

Package ‘gaussratiovegind’

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Title Distribution of Gaussian Ratios

Version 3.0.0

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Description It is well known that the distribution of a Gaussian ratio does not follow a Gaussian distribution.

The lack of awareness among users of vegetation indices about this non-Gaussian nature could lead to incorrect statistical modeling and interpretation.

This package provides tools to accurately handle and analyse such ratios: density function, parameter estimation, simulation.

An example on the study of chlorophyll fluorescence can be found in

A. El Ghaziri et al. (2023) <[doi:10.3390/rs15020528](https://doi.org/10.3390/rs15020528)>

and another method for parameter estimation is given in Bouhlel et al. (2023) <[doi:10.23919/EUSIPCO58844.2023.10290111](https://doi.org/10.23919/EUSIPCO58844.2023.10290111)>.

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URL <https://forge.inrae.fr/imhorphen/gaussratiovegind>

BugReports <https://forge.inrae.fr/imhorphen/gaussratiovegind/-/issues>

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Contents

arabidopsis	2
dnormratio	3
estpnormratio	5
kummer	8
lnpochhammer	9
pnormratio	10
pochhammer	11
rnormratio	12
Index	15

arabidopsis	<i>Statistics on Chlorophyll Fluorescence Parameters</i>
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Description

Mean and standard deviation values on healthy and diseased tissues of chlorophyll fluorescence parameters F_0 (minimum fluorescence) and F_m (maximum fluorescence) for a dataset of *Arabidopsis thaliana* plants infected with fungal pathogen data; parameters of the distribution of the ratio

$$\frac{F_v}{F_m} = \frac{F_m - F_0}{F_m}.$$

Usage

arabidopsis

Format

A data frame with 10 rows and 6 columns:

time times of the acquisition of chlorophyll fluorescence images

condition indicates if the plant was inoculated: healthy (inoculated with water) or diseased (inoculated with the pathogen)

mF0, sF0 Mean and standard deviation values of the chlorophyll parameter F_0

mFm, sFm Mean and standard deviation values of the chlorophyll parameter F_m

beta, rho, delta the β , ρ and δ_y parameters of the distribution of $\frac{F_v}{F_m} = \frac{F_m - F_0}{F_m}$ (distributed according to a normal ratio distribution, see Details)

Details

On each leaf picture, the F_0 and F_m values are normally distributed. Hence, $\frac{F_0}{F_m}$ is a ratio of two normal distributions.

Let μ_{F_0} and σ_{F_0} the mean and standard deviation of F_0 and μ_{F_m} and σ_{F_m} the mean and standard deviation of F_m . The parameters β , ρ and δ_y are given by:

$$\beta = \frac{\mu_{F_0}}{\mu_{F_m}}$$

$$\rho = \frac{\sigma_{F_m}}{\sigma_{F_0}}$$

$$\delta_y = \frac{\sigma_{F_m}}{\mu_{F_m}}$$

References

El Ghaziri, A., Bouhlel, N., Sapoukhina, N., Rousseau, D., On the importance of non-Gaussianity in chlorophyll fluorescence imaging. *Remote Sensing* 15(2), 528 (2023). doi:10.3390/rs15020528

Pavicic, M., Overmyer, K., Rehman, A.u., Jones, P., Jacobson, D., Himanen, K. Image-Based Methods to Score Fungal Pathogen Symptom Progression and Severity in Excised Arabidopsis Leaves. *Plants*, 10, 158 (2021). doi:10.3390/plants10010158

dnormratio

Density Function of a Normal Ratio Distribution

Description

Density of the ratio of two Gaussian distributions.

Usage

dnormratio(z, bet, rho, delta, r = 0)

Arguments

z length p numeric vector.
bet, rho, delta numeric values. The parameters (β, ρ, δ_y) of the distribution, see Details.
r numeric. The correlation coefficient. Default $r=0$ (the two distributions are considered independent).

Details

Let two independent random variables $X \sim N(\mu_x, \sigma_x)$ and $Y \sim N(\mu_y, \sigma_y)$.

If we denote $\beta = \frac{\mu_x}{\mu_y}$, $\rho = \frac{\sigma_y}{\sigma_x}$ and $\delta_y = \frac{\sigma_y}{\mu_y}$, the probability distribution function of the ratio

$Z = \frac{X}{Y}$ is given by:

$$f_Z(z; \beta, \rho, \delta_y) = \frac{\rho}{\pi(1 + \rho^2 z^2)} \left[\exp\left(-\frac{\rho^2 \beta^2 + 1}{2\delta_y^2}\right) + \sqrt{\frac{\pi}{2}} \rho \operatorname{erf}\left(\frac{q}{\sqrt{2}}\right) \exp\left(-\frac{\rho^2(z - \beta)^2}{2\delta_y^2(1 + \rho^2 z^2)}\right) \right]$$

with $q = \frac{1 + \beta\rho^2 z}{\delta_y \sqrt{1 + \rho^2 z^2}}$ and $\operatorname{erf}\left(\frac{q}{\sqrt{2}}\right) = \frac{2}{\sqrt{\pi}} \int_0^{\frac{q}{\sqrt{2}}} \exp(-t^2) dt$

Another expression of this density, used by the `estparnormratio()` function, is:

$$f_Z(z; \beta, \rho, \delta_y) = \frac{\rho}{\pi(1 + \rho^2 z^2)} \exp\left(-\frac{\rho^2 \beta^2 + 1}{2\delta_y^2}\right) {}_1F_1\left(1, \frac{1}{2}; \frac{1}{2\delta_y^2} \frac{(1 + \beta\rho^2 z)^2}{1 + \rho^2 z^2}\right)$$

where ${}_1F_1(a, b; x)$ is the confluent hypergeometric function (Kummer's function):

$${}_1F_1(a, b; x) = \sum_{n=0}^{+\infty} \frac{(a)_n}{(b)_n} \frac{x^n}{n!}$$

If X and Y are not independent, let $r = \operatorname{Cor}(X, Y) = \frac{\operatorname{Cov}(X, Y)}{\sigma_X \sigma_Y}$, the probability distribution of $Z = \frac{X}{Y}$ is:

$$f_Z(z; \beta, \rho, \delta_y, r) = \frac{\rho\sqrt{1-r^2}}{\pi(\rho^2 z^2 - 2r\rho z + 1)} \exp\left(-\frac{\rho^2 \beta^2 - 2r\beta\rho + 1}{2(1-r^2)\delta_y^2}\right) {}_1F_1\left(1, \frac{1}{2}; \frac{1}{2(1-r^2)\delta_y^2} \frac{(\beta\rho^2 z - r\rho(z + \beta) + 1)^2}{\rho^2 z^2 - 2r\rho z + 1}\right)$$

Value

Numeric: the value of density.

Author(s)

Pierre Santagostini, Angéline El Ghaziri, Nizar Bouhlel

References

El Ghaziri, A., Bouhlel, N., Sapoukhina, N., Rousseau, D., On the importance of non-Gaussianity in chlorophyll fluorescence imaging. *Remote Sensing* 15(2), 528 (2023). doi:10.3390/rs15020528

Marsaglia, G. 2006. Ratios of Normal Variables. *Journal of Statistical Software* 16. doi:10.18637/jss.v016.i04

Díaz-Francés, E., Rubio, F.J., On the existence of a normal approximation to the distribution of the ratio of two independent normal random variables. *Stat Papers* 54, 309–323 (2013). doi:10.1007/s0036201204292

Pham-Gia, T., Turkkan, N., Marchand, E. (2006) Density of the Ratio of Two Normal Random Variables and Applications, *Communications in Statistics - Theory and Methods*, 35:9, 1569-1591. doi:10.1080/03610920600683689

See Also

`pnormratio()`: probability distribution function.

`rnormratio()`: sample simulation.

`estparnormratio()`: parameter estimation.

Examples

```
# First example: ratio of independent variables
beta1 <- 0.15
rho1 <- 5.75
delta1 <- 0.22
dnormratio(0, bet = beta1, rho = rho1, delta = delta1)
dnormratio(0.5, bet = beta1, rho = rho1, delta = delta1)
curve(dnormratio(x, bet = beta1, rho = rho1, delta = delta1),
      from = -0.1, to = 0.7)

# Second example: ratio of correlated variables
beta2 <- 2
rho2 <- 2
delta2 <- 2
r2 <- 0.8
dnormratio(0, bet = beta2, rho = rho2, delta = delta2, r = r2)
dnormratio(1, bet = beta2, rho = rho2, delta = delta2, r = r2)
curve(dnormratio(x, bet = beta2, rho = rho2, delta = delta2, r = r2),
      from = -1.5, to = 2.5)
```

 estparnormratio

Estimation of the Parameters of a Normal Ratio Distribution

Description

Estimation of the parameters of a ratio $Z = \frac{X}{Y}$, X and Y being two random variables distributed according to Gaussian distributions, using the EM (estimation-maximization) algorithm or variational inference. Depending on the estimation method, the `estparnormratio` function calls `estparEM` (EM algorithm) or `estparVB` (variational Bayes).

Usage

```
estparnormratio(z, method = c("EM", "VB"), indep = TRUE, eps = 1e-06,
               na.rm = FALSE, display = FALSE, graph = FALSE,
               xlim = NULL, ylim = NULL, mux0 = 1, sigmax0 = 1,
               alphax0 = NULL, betax0 = NULL, muy0 = 1, sigmay0 = 1,
               alphay0 = NULL, betay0 = NULL,
               cov0 = 0)

estparEM(z, indep = TRUE, eps = 1e-06, na.rm = FALSE,
         display = FALSE, graph = FALSE, xlim = NULL, ylim = NULL,
         mux0 = 1, sigmax0 = 1, muy0 = 1, sigmay0 = 1, cov0 = 0)

estparVB(z, eps = 1e-06, na.rm = FALSE, display = FALSE,
         graph = FALSE, xlim = NULL, ylim = NULL,
         mux0 = 1, sigmax0 = 1, alphax0 = 1, betax0 = 1,
         muy0 = 1, sigmay0 = 1, alphay0 = 1, betay0 = 1)
```

Arguments

z	numeric.
method	the method used to estimate the parameters of the distribution. It can be "EM" (expectation-maximization) or "VB" (Variational Bayes).
indep	logical. If indep=TRUE (default) X and Y are two independent Gaussian variables and the parameters β , ρ and δ_{y^2} parameters of $Z = \frac{X}{Y}$ are estimated. If indep=FALSE, X and Y can be correlated, and the correlation coefficient r is also estimated.
eps	numeric. Precision for the estimation of the parameters (see Details).
na.rm	a logical evaluating to TRUE or FALSE indicating whether NA values should be stripped before the computation proceeds.
display	logical. When TRUE the successive values of the parameters are printed.
graph	logical. When TRUE the successive values of the parameters are plotted.
xlim, ylim	if graph is TRUE, the x and y limits of the plot. Default: xlim = c(0, 1000) and ylim depend on the initial values of the parameters: ylim = 10*c(0, max(theta)).
mux0, sigmax0, muy0, sigmay0	initial values of the means and standard deviations of the X and Y variables. Default: mux0 = 1, sigmax0 = 1, muy0 = 1, sigmay0 = 1.
alphax0, betax0, alphay0, betay0	initial values for the variational Bayes method. Omitted if method="EM". If method="VB", if omitted, they are set to 1.
cov0	initial value of the covariance of X and Y . If indep is FALSE, cov0 must be different from 0.

Details

Let a random variable: $Z = \frac{X}{Y}$,

X and Y being normally distributed: $X \sim N(\mu_x, \sigma_x)$ and $Y \sim N(\mu_y, \sigma_y)$.

The probability density of Z is:

$$f_Z(z; \beta, \rho, \delta_y, r) = \frac{\rho\sqrt{1-r^2}}{\pi(\rho^2 z^2 - 2r\rho z + 1)} \exp\left(-\frac{\rho^2 \beta^2 - 2r\beta\rho + 1}{2(1-r^2)\delta_y^2}\right) {}_1F_1\left(1, \frac{1}{2}; \frac{1}{2(1-r^2)\delta_y^2} \frac{(\beta\rho^2 z - r\rho(z + \beta) + 1)^2}{\rho^2 z^2 - 2r\rho z + 1}\right)$$

with: $\beta = \frac{\mu_x}{\mu_y}$, $\rho = \frac{\sigma_y}{\sigma_x}$, $\delta_y = \frac{\sigma_y}{\mu_y}$, $r = \text{Cor}(X, Y) = \frac{\text{Cov}(X, Y)}{\sigma_X \sigma_Y}$.

and ${}_1F_1(a, b; x)$ is the confluent hypergeometric function (Kummer's function):

$${}_1F_1(a, b; x) = \sum_{n=0}^{+\infty} \frac{(a)_n x^n}{(b)_n n!}$$

If X and Y are independent ($r = 0$), the probability density is:

$$f_Z(z; \beta, \rho, \delta_y, r = 0) = f_Z(z; \beta, \rho, \delta_y) = \frac{\rho}{\pi(1 + \rho^2 z^2)} \exp\left(-\frac{\rho^2 \beta^2 + 1}{2\delta_y^2}\right) {}_1F_1\left(1, \frac{1}{2}; \frac{1}{2\delta_y^2} \frac{(1 + \beta\rho^2 z)^2}{1 + \rho^2 z^2}\right)$$

If method = "EM", the means and standard deviations μ_x , σ_x , μ_y and σ_y and the correlation coefficient r are estimated with the EM algorithm.

When $r = 0$, μ_x , σ_x , μ_y and σ_y are estimated using the algorithm presented in El Ghaziri et al.

If method = "VB", they are estimated with the variational Bayes method as presented in Bouhlel et al. For now, this method is available only for the case when X and Y are independent, i.e. $r = 0$.

Then the parameters β , ρ , δ_y of the Z distribution are computed from these means and standard deviations.

The estimation of μ_x , σ_x , μ_y and σ_y uses an iterative algorithm. The precision for their estimation is given by the eps parameter.

The computation uses the `kummer` function.

If there are ties in the z vector, it generates a warning, as there should be no ties in data distributed among a continuous distribution.

Value

A list of 4 elements beta, rho, delta, r: the estimated parameters of the Z distribution $\hat{\beta}$, $\hat{\rho}$, $\hat{\delta}_y$ and \hat{r} , with three attributes `attr(, "epsilon")` (precision of the result), `attr(, "k")` (number of iterations) and `attr(, "method")` (estimation method).

If `indep=FALSE`, r is not estimated, it is set to 0.

Author(s)

Pierre Santagostini, Angéline El Ghaziri, Nizar Bouhlel

References

El Ghaziri, A., Bouhlel, N., Sapoukhina, N., Rousseau, D., On the importance of non-Gaussianity in chlorophyll fluorescence imaging. *Remote Sensing* 15(2), 528 (2023). [doi:10.3390/rs15020528](https://doi.org/10.3390/rs15020528)

Bouhlel, N., Mercier, F., El Ghaziri, A., Rousseau, D., Parameter Estimation of the Normal Ratio Distribution with Variational Inference. 2023 31st European Signal Processing Conference (EU-SIPCO), Helsinki, Finland, 2023, pp. 1823-1827. [doi:10.23919/EUSIPCO58844.2023.10290111](https://doi.org/10.23919/EUSIPCO58844.2023.10290111)

See Also

`dnormratio()`: probability density of a normal ratio.

`rnormratio()`: sample simulation.

Examples

```
# First example: ratio of independent variables
beta1 <- 0.15
rho1 <- 5.75
delta1 <- 0.22

set.seed(1234)
z1 <- rnormratio(800, bet = beta1, rho = rho1, delta = delta1)
```

```

# With the EM method:
estparnormratio(z1, method = "EM", indep = TRUE)

# With the variational method:
estparnormratio(z1, method = "VB")

# Second example: ratio of correlated variables
beta2 <- 0.24
rho2 <- 4.21
delta2 <- 0.25
r2 <- 0.8

set.seed(1234)
z2 <- rnormratio(800, bet = beta2, rho = rho2, r = r2, delta = delta2)

# With the EM method:
estparnormratio(z2, method = "EM", indep = FALSE)

```

kummer

Confluent D-Hypergeometric Function

Description

Computes the Kummer's function, or confluent hypergeometric function.

Usage

```
kummer(a, b, z, eps = 1e-06)
```

Arguments

a	numeric.
b	numeric
z	numeric vector.
eps	numeric. Precision for the sum (default 1e-06).

Details

The Kummer's confluent hypergeometric function is given by:

$${}_1F_1(a, b; z) = \sum_{n=0}^{+\infty} \frac{(a)_n z^n}{(b)_n n!}$$

where $(z)_p$ is the Pochhammer symbol (see [pochhammer](#)).

The eps argument gives the required precision for its computation. It is the attr(, "epsilon") attribute of the returned value.

Value

A numeric value: the value of the Kummer's function, with two attributes `attr(, "epsilon")` (precision of the result) and `attr(, "k")` (number of iterations).

Author(s)

Pierre Santagostini, Angéline El Ghaziri, Nizar Bouhlel

References

El Ghaziri, A., Bouhlel, N., Sapoukhina, N., Rousseau, D., On the importance of non-Gaussianity in chlorophyll fluorescence imaging. *Remote Sensing* 15(2), 528 (2023). [doi:10.3390/rs15020528](https://doi.org/10.3390/rs15020528)

Inpochhammer

Logarithm of the Pochhammer Symbol

Description

Computes the logarithm of the Pochhammer symbol.

Usage

`Inpochhammer(x, n)`

Arguments

<code>x</code>	numeric.
<code>n</code>	positive integer.

Details

The Pochhammer symbol is given by:

$$(x)_n = \frac{\Gamma(x+n)}{\Gamma(x)} = x(x+1)\dots(x+n-1)$$

So, if $n > 0$:

$$\log((x)_n) = \log(x) + \log(x+1) + \dots + \log(x+n-1)$$

If $n = 0$, $\log((x)_n) = \log(1) = 0$

Value

Numeric value. The logarithm of the Pochhammer symbol.

Author(s)

Pierre Santagostini, Nizar Bouhlel

See Also

[pochhammer](#), [kummer](#)

Examples

```
Inpochhammer(2, 0)
Inpochhammer(2, 1)
Inpochhammer(2, 3)
```

pnormratio

Cumulative Distribution of a Normal Ratio Distribution

Description

Cumulative distribution of the ratio of two Gaussian distributions.

Usage

```
pnormratio(z, bet, rho, delta, r = 0)
```

Arguments

`z` length p vector of quantiles.
`bet, rho, delta` numeric values. The parameters (β, ρ, δ_y) of the distribution, see Details.
`r` numeric. The correlation coefficient. Default $r=0$ (the two distributions are considered independent).

Details

Let two random variables $X \sim N(\mu_x, \sigma_x)$ and $Y \sim N(\mu_y, \sigma_y)$ with correlation coefficient r .

If we denote $f_Z(z; \beta, \rho, \delta_y, r)$ the probability distribution function of the ratio $Z = \frac{X}{Y}$, with $\beta =$

$\frac{\mu_x}{\mu_y}$, $\rho = \frac{\sigma_y}{\sigma_x}$, $\delta_y = \frac{\sigma_y}{\mu_y}$ and $r = Cor(X, Y) = \frac{Cov(X, Y)}{\sigma_x \sigma_y}$ (see [dnormratio\(\)](#), Details section).

The cumulative distribution for Z is given by:

$$F(z; \beta, \rho, \delta_y) = \int_{-\infty}^z f_Z(z; \beta, \rho, \delta_y, r) dz$$

This integral is computed using numerical integration.

Value

Numeric: the value of density.

Author(s)

Pierre Santagostini, Angélica El Ghaziri, Nizar Bouhlel

References

El Ghaziri, A., Bouhlel, N., Sapoukhina, N., Rousseau, D., On the importance of non-Gaussianity in chlorophyll fluorescence imaging. *Remote Sensing* 15(2), 528 (2023). doi:10.3390/rs15020528

Marsaglia, G. 2006. Ratios of Normal Variables. *Journal of Statistical Software* 16. doi:10.18637/jss.v016.i04

Díaz-Francés, E., Rubio, F.J., On the existence of a normal approximation to the distribution of the ratio of two independent normal random variables. *Stat Papers* 54, 309–323 (2013). doi:10.1007/s0036201204292

See Also

[dnormratio\(\)](#): density function.

[rnormratio\(\)](#): sample simulation.

[estparnormratio\(\)](#): parameter estimation.

Examples

```
# First example: ratio of independent variables
beta1 <- 0.15
rho1 <- 5.75
delta1 <- 0.22
pnormratio(0, bet = beta1, rho = rho1, delta = delta1)
pnormratio(0.5, bet = beta1, rho = rho1, delta = delta1)
curve(pnormratio(x, bet = beta1, rho = rho1, delta = delta1), from = -0.1, to = 0.7)

# Second example: ratio of correlated variables
beta2 <- 2
rho2 <- 2
delta2 <- 2
r2 <- 0.8
pnormratio(0, bet = beta2, rho = rho2, delta = delta2, r = r2)
pnormratio(1, bet = beta2, rho = rho2, delta = delta2, r = r2)
curve(pnormratio(x, bet = beta2, rho = rho2, delta = delta2, r = r2),
      from = -1.5, to = 2.5)
```

pochhammer

Pochhammer Symbol

Description

Computes the Pochhammer symbol.

Usage

```
pochhammer(x, n)
```

Arguments

x	numeric.
n	positive integer.

Details

The Pochhammer symbol is given by:

$$(x)_n = \frac{\Gamma(x+n)}{\Gamma(x)} = x(x+1)\dots(x+n-1)$$

Value

Numeric value. The value of the Pochhammer symbol.

Author(s)

Pierre Santagostini, Nizar Bouhlel

See Also

[lnpochhammer](#), [kummer](#)

Examples

```
pochhammer(2, 0)
pochhammer(2, 1)
pochhammer(2, 3)
```

rnormratio

Simulate from a Normal Ratio Distribution

Description

Simulate data from a ratio of two Gaussian distributions.

Usage

```
rnormratio(n, bet, rho, delta, r = 0)
```

Arguments

n	integer. Number of observations. If length(n) > 1, the length is taken to be the number required.
bet, rho, delta	numeric values. The parameters (β, ρ, δ_y) of the distribution, see Details.
r	numeric. The correlation coefficient. Default r=0 (the two distributions are considered independent).

Details

Let two random variables $X \sim N(\mu_x, \sigma_x)$ and $Y \sim N(\mu_y, \sigma_y)$

with probability densities f_X and f_Y .

The parameters of the distribution of the ratio $Z = \frac{X}{Y}$ are: $\beta = \frac{\mu_x}{\mu_y}$, $\rho = \frac{\sigma_y}{\sigma_x}$, $\delta_y = \frac{\sigma_y}{\mu_y}$ and

$$r = Cor(X, Y) = \frac{Cov(X, Y)}{\sigma_x \sigma_y}.$$

μ_x , σ_x , μ_y and σ_y are computed from β , ρ and δ_y (by fixing arbitrarily $\mu_x = 1$).

If X and Y are independent, i.e. $r = 0$, two random samples (x_1, \dots, x_n) and (y_1, \dots, y_n) are simulated.

If X and Y are not independent, a sample $((x_1, y_1), \dots, (x_n, y_n))$ is simulated using `MASS::mvrnorm()`.

Then $\left(\frac{x_1}{y_1}, \dots, \frac{x_n}{y_n}\right)$ is returned.

Value

A numeric vector: the produced sample.

Author(s)

Pierre Santagostini, Angéline El Ghaziri, Nizar Bouhlel

References

El Ghaziri, A., Bouhlel, N., Sapoukhina, N., Rousseau, D., On the importance of non-Gaussianity in chlorophyll fluorescence imaging. *Remote Sensing* 15(2), 528 (2023). doi:10.3390/rs15020528

Marsaglia, G. 2006. Ratios of Normal Variables. *Journal of Statistical Software* 16. doi:10.18637/jss.v016.i04

Díaz-Francés, E., Rubio, F.J., On the existence of a normal approximation to the distribution of the ratio of two independent normal random variables. *Stat Papers* 54, 309–323 (2013). doi:10.1007/s0036201204292

Pham-Gia, T., Turkkan, N., Marchand, E. (2006) Density of the Ratio of Two Normal Random Variables and Applications, *Communications in Statistics - Theory and Methods*, 35:9, 1569-1591. doi:10.1080/03610920600683689

See Also

[dnormratio\(\)](#): probability density of a normal ratio.

[pnormratio\(\)](#): probability distribution function.

[estparnormratio\(\)](#): parameter estimation.

Examples

```
# First example: ratio of independent variables
beta1 <- 0.15
rho1 <- 5.75
delta1 <- 0.22
rnormratio(20, bet = beta1, rho = rho1, delta = delta1)
```

```
# Second example: ratio of correlated variables
beta2 <- 0.24
rho2 <- 4.21
delta2 <- 0.25
r2 <- 0.8
rnormratio(20, bet = beta2, rho = rho2, delta = delta2, r = r2)
```

Index

* datasets

arabidopsis, 2

arabidopsis, 2

dnormratio, 3

dnormratio(), 7, 10, 11, 14

estparEM (estparnormratio), 5

estparnormratio, 5

estparnormratio(), 4, 11, 14

estparnormratio, estparEM, estparVB

(estparnormratio), 5

estparVB (estparnormratio), 5

kummer, 7, 8, 10, 12

lnpochhammer, 9, 12

MASS::mvrnorm(), 13

pnormratio, 10

pnormratio(), 4, 14

pochhammer, 8, 10, 11

rnormratio, 12

rnormratio(), 4, 7, 11