

Package ‘modelbpp’

March 1, 2026

Title Model BIC Posterior Probability

Version 0.2.0

Description Fits the neighboring models of a fitted structural equation model and assesses the model uncertainty of the fitted model based on BIC posterior probabilities (BPP), using the method presented in Wu, Cheung, and Leung (2020) [<doi:10.1080/00273171.2019.1574546>](https://doi.org/10.1080/00273171.2019.1574546). See Pesigan, Cheung, Wu, Chang, and Leung (2026) [<doi:10.3758/s13428-025-02921-x>](https://doi.org/10.3758/s13428-025-02921-x) for an introduction to the package.

License GPL (>= 3)

Encoding UTF-8

RoxygenNote 7.3.3

Suggests knitr, rmarkdown, tinytest

Depends R (>= 4.0.0)

Imports lavaan, parallel, pbapply, igraph, manymome

VignetteBuilder knitr

URL <https://sfcheung.github.io/modelbpp/>

BugReports <https://github.com/sfcheung/modelbpp/issues>

LazyData true

NeedsCompilation no

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Repository CRAN

Date/Publication 2026-03-01 13:30:02 UTC

Contents

c.partables	2
dat_cfa	4
dat_path_model	5
dat_path_model_p06	6
dat_sem	6
dat_serial_4	7
dat_serial_4_weak	8
fit_many	8
get_add	10
get_drop	12
measurement_invariance_models	14
min_prior	16
model_graph	18
model_set	21
model_set_combined	26
partables_helpers	28
plot.model_graph	30
print.model_set	31
print.partables	33
print.sem_outs	34
Index	36

c.partables	<i>Manipulate Parameter Tables</i>
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Description

Functions to manipulate a partables-class object

Usage

```
## S3 method for class 'partables'
c(...)

## S3 method for class 'model_set'
c(...)

partables_drop(x, model_names = NULL)
```

Arguments

...	An arbitrary number of objects. All invalid objects (see details) will be discarded. If an object is named and is not partables object, its name will be used.
x	A partables-class object.
model_names	A character vector of the names of models in a partables-class object.

Details

The partables-class objects have a `c()` method that can be used to combine parameter tables. Each object must be

a. a partables-class object, b. a `model_set`-class object, c. a lavaan-class object, or d. a parameter table of the class `lavaan.data.frame()`, usually generated by `lavaan::parameterTable()`. Other objects will be discarded.

Names will be used when combining objects. If two objects have the same names, then only the first one will be retained. No warning message will be issued. Users are encouraged to explicitly name all objects carefully.

Note that, to invoke this method, the first object must be a partables object.

The `model_set` class also has a `c`-method. It will replace the first object by the stored partables and then call the `c`-method of partables objects.

The function `partables_drop()` is for dropping models from a partables-class object.

Value

A partables-class objects with all the objects supplied combined together. If an object is a lavaan-class object, its parameter table will be retrieved by `lavaan::parameterTable()`. If an object is a `model_set`-class object, the stored partables-class object will be retrieved.

Author(s)

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Examples

```
library(lavaan)

moda <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1
ab := a*b
"

fita <- sem(moda, dat_path_model, fixed.x = TRUE)

outa <- model_set(fita,
  progress = FALSE,
  parallel = FALSE)

modb <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x2
ab := a*b
"

fitb <- sem(modb, dat_path_model, fixed.x = TRUE)
```

```
outb <- model_set(fitb,
                  progress = FALSE,
                  parallel = FALSE)

mod2 <-
"
x2 ~ 0*x3 + 0*x4
x1 ~ 0*x3
"
fit2 <- sem(mod2, dat_path_model)

mod3 <-
"
x2 ~ x3 + 0*x4
x1 ~ x3
"
fit3 <- sem(mod3, dat_path_model)

out <- c(outa$models, user2 = fit2, outb$models, user3 = fit3)
out

out2 <- c(outa, user2 = fit2, outb$models, user3 = fit3)
out2

out3 <- c(outa, user2 = fit2, outb, user3 = fit3)
out3
```

dat_cfa

*A Sample Dataset Based On a Confirmatory Factor Analysis Model
(For Testing)*

Description

Generated from a confirmatory factor analysis model (n = 200).

Usage

dat_cfa

Format

A data frame with six variables:

x1 Indicator

x2 Indicator

x3 Indicator

x4 Indicator

x5 Indicator

x6 Indicator

Details

The model used to generate this dataset:

$$f1 \sim x1 + x2 + x3 + x5$$

$$f2 \sim x3 + x4 + x5 + x6$$

$$f1 \sim f2$$

dat_path_model	<i>A Sample Dataset Based on a Path Model (For Testing)</i>
----------------	---

Description

Generated from the a path model (n = 100).

Usage

dat_path_model

Format

A data frame with four variables:

x1 Predictor

x2 Predictor

x3 Mediator

x4 Outcome

Details

The model used to generate this dataset:

$$x1 \sim x2$$

$$x3 \sim x1 + x2$$

$$x4 \sim x3 + x1 + x2$$

dat_path_model_p06 *A Sample Dataset Based On a Complex Path Model (For Testing)*

Description

Generated from a complex path model (n = 200).

Usage

dat_path_model_p06

Format

A data frame with six variables:

x1 Predictor

x2 Predictor

x3 Predictor

y4 Mediator

y5 Mediator

y6 Outcome

Details

The model used to generate this dataset:

$y4 \sim x1 + x2 + x3$

$y5 \sim y4 + x1 + x2$

$y6 \sim y4 + y5 + x1 + x2 + x3$

$x1 \sim x2 + x3$

$x2 \sim x3$

dat_sem *A Sample Dataset Based On a Structural Model (For Testing)*

Description

Generated from a structural model with latent variables (n = 250).

Usage

dat_sem

Format

An object of class `data.frame` with 250 rows and 16 columns.

Details

The model to be fitted:

```
f1 =~ x1 + x2 + x3 + x4
f2 =~ x5 + x6 + x7 + x8
f3 =~ x9 + x10 + x11 + x12
f4 =~ x13 + x14 + x15 + x16
f3 ~ f1 + f2
f4 ~ f3
```

dat_serial_4

A Sample Dataset Based On a Serial Mediation Model (For Testing)

Description

Generated from a serial mediation model ($n = 100$).

Usage

```
dat_serial_4
```

Format

A data frame with four variables:

x Predictor
m1 Mediator
m2 Mediator
y Outcome

Details

The model used to generate this dataset:

```
m1 ~ x
m2 ~ m1
y ~ m2
```

dat_serial_4_weak	<i>A Sample Dataset Based On a Serial Mediation Model With Weak Paths (For Testing)</i>
-------------------	---

Description

Generated from a serial mediation model (n = 100).

Usage

```
dat_serial_4_weak
```

Format

A data frame with four variables:

x Predictor

m1 Mediator

m2 Mediator

y Outcome

Details

The model to be fitted:

$$m1 \sim x$$
$$m2 \sim m1 + x$$
$$y \sim m2 + m1 + x$$

fit_many	<i>Fit a List of Models</i>
----------	-----------------------------

Description

Fit a list of models to a dataset.

Usage

```
fit_many(  
  model_list,  
  sem_out,  
  original = NULL,  
  parallel = FALSE,  
  ncores = max(parallel::detectCores(logical = FALSE) - 1, 1),  
  make_cluster_args = list(),  
  progress = TRUE,  
  verbose = TRUE  
)
```

Arguments

model_list	A list of parameter tables to be used by <code>lavaan::lavaan()</code> or <code>update()</code> . Usually generated by <code>get_add()</code> or <code>get_drop()</code> .
sem_out	The output from an structural equation modeling function. It currently supports <code>lavaan::lavaan</code> objects only. Usually the one used in <code>model_set()</code> , <code>get_add()</code> or <code>get_drop()</code> to generate the list of models.
original	String. If provided, it should be a name of a model in <code>model_list</code> , with which differences in model degrees of freedom will be computed for other models. If NULL, the default, then the model in <code>sem_out</code> will be used to computed the differences in model degrees of freedom. If NA, then differences in model <i>df</i> will not be computed.
parallel	If TRUE, parallel processing will be used to fit the models. Default is FALSE.
ncores	Numeric. The number of CPU cores to be used if <code>parallel</code> is TRUE.
make_cluster_args	A list of named arguments to be passed to <code>parallel::makeCluster()</code> . Used by advanced users to configure the cluster if <code>parallel</code> is TRUE. Default is <code>list()</code> .
progress	Whether a progress bar will be displayed, implemented by the <code>pbapply</code> package. Default is TRUE.
verbose	Whether additional messages will be displayed, such as the expected processing time. Default is TRUE.

Details

It receives a list of models, defined by lavaan parameter tables (usually generated by `model_set()`, `get_add()` or `get_drop()`), and fit them to a dataset stored in a lavaan-class object.

This function is called by `model_set()` and usually users do not need to call it. It is exported for advanced users.

Value

An object of the class `sem_outs`, a list with the following major elements:

- `fit`: A named list of `lavaan::lavaan()` output objects or `update()` for fitting a model with the added parameters.
- `change`: A numeric vector, of the same length as `fit`. The change in model *df* for each fit compared to the original model. A positive number denotes one less free parameter. A negative number denotes one more free parameter or one less constraint.
- `converged`: A named vector of boolean values, of the same length as `fit`. Indicates whether each fit converged or not.
- `post_check`: A named vector of boolean values, of the same length as `fit`. Indicates whether the solution of each fit is admissible or not. Checked by `lavaan::lavInspect()` with the what argument set to "post.check".

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448>

Examples

```

library(lavaan)
dat <- dat_path_model
mod <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1
ab := a*b
"
fit <- sem(mod, dat_path_model, fixed.x = TRUE)
mod_to_add <- get_add(fit)
fit_many(mod_to_add, fit)

```

get_add

Models That Are Less Restricted

Description

Generate a list of models with one or more fixed parameter freed.

Usage

```

get_add(
  sem_out,
  must_add = NULL,
  must_not_add = NULL,
  remove_constraints = TRUE,
  exclude_error_cov = TRUE,
  exclude_feedback = FALSE,
  exclude_xy_cov = FALSE,
  cross_add = c("pure_x", "pure_y"),
  cross_sets = NULL,
  df_change = 1,
  model_id = NA,
  keep_correct_df_change = TRUE,
  remove_duplicated = TRUE,
  progress = FALSE
)

```

Arguments

sem_out	The original model, which is the output from an structural equation modeling function. Currently support <code>lavaan::lavaan</code> objects only.
must_add	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "y ~ x"), that must be added. Default is NULL.

must_not_add	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "x1 ~~ x1"), that must not be added. Default is NULL.
remove_constraints	Whether equality constraints will be removed. Default is TRUE.
exclude_error_cov	Exclude error covariances of indicators. Default is TRUE.
exclude_feedback	Exclude paths that will result in a feedback loop. For example, if there is path from x through m to y, then the path $x \sim y$ will create a feedback loop. Default is FALSE for now, to maintain backward compatibility. Do not rely on the default value because it will be changed to TRUE in a future major version.
exclude_xy_cov	Exclude covariance between two variables, in which one has a path to another. For example, if there is path from x through m to y, then the covariance $x \sim y$, which denotes the covariance between x and the error term of y, will be excluded if this argument is TRUE. Default is FALSE for now, to maintain backward compatibility. Do not rely on the default value because it will be changed to TRUE in a future major version.
cross_add	A character vector of whether and how cross-loadings (an indicator loads on two or more latent factors) will be added. If NULL, no cross-loadings will be added. If "lav_x" is in the vector, then cross-loadings among "pure-x" latent factors, latent factors that do not regress on any other variables, will be considered. If "lav_y" is in the vector, then cross-loadings among "pure-y" latent factors, latent factors that regress on at least one variables but they themselves do not predict any other variables, will be considered. If "user" is in the vector, then cross-loadings among latent factors listed in <code>cross_sets</code> will be considered.
cross_sets	A character vector of latent variables for which cross-loadings will be considered. Ignored if "user" is not in <code>cross_add</code> . Note that cross-loadings involving latent variables which are mediators will not be considered. To add them, they must be specified explicitly in <code>must_add</code> .
df_change	How many degrees of freedom (<i>df</i>) away in the list. All models with <i>df</i> change less than or equal to this number will be included, taking into account requirements set by other arguments. Default is 1.
model_id	The identification number of the starting model. Default is NA, no identification number.
keep_correct_df_change	Keep only models with actual <i>df</i> change equal to expected <i>df</i> change.
remove_duplicated	If TRUE, the default, duplicated models are removed.
progress	Whether a progress bar will be displayed, implemented by the <code>pbapply</code> package. Default is FALSE.

Details

It generates a list of models with one or more fixed parameter freed (and the degrees of freedom, *df*, increases by one or more). If a model has equality constraints, models with one or more of the constraints between two free parameters released will also be included.

Graphically, paths or covariances are "added" to form the list of models.

The models to be included are identified by `lavaan::modificationIndices()`.

The models will be checked by lavaan to make sure that the decrease in model degrees of freedom is of the expected value.

This function is called by `model_set()` and usually users do not need to call it. It is exported for advanced users.

Value

An object of the class `partables`, a named list of parameter tables, each of them to be used by `lavaan::lavaan()` or `update()` for fitting a model with the added parameters.

Author(s)

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See Also

`print.partables()`

Examples

```
library(lavaan)
dat <- dat_path_model
mod <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1
ab := a*b
"
fit <- sem(mod, dat_path_model, fixed.x = TRUE)
mod_to_add <- get_add(fit)
mod_to_add
```

get_drop

Models That Are More Restricted

Description

Generate a list of models with one or more free parameter dropped (fixed to zero).

Usage

```

get_drop(
  sem_out,
  must_drop = NULL,
  must_not_drop = NULL,
  loadings_to_exclude = c("single", "none", "all"),
  df_change = 1,
  model_id = NA,
  keep_correct_df_change = TRUE,
  remove_duplicated = TRUE,
  progress = FALSE
)

```

Arguments

sem_out	The original model, which is the output from an structural equation modeling function. Currently support <code>lavaan::lavaan</code> objects only.
must_drop	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "y ~ x"), that must be included. Default is NULL.
must_not_drop	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "x1 ~~ x1"), that must not be included. Default is NULL.
loadings_to_exclude	Whether factor loadings will be excluded. If "single", then only "single" loadings (an indicator loads on only one latent factor) will be excluded. If "all", then all factor loadings will be excluded. If "none", then no loadings will be excluded. Be careful when using "none" because the models may not make sense. The settings in <code>must_drop</code> and <code>must_not_drop</code> will override this argument.
df_change	How many degrees of freedom away in the list. All models with <i>df</i> change less than or equal to this number will be included, taking into account requirements set by other arguments. Default is 1.
model_id	The identification number of the starting model. Default is NA, no identification number.
keep_correct_df_change	Keep only models with actual <i>df</i> change equal to expected <i>df</i> change.
remove_duplicated	If TRUE, the default, duplicated models are removed.
progress	Whether a progress bar will be displayed, implemented by the <code>pbapply</code> package. Default is FALSE.

Details

It generates a list of models with one or more free parameters dropped, that is, fixed to zero (with degrees of freedom, *df*, increases by one or more).

All free parameters are included in the pool of candidates, except for those explicitly requested to be kept.

The models will be checked by lavaan to make sure that the increase in model degrees of freedom is of the expected value.

This function is called by `model_set()` and usually users do not need to call it. It is exported for advanced users.

Value

An object of the class `partables`, a named list of parameter tables, each of them to be used by `lavaan::lavaan()` or `update()` for fitting a model with the added parameters.

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448>

See Also

`print.partables()`

Examples

```
library(lavaan)

dat <- dat_path_model
mod <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1 + x2
ab := a*b
"

fit <- sem(mod, dat_path_model, fixed.x = TRUE)
mod_to_drop <- get_drop(fit)
mod_to_drop
```

measurement_invariance_models

Measurement Invariance Models

Description

Generate metric and scalar invariance models and their partial invariance versions.

Usage

```
measurement_invariance_models(
  cfa_out,
  max_free = 1,
  metric = TRUE,
  scalar = TRUE,
  progress = TRUE
)
```

Arguments

<code>cfa_out</code>	The output of <code>lavaan::cfa()</code> .
<code>max_free</code>	The maximum number of constraints to be released when generating the partial invariance models. For example, if set to 1, then only the partial metric invariance model only has at most one item allowed to have different loadings across group. Default is 1. If set to zero, then no partial invariance models will be generated.
<code>metric</code>	Logical. If TRUE, the default, then metric invariance model and its partial invariance versions are generated.
<code>scalar</code>	Logical. If TRUE, the default, then scalar invariance model and its partial invariance versions are generated.
<code>progress</code>	Logical. If TRUE, the default, progress bars will be displayed when fitting partial invariance models.

Details

This a helper function to generate, based on a multigroup confirmatory factor analysis (CFA) model with no between-group equality constraints, the following models:

- A metric invariance model (loadings constrained to be equal across groups).
- A scalar invariance model (intercepts and loadings constrained to be equal across groups).
- Partial invariance versions of the previous two models, such as a model with the loadings of all items, except for one, constrained to be equal across groups.

The models generated can then be used in `model_set()` to compute BPPs.

Requirements:

The model used as the input needs to be fitted with no between group constrains, that is, it is a configural invariance model. Although not a must, it is advised to use the default way to identify each factor (that is, fixing a loading to one).

Implementation:

This function simply use the `group.partial` and `group.equal` argument of `lavaan::cfa()` to generate the models.

Value

A list of `lavaan::cfa()` output. The names are automatically generated to indicate whether a model is configural, metric, or scalar invariance, or the item(s) without between-group constraints on the loadings (for partial metric invariance) or intercepts (for partial scalar invariance).

Author(s)

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See Also

`model_set()`

Examples

```
library(lavaan)
# For illustration, only one factor is used,
# with one item from another factor added
# just to make the model not saturated.
HSmod <-
"
spatial =~ x1 + x2 + x3 + x4
"
fit_config <- cfa(model = HSmod,
                 data = HolzingerSwineford1939,
                 group = "school")
fit_mi <- measurement_invariance_models(fit_config)
names(fit_mi)
# Need to add 'skip_check_sem_out = TRUE' to use multigroup models.
out <- model_set(sem_out = fit_mi,
                 skip_check_sem_out = TRUE,
                 progress = FALSE,
                 parallel = FALSE)

print(out)
```

min_prior

Minimum Prior

Description

Find the minimum prior probability required to achieve the desired BIC posterior probability.

Usage

```
min_prior(bic, bpp_target, target_name = "original")
```

Arguments

bic	A named vector of BIC values for a set of models.
bpp_target	A value from zero to 1. The desired BIC posterior probability.
target_name	The name of the original model, as appeared in the names of bic.

Details

It assumes that all models other than the original model have the same prior probabilities.

This function is called by `model_set()` or `print.model_set()` and usually users do not need to call it. It is exported for advanced users.

Value

A scalar. The required prior probability.

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448>

References

Wu, H., Cheung, S. F., & Leung, S. O. (2020). Simple use of BIC to assess model selection uncertainty: An illustration using mediation and moderation models. *Multivariate Behavioral Research*, 55(1), 1–16. doi:10.1080/00273171.2019.1574546

See Also

[model_set\(\)](#) and [print.model_set\(\)](#)

Examples

```
library(lavaan)

dat <- dat_path_model

mod <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1
ab := a*b
"

fit <- sem(mod, dat_path_model, fixed.x = TRUE)

out <- model_set(fit)
min_prior(out$bic, bpp_target = .8)
```

 model_graph

Generate a Graph of Models

Description

Generate an 'igraph' object from a 'model_set' object.

Usage

```
model_graph(
  object,
  node_size_by_x = TRUE,
  x = NULL,
  node_size = 5,
  min_size = 5,
  max_size = 35,
  color_original = "lightblue",
  color_add = "burlywood1",
  color_drop = "lightgreen",
  color_others = "lightgrey",
  color_label = "black",
  node_label_size = 1,
  original = "original",
  drop_redundant_direct_paths = TRUE,
  label_arrow_by_df = NULL,
  arrow_label_size = 1,
  weight_arrows_by_df = c("inverse", "normal", "none"),
  arrow_min_width = 0.5,
  arrow_max_width = 2,
  progress = TRUE,
  short_names = FALSE,
  min_bpp_labelled = NULL,
  ...
)
```

Arguments

object	Must be a model_set-class object for now.
node_size_by_x	Logical. Whether node (vertex) sizes are determined by a variable. Default is TRUE. See x below on how size is determined.
x	If not NULL, it should be a numeric vector of length equal to the number of models. The node sizes will be proportional to the values of x, offset by min_size. If NULL, the default, the BIC posterior probabilities stored in object will be retrieved.
node_size	If node_size_by_x is FALSE, this is the size for all nodes.
min_size	The minimum size of a node. Default is 5.

max_size	The maximum size of a node. Default is 35.
color_original	The color of node of the original model. Default is "lightblue".
color_add	The color of the nodes of models formed by adding one or more free parameters to the original model. Default is "burlywood1".
color_drop	The color of the nodes of models formed by dropping one or more free parameters from the original model. Default is "lightgreen".
color_others	The color of other models not specified above. Default is "grey50".
color_label	The color of the text labels of the nodes. Default is "black".
node_label_size	The size of the labels of the nodes. Default is 1.
original	String. The name of the original model (target model). Default is "original".
drop_redundant_direct_paths	Logical. Whether the redundant direct path between two models. A direct path is redundant if two models are also connected through at least one another model. Default is TRUE.
label_arrow_by_df	If TRUE, then an arrow (edge) is always labelled by the difference in model <i>dfs</i> . If FALSE, then no arrows are labelled. If NULL, then arrows are labelled when not all differences in model <i>dfs</i> are equal to one. Default is NULL.
arrow_label_size	The size of the labels of the arrows (edges), if labelled. Default is 1.
weight_arrows_by_df	String. Use if model <i>df</i> differences are stored. If "inverse", larger the difference in model <i>df</i> , <i>narrower</i> an arrow. That is, more similar two models are, thicker the arrow. If "normal", larger the difference in model <i>df</i> , <i>wider</i> an arrow. If "none", then arrow width is constant, set to arrow_max_width. Default is "inverse".
arrow_min_width	If weight_arrows_by_df is not "none", this is the minimum width of an arrow.
arrow_max_width	If weight_arrows_by_df is not "none", this is the maximum width of an arrow. If weight_arrows_by_df is "none", this is the width of all arrows.
progress	Whether a progress bar will be displayed for some steps (e.g., checking for nested relations). Default is TRUE.
short_names	If TRUE and short model names are stored, they will be used as model labels. Please print the object with short_names = TRUE to find the corresponding full model names.
min_bpp_labelled	If not NULL, this is the minimum BPP for a model to be labelled. Models with BPP less than this value will not be labelled. Useful when the number of models is large.
...	Optional arguments. Not used for now.

Details

It extracts the model list stored in object, creates an adjacency matrix, and then creates an igraph object customized for visualizing model relations.

Construction of the Graph:

This is the default way to construct the graph when the model set is automatically by `model_set()`.

- Each model is connected by an arrow, pointing from one model to another model that
 - a. can be formed by adding one or more free parameter, or
 - b. can be formed by releasing one or more equality constraint between two parameters.
 - c. has nested relation with this model as determined by the method proposed by Bentler and Satorra (2010), if the models are not generated internally.

That is, it points to a model with more degrees of freedom (more complicated), and is nested within that model in either parameter sense or covariance sense.

- By default, the size of the node for each model is scaled by its BIC posterior probability, if available. See *The Size of a Node* below.
- If a model is designated as the original (target) model, than he original model, the models with more degrees of freedom than the original model, and the models with fewer degrees of freedom than the original models, are colored differently.
- The default layout is the Sugiyama layout, with simpler models (models with fewer degrees of freedom) on the top. The lower a model is in the network, the more the degrees of freedom it has. This layout is suitable for showing the nested relations of the models. Models on the same level (layer) horizontally have the same model *df*.

The output is an igraph object. Users can customize it in any way they want using functions from the igraph package.

If a model has no nested relation with all other model, it will not be connected to other models.

If no model is named original (default is "original"), then no model is colored as the original model.

User-Provided Models:

If object contained one or more user-provided models which are not generated automatically by `model_set()` or similar functions (e.g., `gen_models()`), then the method by Bentler and Satorra (2010) will be used to determine model relations. Models connected by an arrow has a nested relation based on the NET method by Bentler and Satorra (2010). An internal function inspired by the `net` function from the `semTools` package is used to implement the NET method.

The Size of a Node:

When a model is scaled by x , which usually is the BIC posterior probability, its size is determined by:

$$\text{max_size} * (x - \min(x)) / (\text{max}(x) - \min(x)) + \text{min_size}$$

Value

A `model_graph`-class object that can be used as as an igraph-object, with a plot method (`plot.model_graph()`) with settings suitable for plotting a network of models with BIC posterior probabilities computed.

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448> The internal function for nesting inspired by the net function from the semTools package, which was developed by Terrence D. Jorgensen.

References

Bentler, P. M., & Satorra, A. (2010). Testing model nesting and equivalence. *Psychological Methods*, 15(2), 111–123. doi:10.1037/a0019625

Asparouhov, T., & Muthén, B. (2019). Nesting and Equivalence Testing for Structural Equation Models. *Structural Equation Modeling: A Multidisciplinary Journal*, 26(2), 302–309. doi:10.1080/10705511.2018.1513795

Examples

```
library(lavaan)

mod <-
"
m1 ~ x
y ~ m1
"

fit <- sem(mod, dat_serial_4, fixed.x = TRUE)

out <- model_set(fit)
out

g <- model_graph(out)
plot(g)
```

model_set

BIC Posterior Probabilities of Neighboring Models

Description

Identify neighboring models, fit them, and return the BIC posterior probabilities.

Usage

```
model_set(
  sem_out,
  partables = NULL,
  model_set_out = NULL,
  prior_sem_out = NULL,
  must_add = NULL,
  must_not_add = NULL,
  must_drop = NULL,
```

```

must_not_drop = NULL,
loadings_to_exclude_from_drop = c("single", "none", "all"),
remove_constraints = TRUE,
exclude_error_cov = TRUE,
exclude_feedback = TRUE,
exclude_xy_cov = TRUE,
cross_add = c("pure_x", "pure_y"),
cross_sets = NULL,
df_change_add = 1,
df_change_drop = 1,
remove_duplicated = TRUE,
fit_models = ifelse(!is.null(model_set_out$fit), FALSE, TRUE),
compute_bpp = TRUE,
original = "original",
parallel = FALSE,
ncores = max(parallel::detectCores(logical = FALSE) - 1, 1),
make_cluster_args = list(),
progress = TRUE,
verbose = TRUE,
skip_check_sem_out = FALSE,
drop_equivalent_models = TRUE
)

gen_models(
  sem_out,
  must_add = NULL,
  must_not_add = NULL,
  must_drop = NULL,
  must_not_drop = NULL,
  loadings_to_exclude_from_drop = c("single", "none", "all"),
  remove_constraints = TRUE,
  exclude_error_cov = TRUE,
  exclude_feedback = TRUE,
  exclude_xy_cov = TRUE,
  cross_add = c("pure_x", "pure_y"),
  cross_sets = NULL,
  df_change_add = 1,
  df_change_drop = 1,
  remove_duplicated = TRUE,
  progress = TRUE,
  output = c("partables", "model_set")
)

```

Arguments

`sem_out` It can be the output from an SEM function. Currently it supports `lavaan::lavaan` objects only. If it is a named list of `lavaan::lavaan` objects, then all arguments for model generation will be ignored, and models will not be refitted. Users need to ensure that the models can be meaningfully compared because they will not be

	checked.
partables	A partables-class object, usually generated by <code>get_add()</code> or <code>get_drop()</code> . A named list of parameter tables to be fitted along with the original model in <code>sem_out</code> . If supplied, all arguments related to identifying models will be ignored. Default is NULL.
model_set_out	If set to the output of a previous call to <code>model_set()</code> (a <code>model_set</code> -class object), the list of stored models will be used. All arguments related to generate neighboring models will be ignored. If supplied, <code>sem_out</code> will also be ignored and will be retrieved from <code>model_set_out</code> , and <code>partables</code> will also be ignored. Default is NULL.
prior_sem_out	The prior of the model fitted in <code>sem_out</code> . Default is NULL, and all models will have equal prior probabilities.
must_add	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "y ~ x"), that must be added. Default is NULL.
must_not_add	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "x1 ~~ x1"), that must not be added. Default is NULL.
must_drop	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "y ~ x"), that must be included. Default is NULL.
must_not_drop	A character vector of parameters, named in <code>lavaan::lavaan()</code> style (e.g., "x1 ~~ x1"), that must not be included. Default is NULL.
loadings_to_exclude_from_drop	Whether factor loadings will be excluded when deciding parameters to drop. If "single", then only "single" loadings (an indicator loads on only one latent factor) will be excluded (they will not be dropped). If "all", then all factor loadings will be excluded (no factor loadings will be dropped). If "none", then no loadings will be excluded, and all free loadings will be considered to be dropped. Be careful when using "none" because the models may not make sense. The settings in <code>must_drop</code> and <code>must_not_drop</code> will override this argument.
remove_constraints	Whether equality constraints will be removed. Default is TRUE.
exclude_error_cov	Exclude error covariances of indicators. Default is TRUE.
exclude_feedback	Exclude paths that will result in a feedback loop. For example, if there is path from x through m to y, then the path $x \sim y$ will create a feedback loop. Default has been changed to TRUE since Version 0.1.3.5 because feedback loops are usually not included except when theoretically justified. To reproduce results based on previous version, set this argument to FALSE.
exclude_xy_cov	Exclude covariance between two variables, in which one has a path to another. For example, if there is path from x through m to y, then the covariance $x \sim y$, which denotes the covariance between x and the error term of y, will be excluded if this argument is TRUE. Default has been changed to TRUE since Version 0.1.3.5 because these covariances rarely are interpretable. To reproduce results based on previous version, set this argument to FALSE.

cross_add	A character vector of whether and how cross-loadings (an indicator loads on two or more latent factors) will be added. If NULL, no cross-loadings will be added. If "lav_x" is in the vector, then cross-loadings among "pure-x" latent factors, latent factors that do not regress on any other variables, will be considered. If "lav_y" is in the vector, then cross-loadings among "pure-y" latent factors, latent factors that regress on at least one variables but they themselves do not predict any other variables, will be considered. If "user" is in the vector, then cross-loadings among latent factors listed in cross_sets will be considered.
cross_sets	A character vector of latent variables for which cross-loadings will be considered. Ignored if "user" is not in cross_add. Note that cross-loadings involving latent variables which are mediators will not be considered. To add them, they must be specified explicitly in must_add.
df_change_add	How many degrees of freedom (<i>df</i>) away in the list. All models with <i>df</i> change less than or equal to this number will be included, taking into account requirements set by other arguments. Default is 1.
df_change_drop	How many degrees of freedom away in the list. All models with <i>df</i> change less than or equal to this number will be included, taking into account requirements set by other arguments. Default is 1.
remove_duplicated	If TRUE, the default, duplicated models are removed.
fit_models	If TRUE, the models will be fitted to the data, usually stored in sem_out. If FALSE, the models will be returned as is, in the element models of the output. If model_set_out is set and models have been fitted, then default is FALSE. Otherwise, default is TRUE.
compute_bpp	If TRUE, then BIC posterior probabilities will be computed. Default is TRUE.
original	String. The name of the original (target) model. Default is "original". Used if prior_sem_out is unnamed and only has one value.
parallel	If TRUE, parallel processing will be used to fit the models. Default is FALSE.
ncores	Numeric. The number of CPU cores to be used if parallel is TRUE.
make_cluster_args	A list of named arguments to be passed to parallel::makeCluster(). Used by advanced users to configure the cluster if parallel is TRUE. Default is list().
progress	Whether a progress bar will be displayed, implemented by the pbapply package or by utils::txtProgressBar. Default is TRUE.
verbose	Whether additional messages will be displayed, such as the expected processing time. Default is TRUE.
skip_check_sem_out	If TRUE and sem_out is set, check whether sem_out is of a supported type (estimator is "ML" and the model has only one group). If not, an error will be raised. Can be set to FALSE for experimenting the functions on models not officially supported.
drop_equivalent_models	If TRUE, the default, equivalent models will be dropped in the final output. This check can only be conducted when no models are fitted in lavaan::lavaan() with fixed.x = TRUE (which is the default of lavaan::sem()).

output If "model_set", then the output is a model_set-class object. If "partables", the output is a partables-class object. Default is partables.

Details

It computes the BIC posterior probabilities of a set of models by the method presented in Wu, Cheung, and Leung (2020).

First, a list of model is identified based on user-specified criteria. By default, models differ from a fitted model by one degree of freedom, the 1-df-away *neighboring* models, will be found using `get_add()` and `get_drop`.

Second, these models will be fitted to the sample dataset, and their BICs will be computed.

Third, their BIC posterior probabilities will be computed using their BICs. By default, equal prior probabilities for all the models being fitted will be assumed in the current version. This can be changed by `prior_sem_out`.

The results can then be printed, with the models sorted by descending order of BIC posterior probabilities. The results can also be visualized using `model_graph()`.

Value

The function `model_set()` returns an object of the class `model_set`, a list with the following major elements:

- `models`: A named list of parameter tables. Each represent the models identified.
- `bic`: A numeric vector, of the same length as `model`. The BIC of each model.
- `postprob`: A numeric vector, of the same length as `model`. The BIC posterior probability of each model.
- `fit`: A named list of `lavaan::lavaan()` output objects or `update()` for fitting a model with the added parameters, of the same length as `model`.
- `change`: A numeric vector, of the same length as `model`. The change in model df for each fit. A positive number denotes one less free parameter. A negative number denotes one more free parameter or one less constraint.
- `converged`: A named vector of boolean values, of the same length as `model`. Indicates whether each fit converged or not.
- `post_check`: A named vector of boolean values, of the same length as `model`. Indicates whether the solution of each fit is admissible or not. Checked by `lavaan::lavInspect()`.

The object returned by `gen_models()` depends on the argument `output`. See the argument `output` for the details

Functions

- `model_set()`: Compute the BPPs of a list of models. Can generate the models and/or fit the models. Can also accept pregenerated models, or just update BPPs.
- `gen_models()`: Generate a list of models (parameter tables).

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448>

References

Wu, H., Cheung, S. F., & Leung, S. O. (2020). Simple use of BIC to assess model selection uncertainty: An illustration using mediation and moderation models. *Multivariate Behavioral Research*, 55(1), 1–16. doi:10.1080/00273171.2019.1574546

See Also

[print.model_set\(\)](#)

Examples

```
library(lavaan)

dat <- dat_path_model

mod <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1
ab := a*b
"

fit <- sem(mod, dat_path_model, fixed.x = TRUE)

out <- model_set(fit)
out
```

model_set_combined *Two or More Hypothesized Models*

Description

Combine the 'model_set()' results of two or more hypothesis models.

Usage

```
model_set_combined(model_set_outputs, ...)
```

Arguments

model_set_outputs

This must be a named list of the outputs of [model_set\(\)](#). The names will be used as prefixes to name the models.

... Additional arguments to be passed to [model_set\(\)](#).

Details

There are cases in which users have more than one hypothesized model, each with its own set of neighboring models.

The function `model_set_combined()` let users combine the `model_set()` results two or more hypothesized model. Users can then compare the BPPs of these hypothesized models, as well as their neighboring models. Equivalent models will be removed in the process.

Value

A `model_set`-class object, which is simply an output of `model_set()`. All methods and functions for the output of `model_set()` will also work on this object.

See Also

[model_set\(\)](#)

Examples

```
library(lavaan)

mod1 <-
"
x4 ~ x1
x7 ~ x4
"

mod2 <-
"
x1 ~ x4
x7 ~ x4
"

fit1 <- sem(mod1,
            HolzingerSwineford1939,
            fixed.x = FALSE)
fit2 <- sem(mod2,
            HolzingerSwineford1939,
            fixed.x = FALSE)

out1 <- model_set(fit1)
out2 <- model_set(fit2)

out1
out2

outb <- model_set_combined(
  list(fit1 = out1,
       fit2 = out2))

outb
```

Description

For tasks such as comparing two parameter tables inside a partables-class object.

Usage

```
identical_partables(object1, object2)

is_partable(x)

same_variables(x)

get_partables(x)

to_partables(...)
```

Arguments

object1	A lavaan parameter table or similar object.
object2	A lavaan parameter table or similar object.
x	An object to be checked.
...	The objects to be combined.

Details

The function `identical_partables()` compare two lavaan parameter tables and see whether they are identical. (Adapted from a similar function in the package `semhelpinghands`).

The function `is_partable()` tries to check whether an object is "likely" to be a parameter table that can be used by `lavaan::lavaan()` and its wrappers, such as `lavaan::sem()`.

Note that there is no guarantee the the parameter table makes sense or will not lead to error when fitted. It can only check whether it has the required columns.

The function `same_variables()` check whether all parameter labels in a partables-class object use the same observed variables.

The function `get_partables()` extract the partable object from a `model_set`-class object.

The function `to_partables()` combine objects to create a partables-class object. The objects to be combined can be a lavaan-class object (e.g., the output of `lavaan::sem()`) or a parameter table of lavaan.

Value

The function `identical_partables()` returns either TRUE or FALSE.

The function `is_partable()` returns either TRUE or FALSE.

The function `same_variables()` returns either TRUE or FALSE.

The function `get_partables()` returns a partables-class object.

The function `to_partables()` returns a partables-class object, created from the objects supplied.

Examples

```
library(lavaan)
mod1 <-
"
x3 ~ x1
x2 ~ x4
"
mod2 <-
"
x2 ~ x4
x3 ~ x1
"
fit1 <- sem(mod1, dat_path_model)
fit2 <- sem(mod2, dat_path_model)
pt1 <- parameterTable(fit1)
pt2 <- parameterTable(fit2)
identical_partables(pt1, pt2)

is_partable(pt1)

out <- model_set(fit1,
                 fit_models = FALSE)
same_variables(get_partables(out))

out <- model_set(fit1,
                 fit_models = FALSE)
get_partables(out)

fit1 <- sem(mod1, dat_path_model)
fit2 <- sem(mod2, dat_path_model)
pt1 <- parameterTable(fit1)
pt2 <- parameterTable(fit2)

to_partables(fit1, fit2)
to_partables(pt1, pt2)
```

plot.model_graph *Plot a Network of Models*

Description

Plot a network of models generated by `model_graph()`.

Usage

```
## S3 method for class 'model_graph'  
plot(x, ...)
```

Arguments

`x` The output of `model_graph()`. (Named `x` because it is required in the naming of arguments of the `plot` generic function.)

`...` Additional arguments, passed to the `plot`-method of an `igraph` object.

Details

This function is the `plot` method of `model_graph` objects, the output of `model_graph()`.

For now, it simply passes the object to `plot`-method of an `igraph` object. This function is created for possible customization of the plot in the future.

Value

NULL. Called for its side effect.

See Also

[model_graph\(\)](#)

Examples

```
library(lavaan)  
  
dat <- dat_path_model  
  
mod <-  
"  
x3 ~ a*x1 + b*x2  
x4 ~ a*x1  
ab := a*b  
"  
  
fit <- sem(mod, dat_path_model, fixed.x = TRUE)  
  
out <- model_set(fit)
```

```

out

g <- model_graph(out)
plot(g)

```

print.model_set *Print a model_set-Class Object*

Description

Print the content of a model_set-class object.

Usage

```

## S3 method for class 'model_set'
print(
  x,
  bic_digits = 3,
  bpp_digits = 3,
  sort_models = TRUE,
  max_models = 20,
  bpp_target = NULL,
  target_name = "original",
  more_fit_measures = c("cfi", "rmsea", "srmr"),
  fit_measures_digits = 3,
  short_names = FALSE,
  cumulative_bpp = FALSE,
  ...
)

```

Arguments

x	A model_set-class object.
bic_digits	The number of decimal places to be displayed for BIC. Default is 3.
bpp_digits	The number of decimal places to be displayed for BIC posterior probability and prior probabilities. Default is 3.
sort_models	Whether the models will be sorted by BIC posterior probability. Default is TRUE.
max_models	The maximum number of models to be printed. Default is 20.
bpp_target	The desired BIC probability. Used to compute and print the minimum prior probability of the target model required to achieve bpp_target. Default is NULL.
target_name	The name of the target model as appeared in the model list. Default is "original". Used if bpp_target is not NULL.
more_fit_measures	Character vector. To be passed to <code>lavaan::fitMeasures()</code> . Default is <code>c("cfi", "rmsea", "srmr")</code> . Set it to NULL to disable printing additional fit measures.

<code>fit_measures_digits</code>	The number of decimal places to be displayed for additional fit measures, if requested. Default is 3.
<code>short_names</code>	If TRUE, then simple short names will be printed along with full model names. Default is FALSE. Short names can be used when interpreting the graph from <code>model_graph()</code> if short names are used in the graph.
<code>cumulative_bpp</code>	If TRUE and the models are sorted by BPPs, cumulative BPPs will be printed. Default is FALSE.
<code>...</code>	Optional arguments. Ignored.

Details

It is the print method of the output of `model_set()`.

Value

`x` is returned invisibly. Called for its side effect.

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448>

See Also

A `model_set`-class object is generated by `model_set()`.

Examples

```
library(lavaan)

dat <- dat_path_model

mod <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1
ab := a*b
"

fit <- sem(mod, dat_path_model, fixed.x = TRUE)

out <- model_set(fit)
out
```

print.partables	<i>Print a partables-Class Object</i>
-----------------	---------------------------------------

Description

Print the content of a partables-class object.

Usage

```
## S3 method for class 'partables'  
print(x, max_tables = 10, ...)
```

Arguments

x	A partables-class object.
max_tables	The maximum number of models to be printed. Default is 10.
...	Optional arguments. Ignored.

Details

The print method for the output of [gen_models\(\)](#), [get_add\(\)](#), and [get_drop\(\)](#).

Value

x is returned invisibly. Called for its side effect.

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448>

See Also

[gen_models\(\)](#), [get_add\(\)](#), and [get_drop\(\)](#).

Examples

```
library(lavaan)  
dat <- dat_path_model  
mod <-  
"  
x3 ~ a*x1 + b*x2  
x4 ~ a*x1  
ab := a*b  
"  
fit <- sem(mod, dat_path_model, fixed.x = TRUE)  
mod_to_add <- get_add(fit)  
mod_to_add  
print(mod_to_add, max_tables = 1)
```

```
mod_to_drop <- get_drop(fit)
mod_to_drop
print(mod_to_drop, max_tables = 1)
```

print.sem_outs *Print an sem_outs-Class Object*

Description

Print the content of an sem_outs-class object.

Usage

```
## S3 method for class 'sem_outs'
print(x, max_models = 20, ...)
```

Arguments

x	An sem_outs-class object.
max_models	The maximum number of models to be printed. Default is 20.
...	Optional arguments. Ignored.

Details

The print method for the output of fit_many().

Value

x is returned invisibly. Called for its side effect.

Author(s)

Shu Fai Cheung <https://orcid.org/0000-0002-9871-9448>

See Also

An sem_outs-class object is generated by fit_many().

Examples

```
library(lavaan)
dat <- dat_path_model
mod <-
"
x3 ~ a*x1 + b*x2
x4 ~ a*x1
ab := a*b
"
```

```
fit <- sem(mod, dat_path_model, fixed.x = TRUE)
mod_to_add <- get_add(fit)
out <- fit_many(mod_to_add, fit)
out
print(out, max_models = 1)
```

Index

- * **datasets**
 - dat_cfa, 4
 - dat_path_model, 5
 - dat_path_model_p06, 6
 - dat_sem, 6
 - dat_serial_4, 7
 - dat_serial_4_weak, 8
- c.model_set (c.partables), 2
- c.partables, 2
- dat_cfa, 4
- dat_path_model, 5
- dat_path_model_p06, 6
- dat_sem, 6
- dat_serial_4, 7
- dat_serial_4_weak, 8
- fit_many, 8
- gen_models (model_set), 21
- gen_models(), 20, 25, 33
- get_add, 10
- get_add(), 9, 23, 25, 33
- get_drop, 12, 25
- get_drop(), 9, 23, 33
- get_partables (partables_helpers), 28
- get_partables(), 28, 29
- identical_partables
 - (partables_helpers), 28
- identical_partables(), 28, 29
- is_partable (partables_helpers), 28
- is_partable(), 28, 29
- lavaan::cfa(), 15, 16
- lavaan::fitMeasures(), 31
- lavaan::lavaan, 9, 10, 13, 22
- lavaan::lavaan(), 9–14, 23–25, 28
- lavaan::lavInspect(), 9, 25
- lavaan::modificationIndices(), 12
- lavaan::parameterTable(), 3
- lavaan::sem(), 24, 28
- manipulate_partables (c.partables), 2
- measurement_invariance_models, 14
- min_prior, 16
- model_graph, 18
- model_graph(), 25, 30
- model_set, 21
- model_set(), 9, 12, 14, 16, 17, 20, 23, 25–27, 32
- model_set_combined, 26
- model_set_combined(), 27
- partables_drop (c.partables), 2
- partables_drop(), 3
- partables_helpers, 28
- plot.model_graph, 30
- plot.model_graph(), 20
- print.model_set, 31
- print.model_set(), 17, 26
- print.partables, 33
- print.partables(), 12, 14
- print.sem_outs, 34
- same_variables (partables_helpers), 28
- same_variables(), 28, 29
- to_partables (partables_helpers), 28
- to_partables(), 28, 29
- update(), 9, 12, 14, 25