournament size is configured by tournamentSize.
- Linear rank selection with selective pressure (configured by "LRSelective"). The selection bias which regulates the selection pressure is configured by selectionBias (should be between 1.0 (uniform selection) and 2.0).
- Linear rank selection with interpolated target sampling rates (configured by "LRTSR"). The maximal target sampling rate is configured by maxTSR (should be between 1 and 2).
- Stochastic universal sampling (configured by "SUS").
- The best (worst) k genes (configured by "TopK". k is configured by topK. Useful for convex functions and for gene migration.

If selectionContinuation=TRUE, then selection functions are computed exactly once per generation. They are transformed into lookup functions which deliver the index of selected genes by indexing a vector of integers.

See package xegaSelectGene <<https://CRAN.R-project.org/package=xegaSelectGene>>

Replication

For genetic algorithms ("sga", "sgp", "sgperm", and "sge") in the replication process of a gene the crossover operator may be configured to produce

1. **one** new gene (replication="Kid1", replication="Kid1Pipeline", or replication="Kid1PipelineG")
2. or **two** new genes (replication="Kid2", replication="Kid2Pipeline", or replication="Kid2PipelineG").

The first version loses genetic information in the crossover operation, whereas the second version retains the genetic material in the population. There is a dependency between replication and crossover: "Kid2", Kid2Pipeline, and Kid2PipelineG require a crossover operator which produces two kids. The replication method is configured by the function xegaGaReplicationFactory() of package xegaGaGene.

For differential evolution (algorithm "sgde") and grammatical evolution with differential evolution operators (algorithm "sgede"), one of

- replication="DE", pipeline="NoPipe" or
- replication="DEPipeline", pipeline="PipeC" or
- replication="DEPipelineG", pipeline="PipeG"

must be configured.

The replication method for differential evolution is configured by the function xegaDfReplicationFactory() of package xegaDfGene. It implements a configurable acceptance rule. For classic differential evolution, use accept="Best".

The pipeline pipeline compilation (configured by pipeline="PipeC" or pipeline="PipeG") builds either a population of function closures of genetic operator pipelines or a population of genes with embedded genetic operator pipelines. As a consequence, the complete genetic mechanism except the selection of genes can be parallelized.

Crossover

The table below summarizes the crossover operators available in the current version.

Algorithm:	"sga" and "sge"	Package:	xegaGaGene	
Kids	Name	Function	crossover=	Influenced by
(2 kids)	1-Point	xegaGaCross2Gene()	"Cross2Gene"	
	Uniform	xegaGaUCross2Gene()	"UCross2Gene"	
	Parametrized Uniform	xegaGaUPCross2Gene()	"UPCross2Gene"	ucrossSwap
(1 kid)	1-Point	xegaGaCrossGene()	"CrossGene"	
	Uniform	xegaGaUCrossGene()	"UCrossGene"	
	Parametrized Uniform	xegaGaUPCrossGene()	"UPCrossGene"	ucrossSwap
Algorithm:	"sgde" and "sgede"	Package:	xegaDfGene	
(1 kid)	1-Point	xegaDfCrossGene()	"CrossGene"	
	Uniform	xegaDfCrossGene()	"UCrossGene"	
	Parametrized Uniform	xegaDfUPCrossGene()	"UPCrossGene"	ucrossSwap
Algorithm:	"sgperm"	Package:	xegaPermGene	
(2 kids)	Position-Based	xegaPermCross2Gene()	"Cross2Gene"	
(1 kid)	Position-Based	xegaPermCrossGene()	"CrossGene"	
Algorithm:	"sgp"	Package:	xegaGpGene	
(2 kids)	of Derivation Trees	xegaGpAllCross2Gene()	"Cross2Gene" or "All2Cross2Gene"	maxcrossdepth, maxdepth, and maxtrials
	of Depth-Filtered Derivation Trees	xegaGpFilterCross2Gene()	"FilterCross2Gene"	maxcrossdepth, mincrossdepth, maxdepth, and maxtrials
(1 kid)	of Derivation Trees	xegaGpAllCrossGene()	"AllCrossGene"	maxcrossdepth, maxdepth, and maxtrials
	of Depth-Filtered Derivation Trees	xegaGpFilterCrossGene()	"FilterCrossGene"	maxcrossdepth, mincrossdepth, maxdepth, and maxtrials

Mutation

The table below summarizes the mutation operators in the current version.

Algorithm:	"sga" and "sge"	Package:	xegaGaGene
Name	Function	mutation=	Influenced by
Bit Mutation	xegaGaMutateGene()	"MutateGene"	bitmutrate
Individually	xegaGaIVAdaptiveMutateGene()	"IVM"	bitmutrate, bitmutrate2, and cutoffFit
Variable Bit Mutation			
Algorithm:	"sgde" and "sgede"	Package:	xegaDfGene
Differential	xegaDfMutateGeneDE()	"MutateGene" or	IF\$ScaleFactor()
Evolution Mutation		"MutateGeneDe"	(Configurable)

Algorithm:	"sgperm"	Package:	xegaPermGene
Generalized Order Based Mutation	xegaPermMutateGeneOrderBased()	"MutateGene"	bitmutrate
k Inversion Mutation	xegaPermMutateGenekInversion()	"MutateGeneOrderBased"	lambda
2-Opt Mutation	xegaPermMutateGene2Opt()	"MutateGene2Opt"	max2opt
k-Opt LK Mutation (Lin-Kernighan)	xegaPermMutateGenekOptLK()	"MutateGenekOptLK"	max2opt
Greedy Path Mutation	xegaPermMutateGeneGreedy()	"MutateGeneGreedy"	lambda
Best Greedy Path Mutation	xegaPermMutateGeneBestGreedy()	"MutateGeneBestGreedy"	lambda
Random Mutation Operator	xegaPermMutateMix()	"MutateGeneMix"	
Algorithm:	"sgp"	Package:	xegaGpGene
Derivation Tree Mutation	xegaGpMutateAllGene()	"MutateGene" or "MutateAllGene"	maxmutdepth
Filtered Derivation Tree Mutation	xegaGpMutateGeneFilter()	"MutateFilterGene"	maxmutdepth, minmutinsertiondepth, and maxmutinsertiondepth

Acceptance

Acceptance rules are extensions of genetic and evolutionary algorithms which - to the best of my knowledge - have their origin in simulated annealing. An acceptance rule compares the fitness value of a modified gene with the fitness value of its parent and determines which of the two genes is passed into the next population.

An acceptance rule is only executed as part of the genetic operator pipeline, if replicate="Kid1", replicate="Kid1Pipeline", replicate="Kid1PipelineG", replicate="Kid2Pipeline", replicate="DE", replicate="DEPipeline", or replicate="DEPipelineG".

Two classes of acceptance rules are provided:

- Simple acceptance rules.
 - Accept the new gene unconditionally (configured by accept="All"). The new gene is always passed to the next population. Choose the rule for configuring a classic genetic algorithm. (The default).
 - Accept only the best gene (configured by accept="Best"). This acceptance rule guarantees an increasing fitness curve over the run of the algorithm. For example, classic differential evolution uses this acceptance rule.
- Configurable acceptance rules. The rules always accept a new gene with a fitness improvement. They also accept a new gene with a lower fitness with a probability which depends on the fitness difference of the old and the new gene and a temperature parameter which is reduced over the algorithm run by a configurable cooling schedule.
 - The Metropolis acceptance rule (configured by accept="Metropolis"). The larger the parameter beta is set, the faster the drop in acceptance probability.

- The individually adaptive Metropolis acceptance rule (configured by `accept="IVMetropolis"`). The larger the parameter `beta` is set, the faster the drop in acceptance probability. Individually adaptive means that the temperature is corrected. The correction (increase) of temperature depends on the difference between the fitness of the currently known best solution and the fitness of the new gene.

The cooling schedule updates the temperature parameter at the end of the main loop. The following cooling schedules are available:

- Exponential multiplicative cooling (configured by `cooling="ExponentialMultiplicative"`). Depends on the discount factor `alpha` and the start temperature `temp0`.
- Logarithmic multiplicative cooling (configured by `cooling="LogarithmicMultiplicative"`). Depends on the scaling factor `alpha` and the start temperature `temp0`.
- Power multiplicative cooling (configured by `cooling="PowerMultiplicative"`). Depends on the scaling factor `alpha`, the cooling power exponent `coolingPower`, and the start temperature `temp0`.
- Power additive cooling (configured by `cooling="PowerAdditive"`). Depends on the number of generations `generations`, the cooling power exponent `coolingPower`, the start temperature `temp0`, and the final temperature `tempN`.
- Exponential additive cooling (configured by `cooling="ExponentialAdditive"`). Depends on the number of generations `generations`, the start temperature `temp0`, and the final temperature `tempN`.
- Trigonometric additive cooling (configured by `cooling="TrigonometricAdditive"`). Depends on the number of generations `generations`, the start temperature `temp0`, and the final temperature `tempN`.

See package `xegaPopulation` <<https://CRAN.R-project.org/package=xegaPopulation>>

Decoder

Decoders are algorithm and task-dependent. Their implementation often makes use of a gene map. The table below summarizes the available decoders and gene maps of the current version.

Algorithm:	"sga"	"sgde"	"sgperm"
In package:	<code>xegaGaGene</code>	<code>xegaDfGene</code>	<code>xegaPermGene</code>
Decoder:	<code>xegaGaDecodeGene()</code>	<code>xegaDfDecodeGene()</code>	<code>xegaPermDecodeGene()</code>
Gene map factories:	<code>xegaGaGeneMapFactory()</code>	<code>xegaDfGeneMapFactory()</code>	(Not configurable)
Method	"Bin2Dec"	"Identity"	
Method	"Gray2Dec"		
Method	"Identity"		
Method	"Permutation"		

Algorithm:	"sgp"	"sge"	"sgede"
In package:	<code>xegaGpGene</code>	<code>xegaGeGene</code>	<code>xegaGeGene</code>
Decoder Factories	(Not configurable)	<code>xegaGeDecodeGeneFactory()</code>	<code>xegaGeDecodeGeneFactory()</code>
Decoder:	<code>xegaGpDecodeGene()</code>		

Method:		"DecodeGene"	"DecodeGene"
Method:		"DecodeGeneDT"	"DecodeGeneDT"
Gene map factories:	(Not configurable)	xegaGeGeneMapFactory()	xegaDfGeneMapFactory()
Method		"Mod"	"Identity"
Method		"Buck"	

Evaluation

The method of evaluation of a gene is configured by `evalmethod`: "EvalGeneU" means that the function is always executed, "Deterministic" evaluates a gene only once, and "Stochastic" incrementally updates the mean and variance of a stochastic function. If `reportEvalErrors==TRUE`, evaluation failures are reported. However, for grammatical evolution without gene repair this should be set to `FALSE`. See package `xegaSelectGene` <<https://CRAN.R-project.org/package=xegaSelectGene>>

The Concept of Genetic Operator Pipelines

In the gene life cycle, a gene is

1. modified by the genetic machinery and then
2. evaluated (expressed as a phenotype and its fitness measured with regard to an environment).

When using `xegaRun()` with default parameters, the genetic operations are evaluated sequentially, whereas the fitness evaluation can be parallelized. For some algorithms, as e.g. differential evolution, fitness evaluation must be performed as part of the genetic machinery. Differential evolution uses an acceptance rule which compares the modified gene with its parent and returns the better one. However, this implies that for such algorithms the sequential part dominates the execution time and the benefits from parallelization remain marginal. Other examples are the integration of randomized numerical gradients as genetic operators or the integration of local search heuristics like the Kernighan-Lin heuristic for traveling-salesman problems.

Genetic operator pipelines are

1. either implemented as function closures which embed a sequence of basic genetic operations
2. or they (and all the genes they need) are embedded in a gene.

`xega` provides two versions of pipeline compilation:

1. Compile genetic operator pipelines to function closures. In `xegaRun()`, by setting the option `pipeline="PipeC"` together with `replication` to one of "Kid1Pipeline", "Kid2Pipeline", or "DEPipeline", the selected replication function performs a set of random experiments to select the proper genes and based on their results compiles a function closure which embeds the genetic operator pipeline. These function closures are then executed in the evaluation step. **Warning.** This version requires proper serialization of function closures together with all objects in the environment of the function closure. E.g. for the package `rmpi`, serialization of function closures is not implemented.
2. Compile genetic operator pipelines by embedding into a gene. In `xegaRun()`, the option `pipeline="PipeG"` must be used together with `replication` to one of "Kid1PipelineG", "Kid2PipelineG", or "DEPipelinG". In the replication phase, the randomly selected genetic operator pipeline together with all genes needed is embedded into a gene. In the evaluation phase, this embedded genetic operator pipeline is executed.

This mechanism shifts the actual computation of all genetic operations but the selection of genes to the evaluation step.

The effect of genetic operator pipelines are

1. moderate for sequential execution. The net effect depends on the relative cost of the compilation process to the evaluation process. By compiling minimal genetic operating pipelines, moderate savings are achieved.
2. potentially high for parallel and distributed execution. The net effect depends on the necessity to evaluate the fitness of one or more genes in the genetic machinery, the cost of the compilation process, the cost of communication and the cost of the evaluation process. The compilation process usually shifts more than 90 percent of the computational load to the evaluation phase of the genetic algorithm (which can be parallelized).

Distributed and Parallel Processing

In general, distributed and parallel processing requires a sequence of three steps:

1. Configure and start the distributed or parallel infrastructure.
2. Distribute processing and collect results. In an evolutionary or genetic algorithm, the architectural pattern used for the implementation of coarse-grained parallelism by parallel evaluation of the fitness of the genes of a population is the master/worker pattern. In principle, the `lapply()`-function for evaluating a population of genes is replaced by a parallel version.
3. Stop the distributed or parallel infrastructure.

For evolutionary and genetic algorithms, the second step is controlled by two parameters, namely `executionModel` and `uParApply`:

1. If `uParApply=NULL`, then `executionModel` provides four ways of evaluating the fitness of a population of genes:
 - (a) `executionModel="Sequential"`: The apply function used is `base::lapply()`. (Default).
 - (b) `executionModel="MultiCore"`: The apply function used is `parallel::mclapply()`. If the number of cores is not specified by `cores`, the number of available cores is determined by `parallelly::availableCores()`.
 - (c) `executionModel="MultiCoreHet"`: The apply function used is `parallel::mclapply()` with `mc.preschedule=FALSE`. If the number of cores is not specified by `cores`, the number of available cores is determined by `parallelly::availableCores()`. This improves speed for tasks with a high variance in execution time.
 - (d) `executionModel="FutureApply"`: The apply function used is `future.apply::future_lapply()`. The parallel/distributed model depends on a proper `future::plan()` statement.
 - (e) `executionModel="Cluster"`: The apply function used is `parallel::parLapply()`. The information about the configuration of the computing cluster (master, port, list of workers) must be provided by `Cluster=c1` where `c1<-parallel::makeClusterPSOCK(rep(localhost, 5))` generates the cluster object and starts the R processes (of 5 workers in the same machine).

2. Assume that a user-defined parallel apply function has been defined and called UPARAPPLY. By setting `uParApply=UPARAPPLY`, the `lapply()` function used is `UPARAPPLY()`. This overrides the specification by `executionModel`. For example, parallelization via the MPI interface can be achieved by providing a user-defined parallel `lapply()` function which is implemented by a user-defined function whose function body is the line `Rmpi::mpi.parLapply(pop, FUN=EvalGene, lF=lF)`.

See package `xegaPopulation` <<https://CRAN.R-project.org/package=xegaPopulation>>

Acknowledgment. The author acknowledges support by the state of Baden-Württemberg through bwHPC.

Reporting

- `verbose` controls the information reported on the screen. If `verbose` is 1, then one dot is printed per generation to the console.
- `reportEvalErrors=TRUE` reports the output of errors of fitness function evaluations to the console. Grammatical evolution (algorithm "sge") routinely attempts to evaluate incomplete derivation trees. This leads to an evaluation error of the fitness function.
- `profile=TRUE` measures the time spent in executing the main blocks of the algorithm: `InitPopulation()`, `NextPopulation()`, `EvalPopulation()`, `ObservePopulation()`, and `SummaryPopulation()`. The measurements are stored in the named list `$timer` of the result object.
- `allSolutions=TRUE` collects all solutions with the same fitness value. The lists of the genotypes and phenotypes of these solutions are stored in `$solution$allgenotypes` and `$allphenotypes` of the result object of the algorithm.
- `batch=TRUE` writes the result object and `logevals=TRUE` writes a list of all evaluated genes in an rds-file in the current directory. `path` allows to write the rds-files into another directory. The existence of the directory specified by `path` is not checked. `batch=TRUE` combined with `verbose=TRUE` should be used in batch environments on HPC environments.
- `anytime=TRUE` writes the result object `path/xegaAnyTimeResult.rds` after each generation. Only the most recent result is available.

Semantics of the local function list IF

This is experimental. The rationale is to save on communication cost in multi-core processing.

- `byValue` is the Default.
- `byReference` converts IF to an environment.

See Also

Other Main Program: [xegaReRun\(\)](#)

Examples

```
a<-xegaRun(penv=Parabola2D, generations=3, popsize=5, verbose=0, debug=TRUE)
b<-xegaRun(penv=Parabola2D, algorithm="sga",
generations=10, popsize=20, max=FALSE,
replication="Kid2Pipeline", crossover="Cross2Gene", pipeline="PipeC",
```

```

    verbose=1, replay=5, profile=TRUE, debug=FALSE)
b1<-xegaRun(penv=Parabola2D, algorithm="sga",
  generations=10, popsize=20, max=FALSE,
  replication="Kid1PipelineG", crossover="Cross2Gene", pipeline="PipeG",
  verbose=1, replay=5, profile=TRUE, debug=FALSE)
c<-xegaRun(penv=Parabola2D, max=FALSE, algorithm="sgde",
  popsize=20, generations=10,
  mutation="MutateGeneDE", scalefactor="Uniform", crossover="UCrossGene",
  genemap="Identity", replication="DE",
  selection="UniformP", mateselection="UniformP", accept="Best")
c1<-xegaRun(penv=Parabola2D, max=FALSE, algorithm="sgde",
  popsize=20, generations=10, elitist=TRUE,
  mutation="MutateGeneDE", scalefactor="Uniform", crossover="UCrossGene",
  genemap="Identity", replication="DEPipeline", pipeline="PipeC",
  selection="UniformP", mateselection="UniformP", accept="Best")
c2<-xegaRun(penv=Parabola2D, max=FALSE, algorithm="sgde",
  popsize=20, generations=10, elitist=TRUE,
  mutation="MutateGeneDE", scalefactor="Uniform", crossover="UCrossGene",
  genemap="Identity", replication="DEPipelineG", pipeline="PipeG",
  selection="UniformP", mateselection="UniformP", accept="Best", debug=FALSE)
envXOR<-NewEnvXOR()
BG<-compileBNF(booleanGrammar())
d<-xegaRun(penv=envXOR, grammar=BG, algorithm="sgp",
  generations=4, popsize=20, verbose=0)
e<-xegaRun(penv=envXOR, grammar=BG, algorithm="sgp",
  generations=4, popsize=20, verbose=0, initgene="InitGeneGe")
f<-xegaRun(penv=envXOR, grammar=BG, algorithm="sge", genemap="Mod",
  generations=4, popsize=20, reportEvalErrors=FALSE, verbose=1)
g<-xegaRun(penv=envXOR, grammar=BG, max=TRUE, algorithm="sgede",
  popsize=20, generations=4, verbose=1, reportEvalErrors=FALSE,
  mutation="MutateGeneDE", scalefactor="Uniform", crossover="UCrossGene",
  genemap="Identity", replication="DE",
  selection="UniformP", mateselection="UniformP", accept="Best")
g1<-xegaRun(penv=envXOR, grammar=BG, max=TRUE, algorithm="sgede",
  popsize=20, generations=4, verbose=1, reportEvalErrors=FALSE,
  mutation="MutateGeneDE", scalefactor="Uniform", crossover="UCrossGene",
  genemap="Identity", replication="DEPipelineG", pipeline="PipeG",
  selection="UniformP", mateselection="UniformP", accept="Best")
h<-xegaRun(penv=lau15, max=FALSE, algorithm="sgperm",
  popsize=20, generations=5, max2opt=20,
  genemap="Identity", mutation="MutateGeneMix")
i<-xegaRun(penv=lau15, max=FALSE, algorithm="sgperm",
  popsize=20, generations=5, max2opt=20,
  genemap="Identity", mutation="MutateGeneMix",
  executionModel="Sequential", replication="Kid1Pipeline", pipeline="PipeC")
j<-xegaRun(penv=lau15, max=FALSE, algorithm="sgperm",
  popsize=20, generations=5, max2opt=20,
  genemap="Identity", mutation="MutateGeneMix",
  executionModel="Sequential", replication="Kid1PipelineG", pipeline="PipeG", verbose=1)
cat("t(s) h:", h$timer$tMainLoop, "i:", i$timer$tMainLoop, "j:", j$timer$tMainLoop, "\n")

```

xegaVersion

About this version.

Description

About this version.

Usage

```
xegaVersion(verbose = TRUE)
```

Arguments

verbose Boolean. If TRUE (Default), print package information and version number to the console.

Value

Version number (invisible).

Examples

```
xegaVersion()
```

Index

* Configuration

- sgXCrossoverFactory, 8
- sgXDecodeGeneFactory, 9
- sgXGeneMapFactory, 10
- sgXInitGeneFactory, 11
- sgXMutationFactory, 11
- sgXReplicationFactory, 12

* File I/O

- createExclusiveFile, 4

* Grammar

- booleanGrammar, 2
- compileBNF, 3

* Main Program

- xegaReRun, 18
- xegaRun, 19

* Package Description

- xega, 13

* Problem Environment

- lau15, 5
- NewEnvXOR, 5
- Parabola2D, 6
- Parabola2DEarly, 7

* datasets

- lau15, 5
- Parabola2D, 6
- Parabola2DEarly, 7

booleanGrammar, 2, 3

compileBNF, 3, 3

createExclusiveFile, 4

lau15, 5, 6–8

NewEnvXOR, 5, 5, 7, 8

Parabola2D, 5, 6, 6, 8

Parabola2DEarly, 5–7, 7, 29, 30

sgXCrossoverFactory, 8, 9–13

sgXDecodeGeneFactory, 9, 9, 10–13

sgXGeneMapFactory, 9, 10, 11–13

sgXInitGeneFactory, 9, 10, 11, 12, 13

sgXMutationFactory, 9–11, 11, 13

sgXReplicationFactory, 9–12, 12

xega, 13

xega-package (xega), 13

xegaAnyTimeResult, 16

xegaDebug, 17

xegaReRun, 18, 43

xegaRun, 19, 19

xegaVersion, 45