

Package ‘cpfa’

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Description Classification using Richard A. Harshman's Parallel Factor Analysis-1 (Parafac) model or Parallel Factor Analysis-2 (Parafac2) model fit to a three-way or four-way data array. See Harshman and Lundy (1994): <doi:10.1016/0167-9473(94)90132-5>. Principal component analysis (PCA) is also supported for a two-way data matrix. Uses component weights from one mode of a Parafac, Parafac2, or PCA model as features to tune parameters for one or more classification methods via a k-fold cross-validation procedure. Allows for constraints on different tensor modes. Supports penalized logistic regression, support vector machine, random forest, feed-forward neural network, regularized discriminant analysis, and gradient boosting machine. Supports binary and multiclass classification. Predicts class labels or class probabilities and calculates multiple classification performance measures. Implements parallel computing via the 'parallel', 'doParallel', and 'doRNG' packages.

License GPL (>= 2)

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cpfa

Classification with Parallel Factor Analysis

Description

Fits Richard A. Harshman's Parallel Factor Analysis-1 (Parafac) model or Parallel Factor Analysis-2 (Parafac2) model to a three-way or four-way data array. Also fits a principal component analysis model (PCA) to a two-way matrix. Allows for different constraint options on multiple tensor modes. For PCA, allows for either an unrotated or varimax rotated solution. Uses component weights from a single mode of the selected component model as predictors to tune parameters for one or more classification methods via a k-fold cross-validation procedure. Predicts class labels and calculates multiple performance measures for binary or multiclass classification across multiple replications with different train-test splits. Provides descriptive statistics to pool output across replications.

Usage

```
cpfa(x, y, model = c("parafac", "parafac2", "pca"), nfac = 1, nrep = 5,
     ratio = 0.8, nfolds = 10,
     method = c("PLR", "SVM", "RF", "NN", "RDA", "GBM"),
     family = c("binomial", "multinomial"), parameters = list(),
     type.out = c("measures", "descriptives"), foldid = NULL, prior = NULL,
     cmode = NULL, seeds = NULL, plot.out = FALSE, plot.measures = NULL,
     parallel = FALSE, cl = NULL, verbose = TRUE, compscale = TRUE,
     pcarot = c("unrotated", "varimax"), ...)
```

Arguments

- x A three-way or four-way data array. For Parafac2, can be a list where each element is a matrix or three-way array. Array or list must contain only real numbers. See note below. For PCA, can be a two-way matrix, a three-way array, or a four-way array. If a three-way or four-way array for PCA, array is unfolded across all modes except the classification mode. Note that if three-way or four-way array for PCA, classification mode must be the last mode.
- y A vector containing at least two unique class labels. Should be a factor that contains two or more levels. For binary case, ensure the order of factor levels (left to right) is such that negative class is first and positive class is second. Levels should be sequential integers starting from 0, 1, ..., etc.

model	Character designating the component model to use, including: model = "parafac" to fit the Parafac model, model = "parafac2" to fit the Parafac2 model, or model = "pca" to fit the PCA model.
nfac	Vector containing integers that specify the number of components for each component model to fit. Default is nfac = 1.
nrep	Number of replications to repeat the procedure. Default is nrep = 5.
ratio	Split ratio for dividing data into train and test sets. Default is ratio = 0.8.
nfolds	Numeric value specifying number of folds for k-fold cross-validation. Must be 2 or greater. Default is nfolds = 10.
method	Character vector indicating classification methods to use. Possible methods include penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM). If none are selected, default is to use all methods with method = c("PLR", "SVM", "RF", "NN", "RDA", "GBM").
family	Character value specifying binary classification (family = "binomial") or multiclass classification (family = "multinomial"). If not provided, number of levels of input y is used, where two levels is binary, and where three or more levels is multiclass.
parameters	List containing arguments related to classification methods. When specified, must contain one or more of the following: <p>alpha Values for penalized logistic regression alpha parameter; default is alpha = seq(0, 1, length = 6). Must be numeric and contain only real numbers between 0 and 1, inclusive.</p> <p>lambda Optional user-supplied lambda sequence for cv.glmnet for penalized logistic regression. Default is NULL.</p> <p>cost Values for support vector machine cost parameter; default is cost = c(1, 2, 4, 8, 16, 32, 64). Must be numeric and contain only real numbers greater than 0.</p> <p>gamma Values for support vector machine gamma parameter; default is gamma = c(0, 0.01, 0.1, 1, 10, 100, 1000). Must be numeric and greater than or equal to 0.</p> <p>ntree Values for random forest number of trees parameter; default is ntree = c(100, 200, 400, 600, 800, 1600, 3200). Must be numeric and contain only integers greater than or equal to 1.</p> <p>nodesize Values for random forest node size parameter; default is nodesize = c(1, 2, 4, 8, 16, 32, 64). Must be numeric and contain only integers greater than or equal to 1.</p> <p>size Values for neural network size parameter; default is size = c(1, 2, 4, 8, 16, 32, 64). Must be numeric and contain only integers greater than or equal to 0.</p> <p>decay Values for neural network decay parameter; default is decay = c(0.001, 0.01, 0.1, 1, 2, 4, 8, 16). Must be numeric and contain only real numbers.</p>

	<p>rda.alpha Values for regularized discriminant analysis alpha parameter; default is <code>rda.alpha = seq(0, 0.999, length = 6)</code>. Must be numeric and contain only real numbers between 0 (inclusive) and 1 (exclusive).</p> <p>delta Values for regularized discriminant analysis delta parameter; default is <code>delta = c(0, 0.1, 1, 2, 3, 4)</code>. Must be numeric and contain only real numbers greater than or equal to 0.</p> <p>eta Values for gradient boosting machine eta parameter; default is <code>eta = c(0.1, 0.3, 0.5, 0.7, 0.9)</code>. Must be numeric and contain only real numbers greater than 0 and less than 1.</p> <p>max.depth Values for gradient boosting machine max.depth parameter; default is <code>max.depth = c(1, 2, 3, 4)</code>. Must be numeric and contain only integers greater than or equal to 1.</p> <p>subsample Values for gradient boosting machine subsample parameter; default is <code>subsample = c(0.6, 0.7, 0.8, 0.9)</code>. Must be numeric and contain only real numbers greater than 0 and less than or equal to 1.</p> <p>nrounds Values for gradient boosting machine nrounds parameter; default is <code>nrounds = c(100, 200, 300, 500)</code>. Must be numeric and contain only integers greater than or equal to 1.</p>
type.out	Type of output desired: <code>type.out = "measures"</code> returns an array containing classification performance measures for all replications while <code>type.out = "descriptives"</code> returns the list of descriptive statistics calculated across all replications for each performance measure. Both options also provide the estimated training weights and classification weights. Defaults to <code>type.out = "descriptives"</code> .
foldid	List containing, for each replication, an integer vector. Should have length equal to <code>'nrep'</code> . Each list element contains fold IDs for k-fold cross-validation. If not provided, fold IDs are generated randomly for the number of folds <code>nfolds</code> .
prior	Prior probabilities of class membership. If specified, the probabilities should be in the order of the factor levels of input <code>y</code> . If unspecified, the observed class proportions for input <code>y</code> are used. Based on <code>prior</code> , inverse probability weights are calculated to account for class imbalance. Note that RF and RDA ignore <code>prior</code> and use uniform priors to handle imbalance.
cmode	Integer value of 1, 2, or 3 (or 4 if <code>x</code> is a four-way array) specifying the mode whose component weights will be predictors for classification. Defaults to the last mode of the input array (i.e., defaults to 3 for a three-way array, and to 4 for a four-way array). If <code>model = "parafac2"</code> , the last mode will be used. If <code>model = "pca"</code> , and if input <code>x</code> is a matrix, <code>cmode</code> can be 1 or 2; if not provided, defaults to 1. However, if <code>model = "pca"</code> , and if input <code>x</code> is a 3-way or 4-way array, <code>cmode</code> must be the last mode when supplied.
seeds	Random seeds to be associated with each replication. Default is <code>seeds = 1:nrep</code> .
plot.out	Logical indicating whether to output one or more box plots of classification performance measures that are plotted across classification methods and number of components.
plot.measures	Character vector containing values that specify for plotting one or more of 11 possible classification performance measures. Only relevant when <code>plot.out = TRUE</code> . Should contain one or more of the following labels: <code>c("err", "acc", "tpr", "fpr", "tnr", "fnr", "ppv", "npv", "fdr", "fom", "fs")</code> . A box

	plot will be created for each measure that is specified, summarizing output across replications. Note that additional information about each label is available in the Details section of the help file for function <code>cpm</code> . If <code>NULL</code> , defaults to classification accuracy.
<code>parallel</code>	Logical indicating if parallel computing should be implemented. If <code>TRUE</code> , the package parallel is used for parallel computing. For all classification methods except penalized logistic regression, the doParallel package is used as a wrapper. Defaults to <code>FALSE</code> , which implements sequential computing.
<code>c1</code>	Cluster for parallel computing, which is used when <code>parallel = TRUE</code> . Note that if <code>parallel = TRUE</code> and <code>c1 = NULL</code> , then the cluster is defined as <code>makeCluster(detectCores())</code> .
<code>verbose</code>	If <code>TRUE</code> , progress is printed.
<code>compscale</code>	Logical indicating whether to scale each column of the estimated classification component weights matrix (i.e., the features/predictors). If <code>TRUE</code> , each column is scaled to have mean zero and unit variance. If <code>FALSE</code> , no scaling is performed.
<code>pcarot</code>	Character indicating whether to apply a varimax rotation or leave PCA loadings unrotated when <code>model</code> is set to <code>pca</code> . Ignored when <code>model</code> is not <code>pca</code> . Defaults to "unrotated" if not specified.
<code>...</code>	Additional arguments to be passed to function <code>parafac</code> for fitting a Parafac model or function <code>parafac2</code> for fitting a Parafac2 model. Example: can impose different constraints on different modes of the input array using the argument <code>const</code> . See help file for function <code>parafac</code> or for function <code>parafac2</code> for additional details.

Details

Data are split into a training set and a testing set. After fitting a Parafac or Parafac2 model with the training set using package **multiway** (see `parafac` or `parafac2` in **multiway** for details), or after fitting a PCA model using the singular value decomposition, the estimated classification mode weight matrix is passed to one or more classification methods. The methods include: penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM).

Package **glmnet** fits models for PLR. PLR tunes penalty parameter λ while the elastic net parameter α is set by the user (see the help file for function `cv.glmnet` in package **glmnet**). For SVM, package **e1071** is used with a radial basis kernel. Penalty parameter `cost` and radial basis parameter `gamma` are used (see `svm` in package **e1071**). For RF, package **randomForest** is used and implements Breiman's random forest algorithm. The number of predictors sampled at each node split is set at the default of \sqrt{R} , where R is the number of Parafac or Parafac2 components. Two tuning parameters allowed are `ntree`, the number of trees to be grown, and `nodesize`, the minimum size of terminal nodes (see `randomForest` in package **randomForest**). For NN, package **nnet** fits a single-hidden-layer, feed-forward neural network model. Penalty parameters `size` (i.e., number of hidden layer units) and `decay` (i.e., weight decay) are used (see **nnet**). For RDA, package **rda** fits a shrunken centroids regularized discriminant analysis model. Tuning parameters include `rda.alpha`, the shrinkage penalty for the within-class covariance matrix, and `delta`, the shrinkage penalty of class centroids towards the overall dataset centroid. For GBM, package **xgboost** fits a gradient boosting machine model. Four tuning parameters are allowed: (1) `eta`, the learning rate; (2) `max.depth`, the maximum tree depth; (3) `subsample`, the fraction of samples per tree; and (4) `nrounds`, the number of boosting trees to build.

For all six methods, k-fold cross-validation is implemented to tune classification parameters where the number of folds is set by argument `nfold`s. Separately, the trained Parafac, Parafac2, or PCA model is used to predict the classification mode's component weights using the testing set data. The predicted component weights and the optimized classification method are then used to predict class labels. Finally, classification performance measures are calculated. The process is repeated over a number of replications with different random splits of the input array and of the class labels at each replication.

Value

Returns an object of class `wrapcpfa` that either (1) contains a three-way array with classification performance measures for each model and for each replication, or (2) contains a list with matrices with descriptive statistics for performance measures calculated across all replications. Specify `type.out = "measures"` to output the array of performance measures. Specify `type.out = "descriptives"` to output descriptive statistics across replications. In addition, for either option, the returned list object includes the following:

<code>predweights</code>	List of predicted classification weights for each Parafac, Parafac2, or PCA model and for each replication.
<code>train.weights</code>	List of lists of training weights for each Parafac, Parafac2, or PCA model and for each replication.
<code>opt.tune</code>	List of optimal tuning parameters for classification methods for each Parafac or Parafac2 model and for each replication.
<code>mean.opt.tune</code>	Mean across all replications of optimal tuning parameters for classification methods for each Parafac or Parafac2 model.
<code>X</code>	Two-way matrix, or three-way or four-way data array or list used in argument <code>x</code> . If <code>x</code> was a three-way or four-way array, and if <code>model</code> was <code>pca</code> , returns the flattened two-way matrix.
<code>y</code>	Vector of class labels used in input argument <code>y</code> .
<code>nfac</code>	Number of components used to fit each Parafac, Parafac2, or PCA model.
<code>model</code>	Character designating the component model that was used, including: <code>model = "parafac"</code> for the Parafac model, <code>model = "parafac2"</code> for the Parafac2 model, or <code>model = "pca"</code> for the PCA model.
<code>method</code>	Classification methods used.
<code>const</code>	Constraints used in fitting the Parafac, Parafac2, or PCA model. When <code>model</code> was <code>pca</code> , contains the value used in input <code>pcarot</code> to indicate whether a rotation was applied to the solution.
<code>cmode</code>	Integer value used to specify the mode whose component weights were predictors for classification.
<code>family</code>	Character value used to specify binary classification (<code>family = "binomial"</code>) or multiclass classification (<code>family = "multinomial"</code>).
<code>lxdim</code>	Integer specifying the number of modes of the output <code>x</code> . Identical to the number of modes of input <code>x</code> , except when input <code>x</code> was a 3-way or 4-way array and when <code>model</code> was <code>pca</code> . In this case, <code>lxdim</code> is 2.

trainIDs	List where each element contains the vector of integer IDs that specify the rows/observations of the classification mode assigned to the train set for a given replication.
testIDs	List where each element contains the vector of integer IDs that specify the rows/observations of the classification mode assigned to the test set for a given replication.
flattened	Logical indicating whether input <code>x</code> was flattened into a two-way matrix. Only TRUE when <code>model</code> was <code>pca</code> and input <code>x</code> was a 3-way or 4-way array.

Note

For Parafac and Parafac2, if argument `cmode` is not null, input array `x` is reshaped with function `aperm` such that the `cmode` dimension of `x` is ordered last. Estimated mode A and B (and mode C for a four-way array) weights that are outputted as `Aweights` and `Bweights` (and `Cweights`) reflect this permutation. For example, if `x` is a four-way array and `cmode = 2`, the original input modes 1, 2, 3, and 4 will correspond to output modes 1, 3, 4, 2. Here, output A = input 1; B = 3, and C = 4 (i.e., the second mode specified by `cmode` has been moved to the D mode/last mode). For `model = "parafac2"`, classification mode is assumed to be the last mode (i.e., mode C for three-way array and mode D for four-way array). For PCA, if argument `cmode` is not NULL, and if `x` is a 3-way or 4-way array, the array is reshaped with `aperm` such that the `cmode` dimension of `x` is ordered first. Then, the array is unfolded into a two-way matrix. If `x` is already input as a two-way matrix, the matrix is reshaped if `cmode` is 2, such that the matrix is transposed. Note that for PCA, `Aweights` contains the PCA model loadings.

In addition, note that the following combination of arguments will give an error: `nfac = 1`, `family = "multinomial"`, `method = "PLR"`. The issue arises from providing `glmnet::cv.glmnet` input `x` an input matrix that has a single column. The issue is resolved for `family = "binomial"` because a column of 0s is appended to the single column, but this solution does not appear to work for the multiclass case. As such, this combination of arguments is not currently allowed. Future updates are planned to resolve this issue.

Applications of this function to real datasets can be explored at the following repository: <https://github.com/matthewasisgress/multiway-classification/>.

Author(s)

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Examples

```
##### Parafac2 example with 4-way array and multiclass response #####
## Not run:
# set seed
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),                # for A weights
                distG = list(dname = "gamma", shape = 2,
                             scale = 4))                # for G weights

# define target correlation matrix for columns of D mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# simulate a four-way ragged array connected to a response
```

```

data <- simcpfa(arraydim = c(10, 11, 12, 100), model = "parafac2", nfac = 3,
               nclass = 3, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
               meanpred = rep(2, 3), modes = 4, corrpred = cormat,
               technical = techlist, smethod = "eigende")

# initialize
alpha <- seq(0, 1, length = 20)
gamma <- c(0, 1)
cost <- c(0.1, 5)
ntree <- c(200, 300)
nodesize <- c(1, 2)
size <- c(1, 2)
decay <- c(0, 1)
rda.alpha <- seq(0.1, 0.9, length = 2)
delta <- c(0.1, 2)
eta <- c(0.3, 0.7)
max.depth <- c(1, 2)
subsample <- c(0.75)
nrounds <- c(100)
method <- c("PLR", "SVM", "RF", "NN", "RDA", "GBM")
family <- "multinomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost, ntree = ntree,
                  nodesize = nodesize, size = size, decay = decay,
                  rda.alpha = rda.alpha, delta = delta, eta = eta,
                  max.depth = max.depth, subsample = subsample,
                  nrounds = nrounds)

model <- "parafac2"
nfolds <- 10
nstart <- 10

# constrain first mode weights to be orthogonal, fourth mode to be nonnegative
const <- c("orthog", "uncons", "uncons", "nonneg")

# fit Parafac2 model and use fourth mode weights to tune classification
# methods, to predict class labels, and to return classification
# performance measures pooled across multiple train-test splits
output <- cpfa(x = data$X, y = data$y, model = model, nfac = 3,
              nrep = 5, ratio = 0.9, nfolds = nfolds, method = method,
              family = family, parameters = parameters,
              type.out = "descriptives", seeds = NULL, plot.out = TRUE,
              parallel = FALSE, const = const, nstart = nstart)

# print performance measure means across train-test splits
output$descriptive$mean

## End(Not run)

```

Description

Calculates multiple performance measures for binary or multiclass classification. Uses known class labels and evaluates against predicted labels.

Usage

```
cpm(x, y, level = NULL, fbeta = NULL, prior = NULL)
```

Arguments

x	Known class labels of class numeric, factor, or integer. If factor, converted to class integer in the order of factor levels with integers beginning at 0 (i.e., for binary classification, factor levels become 0 and 1; for multiclass, levels become 0, 1, 2, etc.).
y	Predicted class labels of class numeric, factor, or integer. If factor, converted to class integer in the order of factor levels with integers beginning at 0 (i.e., for binary classification, factor levels become 0 and 1; for multiclass, levels become 0, 1, 2, etc.).
level	Optional argument specifying possible class labels. For cases where x or y do not contain all possible classes. Can be of class numeric, integer, or character. Must contain two elements for binary classification, and contain three or more elements for multiclass classification. If integer, integers should be ordered (e.g., binary with c(0, 1); or three-class with c(0, 1, 2)). Note: if both x and y jointly contain only a single value (e.g., 1), must specify argument level in order to identify classification as binary or multiclass.
fbeta	Optional numeric argument specifying beta value for F-score. Defaults to fbeta = 1, providing an F1-score (i.e., the balanced harmonic mean between precision and recall). Can be any real number.
prior	Optional numeric argument specifying weights for classes. Currently only implemented with multiclass problems. Defaults to prior = c(rep(1/1lev, 1lev)), where 1lev is the number of classes, providing equal importance across classes.

Details

Selecting one class as a negative class and one class as a positive class, binary classification generates four possible outcomes: (1) negative cases classified as positives, called false positives (FP); (2) negative cases classified as negatives, called true negatives (TN); (3) positive cases classified as negatives, called false negatives (FN); and (4) positive cases classified as positives, called true positives (TP).

Multiple evaluation measures are calculated using these four outcomes. Measures include: overall error (ERR), also called fraction incorrect; overall accuracy (ACC), also called fraction correct; true positive rate (TPR), also called recall, hit rate, or sensitivity; false negative rate (FNR), also called miss rate; false positive rate (FPR), also called fall-out; true negative rate (TNR), also called specificity or selectivity; positive predictive value (PPV), also called precision; false discovery rate (FDR); negative predictive value (NPV); false omission rate (FOR); and F-score (FS).

In multiclass classification, the four outcomes are possible for each individual class in macro-averaging, and performance measures are averaged over classes. Macro-averaging gives equal importance to all classes. For multiclass classification, calculated measures are currently only macro-averaged. See the listed reference in this help file for additional details on micro-averaging.

For binary classification, this function assumes a negative class and a positive class (i.e., it contains a reference group) and is ordered. Multiclass classification is currently assumed to be unordered.

Computational details:

$$\text{ERR} = (\text{FP} + \text{FN}) / (\text{TP} + \text{TN} + \text{FP} + \text{FN}).$$

$$\text{ACC} = (\text{TP} + \text{TN}) / (\text{TP} + \text{TN} + \text{FP} + \text{FN}), \text{ and } \text{ACC} = 1 - \text{ERR}.$$

$$\text{TPR} = \text{TP} / (\text{TP} + \text{FN}).$$

$$\text{FNR} = \text{FN} / (\text{FN} + \text{TP}), \text{ and } \text{FNR} = 1 - \text{TPR}.$$

$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN}).$$

$$\text{TNR} = \text{TN} / (\text{TN} + \text{FP}), \text{ and } \text{TNR} = 1 - \text{FPR}.$$

$$\text{PPV} = \text{TP} / (\text{TP} + \text{FP}).$$

$$\text{FDR} = \text{FP} / (\text{FP} + \text{TP}), \text{ and } \text{FDR} = 1 - \text{PPV}.$$

$$\text{NPV} = \text{TN} / (\text{TN} + \text{FN}).$$

$$\text{FOR} = \text{FN} / (\text{FN} + \text{TN}), \text{ and } \text{FOR} = 1 - \text{NPV}.$$

$$\text{FS} = (1 + \text{beta}^2) * ((\text{PPV} * \text{TPR}) / (((\text{beta}^2) * \text{PPV}) + \text{TPR})).$$

All performance measures calculated are between 0 and 1, inclusive. For multiclass classification, macro-averaged values are provided for each performance measure. Note that 'beta' in FS represents the relative weight such that recall (TPR) is beta times more important than precision (PPV). See reference for more details.

Value

Returns list where first element is a full confusion matrix `cm` and where the second element is a data frame containing performance measures. For multiclass classification, macro-averaged values are provided (i.e., each measure is calculated for each class, then averaged over all classes; the average is weighted by argument `pr i` or if provided). The second list element contains the following performance measures:

<code>cm</code>	A confusion matrix with counts for each of the possible outcomes.
<code>err</code>	Overall error (ERR). Also called fraction incorrect.
<code>acc</code>	Overall accuracy (ACC). Also called fraction correct.
<code>tp</code>	True positive rate (TPR). Also called recall, hit rate, or sensitivity.
<code>fpr</code>	False positive rate (FPR). Also called fall-out.
<code>tnr</code>	True negative rate (TNR). Also called specificity or selectivity.
<code>fnr</code>	False negative rate (FNR). Also called miss rate.
<code>ppv</code>	Positive predictive value (PPV). Also called precision.
<code>npv</code>	Negative predictive value (NPV).
<code>fdr</code>	False discovery rate (FDR).
<code>fom</code>	False omission rate (FOR).
<code>fs</code>	F-score. Mean between TPR (recall) and PPV (precision) varying by importance given to recall over precision (see Details section and argument <code>fbeta</code>).

Author(s)

Matthew Asisgress <mattgress@protonmail.ch>

References

Sokolova, M. and Lapalme, G. (2009). A systematic analysis of performance measures for classification tasks. *Information Processing and Management*, 45(4), 427-437.

Examples

```
##### Parafac example with 3-way array and binary response #####
## Not run:
# set seed and simulate a three-way array related to a binary response
set.seed(5)

# define target correlation matrix for columns of C mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),                # for A weights
                distG = list(dname = "gamma", shape = 2,
                             scale = 4))                  # for G weights

# simulate a three-way array connected to a response
data <- simcpfa(arraydim = c(11, 12, 100), model = "parafac", nfac = 3,
               nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
               meanpred = rep(2, 3), modes = 3, corrpred = cormat,
               technical = techlist, smethod = "eigende")

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
method <- c("PLR", "SVM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X[, , 1:80], y = data$y[1:80],
                      model = model, nfac = 3, nfolds = nfolds,
                      method = method, family = family,
                      parameters = parameters, parallel = FALSE,
                      const = const, nstart = nstart)

# predict class labels
```

```

predict.labels <- predict(object = tune.object, newdata = data$X[, , 81:100],
                          type = "response")

# calculate performance measures for predicted class labels
y.pred <- predict.labels[, 1]
yproc <- as.numeric(data$y[81:100]) - 1
evalmeasure <- cpm(x = yproc, y = y.pred)

# print performance measures
evalmeasure

## End(Not run)

```

cpm.all

*Wrapper for Calculating Classification Performance Measures***Description**

Applies function `cpm` to multiple sets of class labels. Each set of class labels is evaluated against the same set of predicted labels. Works with output from function `predict.tunecpfa` and calculates classification performance measures for multiple classifiers or numbers of components.

Usage

```
cpm.all(x, y, ...)
```

Arguments

<code>x</code>	A data frame where each column contains a set of class labels of class numeric, factor, or integer. If a set is of class factor, that set is converted to class integer in the order of factor levels with integers beginning at 0 (i.e., for binary classification, factor levels become 0 and 1; for multiclass, levels become 0, 1, 2, etc.).
<code>y</code>	Class labels of class numeric.
<code>...</code>	Additional arguments passed to function <code>cpm</code> for calculating classification performance measures.

Details

Wrapper function that applies function `cpm` to multiple sets of class labels and one other set of labels. See help file for function `cpm` for additional details.

Value

Returns a list with the following two elements:

<code>cm.list</code>	A list of confusion matrices, denoted <code>cm</code> , where each confusion matrix is associated with one comparison.
<code>cpms</code>	A data frame containing classification performance measures where each row contains measures for one comparison.

Author(s)

Matthew Asisgress <mattgress@protonmail.ch>

References

Sokolova, M. and Lapalme, G. (2009). A systematic analysis of performance measures for classification tasks. *Information Processing and Management*, 45(4), 427-437.

Examples

```
##### Parafac example with 3-way array and binary response #####
## Not run:
# set seed and simulate a three-way array related to a binary response
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),                # for A weights
                distG = list(dname = "gamma", shape = 2,
                             scale = 4))                # for G weights

# define target correlation matrix for columns of C mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# simulate a three-way array connected to a response
data <- simcpfa(arraydim = c(11, 12, 100), model = "parafac", nfac = 3,
               nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
               meanpred = rep(2, 3), modes = 3, corrpred = cormat,
               technical = techlist, smethod = "eigende")

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
method <- c("PLR", "SVM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tuneecpfa(x = data$X[, , 1:80], y = data$y[1:80],
                      model = model, nfac = 3, nfolds = nfolds,
                      method = method, family = family,
                      parameters = parameters, parallel = FALSE,
                      const = const, nstart = nstart)

# predict class labels
```

```

predict.labels <- predict(object = tune.object, newdata = data$X[, , 81:100],
                          type = "response")

# calculate performance measures for predicted class labels
yproc <- as.numeric(data$y[81:100]) - 1
evalmeasure <- cpm.all(x = predict.labels, y = yproc)

# print performance measures
evalmeasure

## End(Not run)

```

plotcpfa

Plot Optimal Model from Classification with Parallel Factor Analysis

Description

Plots optimal model based on results from a 'wrapcpfa' object generated by function cpfa.

Usage

```

plotcpfa(object, cmeasure = "acc", meanvalue = TRUE, supNum = FALSE,
          cmode = NULL, parallel = FALSE, cl = NULL, scale.remove = NULL,
          newscales = 1, scale.abmode = NULL, sign.remove = NULL, newsigns = 1,
          sign.abmode = NULL, ...)

```

Arguments

object	An object of class 'wrapcpfa' from function cpfa.
cmeasure	Classification performance measure used to select the optimal number of components. Options include c("err", "acc", "tpr", "fpr", "tnr", "fnr", "ppv", "npv", "fdr", "fom", "fs"). If cmeasure is in c("err", "fpr", "fnr", "fdr", "fom"), the number of components that minimized cmeasure is selected among all classification methods. Otherwise, the number that maximized cmeasure is selected.
meanvalue	Logical indicating whether to find the optimal number of components based on the mean performance across replications from the results generated by cpfa. If meanvalue = FALSE, the median is used.
supNum	Logical indicating whether to suppress text displaying component weight values within plot cells. If TRUE, values are not displayed.
cmode	Integer value of 1, 2, or 3 (or 4 if x is a four-way array) specifying the mode whose component weights were predictors for classification when generating the 'wrapcpfa' object using function cpfa. If the original input model from function cpfa was pca, cmode must be 1 or 2 when the original input x was a two-way matrix. If the original input x was a three-way or four-way array, cmode values greater than 2 are ignored with a warning.

<code>parallel</code>	Logical indicating whether parallel computing should be used. If TRUE, parallel computing is used.
<code>cl</code>	Cluster for parallel computing, which is used when <code>parallel = TRUE</code> . Note that if <code>parallel = TRUE</code> and <code>cl = NULL</code> , then the cluster is defined as <code>makeCluster(detectCores())</code> .
<code>scale.remode</code>	Character that indicates a mode to rescale. Must be one of <code>c("A", "B", "C", "D")</code> . Sent directly to argument <code>mode</code> in function <code>rescale</code> from package multiway . See help file for <code>rescale</code> for additional details. Ignored when function <code>cpfa</code> argument <code>model = 'pca'</code> . If supplied, argument <code>scale.abmode</code> must also be supplied.
<code>newscales</code>	The root mean-square for columns of the mode indicated by <code>scale.remode</code> . See help file for <code>rescale</code> for additional details. Ignored when function <code>cpfa</code> argument <code>model = 'pca'</code> .
<code>scale.abmode</code>	Character that indicates the mode that absorbs the inverse of rescalings applied to the mode indicated by <code>scale.remode</code> . Must be one of <code>c("A", "B", "C", "D")</code> . Sent directly to argument <code>absorb</code> in function <code>rescale</code> from package multiway . See help file for <code>rescale</code> for additional details. Ignored when function <code>cpfa</code> argument <code>model = 'pca'</code> . If supplied, argument <code>scale.remode</code> must also be supplied.
<code>sign.remode</code>	Character that indicates a mode to resign. Must be one of <code>c("A", "B", "C", "D")</code> . Sent directly to argument <code>mode</code> in function <code>resign</code> from package multiway . See help file for <code>resign</code> for additional details. Ignored when function <code>cpfa</code> argument <code>model = 'pca'</code> . If supplied, argument <code>sign.abmode</code> must also be supplied.
<code>newsigns</code>	Scalar or vector indicating resignings for columns of the mode indicated by <code>sign.remode</code> . See help file for <code>resign</code> for additional details. Ignored when function <code>cpfa</code> argument <code>model = 'pca'</code> .
<code>sign.abmode</code>	Character that indicates the mode that absorbs the negation of the resignings applied to the mode indicated by <code>sign.remode</code> . Must be one of <code>c("A", "B", "C", "D")</code> . Sent directly to argument <code>absorb</code> in function <code>resign</code> from package multiway . See help file for <code>resign</code> for additional details. Ignored when function <code>cpfa</code> argument <code>model = 'pca'</code> . If supplied, argument <code>sign.remode</code> must also be supplied.
<code>...</code>	Additional arguments to be passed to function <code>parafac</code> for fitting a Parafac model or function <code>parafac2</code> for fitting a Parafac2 model. See help file for function <code>parafac</code> or for function <code>parafac2</code> for additional details.

Details

Selects the number of components that optimized a performance measure across all classification methods used by `cpfa`. With this optimal number of components, fits the component model that was used by `cpfa` to create the input `'wrapcpfa'` object. Uses same constraints used in `cpfa`. Plots component weights for this optimal model using heatmaps. Darker red indicates component weights that are more negative while darker green indicates component weights that are more positive. For three-way Parafac, plots A and B weights. For four-way Parafac, plots A, B, and C weights. For three-way Parafac2, plots B weights. For four-way Parafac2, plots B and C weights. For PCA, plots loadings (i.e., A weights).

Value

Returns one or more heatmap plots of component weights for the optimal component model. Returns list of estimated component weights from the optimal model.

Aweights	Estimated A mode weights for optimal Parafac or Parafac2 model. For PCA, contains the component loadings.
Bweights	Estimated B mode weights for optimal Parafac or Parafac2 model. For PCA, contains the component scores.
Cweights	Estimated C mode weights for optimal Parafac or Parafac2 model. For PCA, returns NULL.
Dweights	Estimated D mode weights for optimal Parafac or Parafac2 model. For PCA, returns NULL.

Note

Applications of this function to real datasets can be explored at the following repository: <https://github.com/matthewasisgress/multiway-classification/>.

Author(s)

Matthew Asisgress <matgress@protonmail.ch>

References

See help file for function cpfa for a list of references.

Examples

```
##### Parafac2 example with 4-way array and multiclass response #####
## Not run:
# set seed and simulate a four-way ragged array related to a multiclass response
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),                # for A weights
                 distG = list(dname = "gamma", shape = 2,
                              scale = 4))                # for G weights

# define target correlation matrix for columns of D mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# simulate a four-way ragged array connected to a response
data <- simcpfa(arraydim = c(10, 11, 12, 100), model = "parafac2", nfac = 3,
                nclass = 3, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
                meanpred = rep(2, 3), modes = 4, corrpred = cormat,
                technical = techlist, smethod = "eigende")

# initialize
alpha <- seq(0, 1, length = 2)
```

```

gamma <- c(0, 1)
cost <- c(0.1, 5)
rda.alpha <- seq(0.1, 0.9, length = 2)
delta <- c(0.1, 2)
method <- c("PLR", "SVM", "RDA")
family <- "multinomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost,
                   rda.alpha = rda.alpha, delta = delta)
model <- "parafac2"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal, fourth mode to be nonnegative
const <- c("orthog", "uncons", "uncons", "nonneg")

# fit Parafac2 model and use fourth mode weights to tune classification
# methods, to predict class labels, and to return classification
# performance measures pooled across multiple train-test splits
output <- cpfa(x = data$X, y = data$y, model = model, nfac = 3,
              nrep = 2, ratio = 0.8, nfolds = nfolds, method = method,
              family = family, parameters = parameters,
              type.out = "descriptives", seeds = NULL, plot.out = TRUE,
              parallel = FALSE, const = const, nstart = nstart, ctol = 1e-2)

# plot heatmap of component weights for optimal model
plotcpfa(output, nstart = nstart, ctol = 1e-3)

## End(Not run)

```

predict.tunecpfa	<i>Predict Method for Tuning for Classification with Parallel Factor Analysis</i>
------------------	---

Description

Obtains predicted class labels from a 'tunecpfa' model object generated by function tunecpfa.

Usage

```

## S3 method for class 'tunecpfa'
predict(object, newdata = NULL, method = NULL,
        type = c("response", "prob", "classify.weights"),
        threshold = NULL, ...)

```

Arguments

object A fit object of class 'tunecpfa' produced by function tunecpfa.

newdata	An optional two-way matrix, three-way array, or four-way data array used to predict Parafac, Parafac2, or PCA component weights using estimated Parafac, Parafac2, or PCA model component weights from the input object. For Parafac2, can be a list of length K where the k-th element is a matrix or three-way array associated with the k-th observation. Matrix, array, or list must contain only real numbers. Dimensions must match dimensions of original data for all modes except the classification mode. If omitted, the original data are used.
method	Character vector indicating classification methods to use. Possible methods include penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM). If none selected, default is to use methods used in original <code>tunecpfa</code> run.
type	Character vector indicating type of prediction to return. Possible values include: (1) "response", returning predicted class labels; (2) "prob", returning predicted class probabilities; or (3) "classify.weights", returning predicted component weights used for classification in the specified component models. Defaults to "response".
threshold	For binary classification, value indicating prediction threshold over which observations are classified as the positive class. If not provided, calculates threshold using class proportions in original data. For multiclass classification, threshold is not currently implemented.
...	Additional predict arguments. Currently ignored.

Details

Predicts class labels for a binary or a multiclass outcome. Specifically, predicts component weights for one mode of a Parallel Factor Analysis-1 (Parafac) model, one mode of a Parallel Factor Analysis-2 (Parafac2) model, or scores from a PCA model, using new data and previously estimated mode weights from original data. Passes predicted component weights (or scores for PCA) to one or several classification methods as new data for predicting class labels.

Tuning parameters optimized by k-fold cross-validation are used for each classification method (see help for `tunecpfa`). If not supplied in argument `threshold`, prediction threshold for all classification methods is calculated using proportions of class labels for original data in the binary case (and the positive class proportion is set as the threshold). For multiclass case, class with highest probability is chosen.

Value

Returns one of the following, depending on the choice for argument `type`:

`type = "response"`

A data frame containing predicted class labels for each component model and classification method selected (see argument `type`). Number of columns is equal to number of methods times number of component models. Number of rows is equal to number of predicted observations.

`type = "prob"`

A list containing predicted probabilities for each component model and classification method selected (see argument `type`). The number of list elements is equal to the number of methods times the number of component models.

```
type = "classify.weights"
```

List containing predicted component weights for each component model. Length is equal to number of component models that were fit.

Note

Applications of this function to real datasets can be explored at the following repository: <https://github.com/matthewasisgress/multiway-classification/>.

Author(s)

Matthew Asisgress <mattgress@protonmail.ch>

References

See help file for function tunecpfa for a list of references.

Examples

```
##### Parafac example with 3-way array and binary response #####
## Not run:
# set seed and simulate a three-way array related to a binary response
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),          # for A weights
                 distG = list(dname = "gamma", shape = 2,
                             scale = 4))          # for G weights

# define target correlation matrix for columns of C mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# simulate a three-way array connected to a response
data <- simcpfa(arraydim = c(11, 12, 100), model = "parafac", nfac = 3,
                nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
                meanpred = rep(2, 3), modes = 3, corrpred = cormat,
                technical = techlist, smethod = "eigende")

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
method <- c("PLR", "SVM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")
```

```

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X[, , 1:80], y = data$y[1:80],
                      model = model, nfac = 3, nfolds = nfolds,
                      method = method, family = family,
                      parameters = parameters, parallel = FALSE,
                      const = const, nstart = nstart)

# predict class labels
predict.labels <- predict(object = tune.object, newdata = data$X[, , 81:100],
                          type = "response")

# print predicted labels
predict.labels

## End(Not run)

```

print.tunecpfa	<i>Print Method for Tuning for Classification with Parallel Factor Analysis</i>
----------------	---

Description

Prints summary of a 'tunecpfa' model object generated by function tunecpfa.

Usage

```

## S3 method for class 'tunecpfa'
print(x, ...)

```

Arguments

x	A fit object of class 'tunecpfa' from function tunecpfa.
...	Additional print arguments.

Details

Prints names of the models and methods used to create the input 'tunecpfa' model object. Prints misclassification error rates and estimation times in seconds.

Value

Returns a summary of the 'tunecpfa' model object.

Author(s)

Matthew Asisgress <mattgress@protonmail.ch>

References

See help file for function `tunecpfa` for a list of references.

Examples

```
##### Parafac example with 3-way array and binary response #####
## Not run:
# set seed and simulate a three-way array connected to a binary response
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),          # for A weights
                distG = list(dname = "gamma", shape = 2,
                             scale = 4))          # for G weights

# define target correlation matrix for columns of C mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# simulate a three-way array connected to a response
data <- simcpfa(arraydim = c(11, 12, 100), model = "parafac", nfac = 3,
               nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
               meanpred = rep(2, 3), modes = 3, corrpred = cormat,
               technical = techlist, smethod = "eigende")

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
method <- c("PLR", "SVM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X, y = data$y, model = model,
                      nfac = 3, nfolds = nfolds, method = method,
                      family = family, parameters = parameters,
                      parallel = FALSE, const = const, nstart = nstart)

# print summary of output
print(tune.object)

## End(Not run)
```

simcpfa

*Simulate Data for Classification with Parallel Factor Analysis***Description**

Simulates a two-way matrix, three-way array, or four-way array; and simulates a set of class labels that are related to the simulated matrix or array through one mode of that matrix or array. Data matrix or array is simulated using one of the following component models without constraints: Parafac, Parafac2, or PCA. Weights for mode weight matrices can be drawn from 12 common probability distributions. Alternatively, custom weights can be provided for any mode.

Usage

```
simcpfa(arraydim = NULL, model = "parafac", nfac = 2, nclass = 2,
        smethod = "logistic", nreps = 100, onreps = 10, props = NULL,
        corresp = NULL, meanpred = NULL, modes = 3, corrpred = NULL,
        pf2num = NULL, Amat = NULL, Bmat = NULL, Cmat = NULL, Dmat = NULL,
        Gmat = NULL, Emat = NULL, technical = list())
```

Arguments

arraydim	Numeric vector containing the number of dimensions for each mode of the simulated data matrix or array. Must contain integers greater than or equal to 2. Defaults to <code>c(10, 100)</code> for <code>modes = 2</code> ; to <code>c(10, 10, 100)</code> for <code>modes = 3</code> ; and to <code>c(10, 10, 10, 100)</code> for <code>modes = 4</code> .
model	Character specifying the model to use for simulating the data array. Must be 'parafac', 'parafac2', or 'pca'.
nfac	Number of components in the component model. Must be an integer greater than or equal to 1.
nclass	Number of classes in simulated class labels. Must be an integer greater than or equal to 2.
smethod	Simulation method, either "logistic" or "eigende". The former implements an iterative Monte Carlo rejection sampling method based on the generalized linear model (slower). The latter uses a multivariate normal distribution and constructs a joint covariance matrix, employing an eigendecomposition and assuming class labels arise from discretizing continuous latent variables (faster).
nreps	Number of replications for simulating class labels for a given set of classification mode component weights.
onreps	Number of replications for simulating a set of classification mode component weights.
props	Target proportions for simulated class labels in output 'y'. Defaults to equal proportions across classes.
corresp	Numeric vector of target correlations between simulated class labels and columns of the classification mode component weight matrix. Must have length equal to 'nfac'. Defaults to 0.5 for all components.

meanpred	Numeric vector of means used to generate the classification mode component weights. Must be real numbers. Operates as the mean vector parameterizing a multivariate normal distribution from which classification mode component weights are generated. Length must be equal to input <code>nfac</code> . Defaults to a vector of zeros.
modes	Single integer of 2, 3, or 4, indicating whether to simulate a two-way matrix, three-way array, or four-way array, respectively.
corrpred	A positive definite correlation matrix containing the target correlations for the classification mode component weights. Must have number of rows and columns equal to input <code>'nfac'</code> . Operates as the covariance matrix parameterizing a multivariate normal distribution from which classification mode component weights are generated. Defaults to a correlation matrix with 1 on the diagonal and 0.2 on the off-diagonals.
pf2num	When <code>model = 'parafac2'</code> , number of rows for each simulated matrix in the list of matrices <code>Amat</code> . Replaces the first element of input <code>arraydim</code> because, for the Parafac2 model, the number of rows in each simulated matrix can vary. If not specified when <code>model = 'parafac2'</code> , defaults to <code>rep(c((nfac + 1), (nfac + 2), (nfac + 3)), length.out = arraydim[modes])</code> .
Amat	When <code>model = 'parafac'</code> , a matrix of A mode weights with number of rows equal to the first element of input <code>'arraydim'</code> and with number of columns equal to input <code>'nfac'</code> . When <code>model = 'parafac2'</code> , a list with length equal to the last element of input <code>'arraydim'</code> , where each list element contains a matrix with number of rows of at least 2 and with number of columns equal to input <code>'nfac'</code> . When provided, replaces a simulated <code>Amat</code> . When <code>model = 'pca'</code> , a matrix of loadings with number of rows equal to the second element of input <code>'arraydim'</code> and with number of columns equal to input <code>'nfac'</code> .
Bmat	A matrix of B mode weights with number of rows equal to the second element of input <code>'arraydim'</code> and with number of columns equal to the input <code>'nfac'</code> . When provided, replaces a simulated <code>Bmat</code> . When <code>model = 'pca'</code> , a matrix of scores with number of rows equal to the first element of input <code>'arraydim'</code> and with number of columns equal to input <code>'nfac'</code> . If provided when <code>modes = 2</code> , <code>onreps</code> is reduced to one when <code>smethod</code> is <code>logistic</code> .
Cmat	A matrix of C mode weights with number of rows equal to the third element of input <code>'arraydim'</code> and with number of columns equal to the input <code>'nfac'</code> . When provided, replaces a simulated <code>Cmat</code> when <code>modes = 4</code> . When <code>modes = 3</code> , replaces the simulated classification mode weight matrix. If provided when <code>modes = 3</code> , <code>onreps</code> is reduced to one when <code>smethod</code> is <code>logistic</code> . When <code>modes</code> is 2, this argument is ignored.
Dmat	A matrix of D mode weights with number of rows equal to the fourth element of input <code>'arraydim'</code> and with number of columns equal to the input <code>'nfac'</code> . When <code>modes = 4</code> , replaces the simulated classification mode weight matrix. When <code>modes</code> is 2 or 3, this argument is ignored. If provided when <code>modes = 4</code> , <code>onreps</code> is reduced to one when <code>smethod</code> is <code>logistic</code> .
Gmat	When <code>model = 'parafac2'</code> , a matrix of G mode weights with number of rows equal to input <code>'nfac'</code> and with number of columns equal to input <code>'nfac'</code> . When provided, replaces a simulated <code>Gmat</code> .

Emat	When <code>model = 'parafac'</code> , a 3-way or 4-way array containing noise to be added to the corresponding elements in the simulated data array. Error array dimensions must be equal to the values contained in <code>arraydim</code> . When <code>model = 'parafac2'</code> , a list containing either matrices (i.e., when <code>modes = 3</code>) or three-way arrays (i.e., when <code>modes = 4</code>) whose elements contain noise to be added to corresponding elements in the simulated data array. When provided, replaces a simulated <code>Emat</code> . When <code>model = 'pca'</code> , a matrix whose elements contain noise to be added to corresponding elements in the simulated data matrix. When provided, replaces a simulated <code>Emat</code> .
technical	<p>List containing arguments related to distributions from which to simulate data. When specified, must contain one or more of the following:</p> <p>distA List containing arguments specifying the distribution from which deviates are drawn for A mode weights contained in <code>Amat</code>. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.</p> <p>distB List containing arguments specifying the distribution from which deviates are drawn for B mode weights contained in <code>Bmat</code>. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments. Ignored if <code>model = 'pca'</code>.</p> <p>distC For when <code>modes = '4'</code>, list containing arguments specifying the distribution from which deviates are drawn for C mode weights contained in <code>Cmat</code>. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments. Ignored when <code>modes = 3</code>.</p> <p>distG For when <code>model = 'parafac2'</code>, list containing arguments specifying the distribution from which deviates are drawn for G weights contained in <code>Gmat</code>. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.</p> <p>distE List containing arguments specifying the distribution from which deviates are drawn for error contained in <code>Emat</code>. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.</p>

Details

By selecting `smethod = "logistic"`, the data array simulation consists of two steps. First, a Monte Carlo simulation is conducted to simulate class labels using a binomial logistic (i.e., in the binary case) or multinomial logistic (i.e., in the multiclass case) regression model. Specifically, columns of the classification mode weights matrix (e.g., `Cmat` when `modes = 3`) are generated from a multivariate normal distribution with mean vector `meanpred` and with covariance matrix `corrpred`. Values are then drawn randomly from a uniform or a normal distribution and serve as beta coefficients. A linear combination of these beta coefficients and the generated classification weights produces a linear systematic part, which is passed through the logistic function (i.e., the sigmoid) in the binary case or through the softmax function in the multiclass case. Resulting probabilities are used to assign class labels. The simulation repeats classification weights generation `onreps` times and repeats class label generation, within each `onreps` iteration, a total of `nreps` times. The generated class labels that correlate best with the generated classification weights (i.e., with correlations closest to `corresp`) are retained as the final class labels with corresponding final classification weights. An

adaptive sampling technique is used during the simulation such that optimal beta coefficients from previous iterations are used to parameterize a normal distribution, from which new coefficients are drawn in subsequent iterations. Note that, if any simulation replicate produces a set of class labels where all labels are the same (i.e., have no variance), that replicate is discarded. Note also that onreps is ignored when the classification mode weight matrix (i.e., Bmat when modes = 2, Cmat when modes = 3, or Dmat when modes = 4) is provided; in this case, class labels are simulated with respect to the provided classification mode weight matrix.

Second, depending on the chosen model (i.e., Parafac, Parafac2, or PCA) specified via model, and depending on the number of modes specified via modes, component matrices are randomly generated for each mode of the data matrix or array. A data matrix or array is then constructed using a Parafac, Parafac2, or PCA structure from these weight matrices, including the generated classification mode weight matrix (i.e., Bmat, Cmat, or Dmat) from the first step. Alternatively, weight matrices can be provided to override random generation for any weight matrix with the exception of the classification mode. When provided, weight matrices are used to form the final data matrix or array. Finally, random noise is added to each value in the matrix or array. The resulting output is a synthetic data matrix or array paired, through one mode of that matrix or array, with a simulated binary or multiclass response.

Alternatively, by selecting smethod = "eigende", the function simulates component weights and a latent response variable simultaneously from a joint multivariate normal distribution using an eigendecomposition. The covariance structure is defined by corrpred and by a corrected version of corresp that accounts for the attenuation in correlation caused by discretizing the latent response. This continuous latent response vector is then discretized into class labels using quantile cuts defined by the cumulative sum of props. This method offers an efficient, non-iterative alternative that satisfies the target covariance structure without rejection sampling.

The technical argument controls the probability distributions used to simulate weights for different modes. Currently, technical is highly structured. In particular, technical must be provided as a named list whose elements must be one of 'distA', 'distB', 'distC', 'distG', or 'distE', with the last letter of each name designating a mode or, in the case of 'distE', designating error. Each element provided must itself be a list where the first inner list element is named 'dname', specifying the distribution to be used to generate weights for a given mode or for error. There are 12 'dname' options: 'normal', 'uniform', 'gamma', 'beta', 'binomial', 'poisson', 'exponential', 'geometric', 'negbinomial', 'hypergeo', 'lognormal', and 'cauchy'. Additional arguments can be added to each inner list to parameterize the probability distribution being used. These arguments can be one of the following, for each distribution allowed:

For dname = 'normal', allowed arguments are mean or sd (i.e., function rnorm is called).

For dname = 'uniform', allowed arguments are min or max (i.e., function runif is called).

For dname = 'gamma', allowed arguments are shape or scale (i.e., function rgamma is called).

For dname = 'beta', allowed arguments are shape1 or shape2 (i.e., function rbeta is called).

For dname = 'binomial', allowed arguments are size or prob (i.e., function rbinom is called).

For dname = 'poisson', allowed argument is lambda (i.e., function rpois is called).

For dname = 'exponential', allowed argument is rate (i.e., function rexp is called).

For dname = 'geometric', allowed argument is prob (i.e., function rgeom is called).

For dname = 'negbinomial', allowed arguments are size or prob (i.e., function rnbinom is called).

For dname = 'hypergeo', allowed arguments are m, n, or k (i.e., function rhyper is called).

For `dname = 'lognormal'`, allowed arguments are `meanlog` or `sdlog` (i.e., function `rlnorm` is called).

For `dname = 'cauchy'`, allowed arguments are `location` or `scale` (i.e., function `rcauchy` is called).

Note that if a weight matrix and technical information are both provided for a given mode (or for error), the weight matrix is used while technical information is ignored. See Examples below for an example of how to set up technical.

Value

<code>X</code>	Simulated data matrix or array with dimensions specified by <code>arraydim</code> and, when <code>model = 'parafac2'</code> , also by <code>pf2num</code> . When <code>model = 'parafac'</code> , <code>X</code> is an object of class <code>'array'</code> . When <code>model = 'parafac2'</code> , <code>X</code> is an object of class <code>'list'</code> . When <code>model = 'pca'</code> , <code>X</code> is an object of class <code>'matrix'</code> .
<code>y</code>	Simulated class labels provided as an object of class <code>'factor'</code> . When <code>model = 'parafac'</code> or <code>model = 'parafac2'</code> , the number of labels is equal to the last element of <code>arraydim</code> . When <code>model = 'pca'</code> , the number of labels is equal to the first element of <code>arraydim</code> .
<code>model</code>	Character value indicating the component model that was used to simulate the data matrix or array.
<code>Amat</code>	Simulated A mode weights. When <code>model = 'parafac'</code> , output is a matrix with number of rows equal to the first element of <code>arraydim</code> and with number of columns equal to the number of components <code>nfac</code> . When <code>model = 'parafac2'</code> , output is a list of matrices with number of rows for each matrix equal to those specified by <code>pf2num</code> and with number of columns equal to <code>nfac</code> . When <code>model = 'pca'</code> , output is a matrix with number of rows equal to the second element of <code>arraydim</code> . If <code>Amat</code> was supplied, returns original <code>Amat</code> instead of a simulated <code>Amat</code> .
<code>Bmat</code>	Simulated B mode weights provided as a matrix with number of rows equal to the second element of <code>arraydim</code> and with number of columns equal to the number of components <code>nfac</code> . When <code>model = 'pca'</code> , output is a matrix with number of rows equal to the first element of <code>arraydim</code> . If <code>Bmat</code> was supplied, returns original <code>Bmat</code> instead of a simulated <code>Bmat</code> .
<code>Cmat</code>	Simulated C mode weights provided as a matrix with number of rows equal to the third element of <code>arraydim</code> and with number of columns equal to the number of components <code>nfac</code> . If <code>Cmat</code> was supplied when <code>modes = 4</code> , returns original <code>Cmat</code> instead of a simulated <code>Cmat</code> . Not provided when <code>modes = 2</code> .
<code>Dmat</code>	Simulated D mode weights provided when <code>modes = 4</code> . Output is a matrix with number of rows equal to the fourth element of <code>arraydim</code> and with number of columns equal to the number of components <code>nfac</code> . Not provided when <code>modes = 2</code> or when <code>modes = 3</code> .
<code>Gmat</code>	Simulated G weights provided when <code>model = 'parafac2'</code> . Provided as a matrix with number of rows and columns equal to <code>nfac</code> . If <code>Gmat</code> was supplied, returns original <code>Gmat</code> instead of a simulated <code>Gmat</code> .
<code>Emat</code>	Error matrix, array, or list containing noise added to corresponding elements of simulated data matrix or array. Output has dimensions specified by <code>arraydim</code> and, when <code>model = 'parafac2'</code> , also by <code>pf2num</code> . When <code>model = 'parafac'</code> ,

Emat is an object of class 'array'. When model = 'parafac2', Emat is an object of class 'list'. When model = 'pca', Emat is an object of class 'matrix'.

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References

See help file for function cpfa for a list of references.

Examples

```
##### Parafac2 example with 4-way array and multiclass response #####
## Not run:
# set seed for reproducibility
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),                # for A weights
                distG = list(dname = "gamma", shape = 2,
                             scale = 4))                # for G weights

# define target correlation matrix for columns of D mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# simulate a four-way ragged array connected to a response
data <- simcpfa(arraydim = c(10, 11, 12, 100), model = "parafac2", nfac = 3,
               nclass = 3, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
               meanpred = rep(2, 3), modes = 4, corrpred = cormat,
               technical = techlist, smethod = "eigende")

# examine correlations among columns of classification mode matrix Dmat
cor(data$Dmat)

# examine correlations between columns of classification mode matrix Dmat and
# simulated class labels
yproc <- as.numeric(data$y) - 1
cor(data$Dmat, yproc)

## End(Not run)
```

Description

Fits Richard A. Harshman's Parallel Factor Analysis-1 (Parafac) model or Parallel Factor Analysis-2 (Parafac2) model to a three-way or four-way data array. Also fits a principal component analysis model (PCA) to a two-way matrix. Allows for different constraint options on multiple tensor modes. For PCA, allows for either an unrotated or varimax rotated solution. Uses component weights from a single mode of the model as predictors to tune parameters for one or more classification methods via a k-fold cross-validation procedure. Supports binary and multiclass classification.

Usage

```
tunecpfa(x, y, model = c("parafac", "parafac2", "pca"), nfac = 1, nfolds = 10,
         method = c("PLR", "SVM", "RF", "NN", "RDA", "GBM"),
         family = c("binomial", "multinomial"), parameters = list(),
         foldid = NULL, prior = NULL, cmode = NULL, parallel = FALSE,
         cl = NULL, verbose = TRUE, compscale = TRUE,
         pcarot = c("unrotated", "varimax"), ...)
```

Arguments

x	A three-way or four-way data array. For Parafac2, can be a list where each element is a matrix or three-way array. Array or list must contain only real numbers. See note below. For PCA, can be a two-way matrix, a three-way array, or a four-way array. If a three-way or four-way array for PCA, array is unfolded across all modes except the classification mode.
y	A vector containing at least two unique class labels. Should be a factor that contains two or more levels. For binary case, ensure the order of factor levels (left to right) is such that negative class is first and positive class is second.
model	Character designating the component model to use, including: model = "parafac" to fit the Parafac model, model = "parafac2" to fit the Parafac2 model, or model = "pca" to fit the PCA model.
nfac	Vector containing integers that specify the number of components for each component model to fit. Default is nfac = 1.
nfolds	Numeric value specifying the number of folds for k-fold cross-validation. Must be 2 or greater. Default is nfolds = 10.
method	Character vector indicating classification methods to use. Possible methods include penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM). If none selected, default is to use all methods.
family	Character value specifying binary classification (family = "binomial") or multiclass classification (family = "multinomial"). If not provided, number of levels of input y is used, where two levels is binary, and where three or more levels is multiclass.
parameters	List containing arguments related to classification methods. When specified, must contain one or more of the following:

	<p>alpha Values for penalized logistic regression alpha parameter; default is $\alpha = \text{seq}(0, 1, \text{length} = 6)$. Must be numeric and contain only real numbers between 0 and 1, inclusive.</p> <p>lambda Optional user-supplied lambda sequence for <code>cv.glmnet</code> for penalized logistic regression. Default is NULL.</p> <p>cost Values for support vector machine cost parameter; default is $\text{cost} = c(1, 2, 4, 8, 16, 32, 64)$. Must be numeric and contain only real numbers greater than or equal to 0.</p> <p>gamma Values for support vector machine gamma parameter; default is $\text{gamma} = c(0, 0.01, 0.1, 1, 10, 100, 1000)$. Must be numeric and greater than or equal to 0.</p> <p>ntree Values for random forest number of trees parameter; default is $\text{ntree} = c(100, 200, 400, 600, 800, 1600, 3200)$. Must be numeric and contain only integers greater than or equal to 1.</p> <p>nodesize Values for random forest node size parameter; default is $\text{nodesize} = c(1, 2, 4, 8, 16, 32, 64)$. Must be numeric and contain only integers greater than or equal to 1.</p> <p>size Values for neural network size parameter; default is $\text{size} = c(1, 2, 4, 8, 16, 32, 64)$. Must be numeric and contain only integers greater than or equal to 0.</p> <p>decay Values for neural network decay parameter; default is $\text{decay} = c(0.001, 0.01, 0.1, 1, 2, 4, 8, 16)$. Must be numeric and contain only real numbers.</p> <p>rda.alpha Values for regularized discriminant analysis alpha parameter; default is $\text{rda.alpha} = \text{seq}(0, 0.999, \text{length} = 6)$. Must be numeric and contain only real numbers between 0 (inclusive) and 1 (exclusive).</p> <p>delta Values for regularized discriminant analysis delta parameter; default is $\text{delta} = c(0, 0.1, 1, 2, 3, 4)$. Must be numeric and contain only real numbers greater than or equal to 0.</p> <p>eta Values for gradient boosting machine eta parameter; default is $\text{eta} = c(0.1, 0.3, 0.5, 0.7, 0.9)$. Must be numeric and contain only real numbers greater than 0 and less than 1.</p> <p>max.depth Values for gradient boosting machine max.depth parameter; default is $\text{max.depth} = c(1, 2, 3, 4)$. Must be numeric and contain only integers greater than or equal to 1.</p> <p>subsample Values for gradient boosting machine subsample parameter; default is $\text{subsample} = c(0.6, 0.7, 0.8, 0.9)$. Must be numeric and contain only real numbers greater than 0 and less than or equal to 1.</p> <p>nrounds Values for gradient boosting machine nrounds parameter; default is $\text{nrounds} = c(100, 200, 300, 500)$. Must be numeric and contain only integers greater than or equal to 1.</p>
foldid	Vector containing fold IDs for k-fold cross-validation. Can be of class integer, numeric, or data frame. Should contain integers from 1 through the number of folds. If not provided, fold IDs are generated randomly for observations using 1 through the number of folds <code>nfolds</code> .
prior	Prior probabilities of class membership. If specified, the probabilities should be in the order of the factor levels of input <code>y</code> . If unspecified, the observed class

	proportions for input y are used. Based on prior, inverse probability weights are calculated to account for class imbalance. Note that RF and RDA ignore prior and use uniform priors to handle imbalance.
<code>cmode</code>	Integer value of 1, 2, or 3 (or 4 if x is a four-way array) specifying the mode whose component weights will be predictors for classification. Defaults to the last mode of the input array (i.e., defaults to 3 for a three-way array, and to 4 for a four-way array). If <code>model = "parafac2"</code> , last mode will be used. If <code>model = "pca"</code> , <code>cmode</code> is set to the first mode.
<code>parallel</code>	Logical indicating whether to use parallel computing. If TRUE, the package parallel is used for parallel computing. For all classification methods except penalized logistic regression, the doParallel package is used as a wrapper. Defaults to FALSE, which implements sequential computing.
<code>c1</code>	Cluster for parallel computing, which is used when <code>parallel = TRUE</code> . Note that if <code>parallel = TRUE</code> and <code>c1 = NULL</code> , then the cluster is defined as <code>makeCluster(detectCores())</code> .
<code>verbose</code>	If TRUE, progress is printed.
<code>compscale</code>	Logical indicating whether to scale each column of the estimated classification component weights matrix (i.e., the features/predictors). If TRUE, each column is scaled to have mean zero and unit variance. If FALSE, no scaling is performed.
<code>pcarot</code>	Character indicating whether to apply a varimax rotation or leave PCA loadings unrotated when <code>model</code> is set to <code>pca</code> . Ignored when <code>model</code> is not <code>pca</code> . Defaults to "unrotated" if not specified.
<code>...</code>	Additional arguments to be passed to function <code>parafac</code> for fitting a Parafac model or function <code>parafac2</code> for fitting a Parafac2 model. Example: can impose different constraints on different modes of the input array using the argument <code>const</code> . See help file for function <code>parafac</code> or for function <code>parafac2</code> for additional details.

Details

After fitting a Parafac or Parafac2 model with the training set using package **multiway** (see `parafac` or `parafac2` in **multiway** for details), or after fitting a PCA model using the singular value decomposition, the estimated classification mode weight matrix is passed to one or more classification methods. The methods include: penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM).

Package **glmnet** fits models for PLR. PLR tunes penalty parameter λ while the elastic net parameter α is set by the user (see the help file for function `cv.glmnet` in package **glmnet**). For SVM, package **e1071** is used with a radial basis kernel. Penalty parameter `cost` and radial basis parameter `gamma` are used (see `svm` in package **e1071**). For RF, package **randomForest** is used and implements Breiman's random forest algorithm. The number of predictors sampled at each node split is set at the default of `sqrt(R)`, where R is the number of Parafac or Parafac2 components. Two tuning parameters allowed are `ntree`, the number of trees to be grown, and `nodesize`, the minimum size of terminal nodes (see `randomForest` in package **randomForest**). For NN, package **nnet** fits a single-hidden-layer, feed-forward neural network model. Penalty parameters `size` (i.e., number of hidden layer units) and `decay` (i.e., weight decay) are used (see **nnet**). For RDA, package **rda** fits a shrunken centroids regularized discriminant analysis model. Tuning parameters include

rda.alpha, the shrinkage penalty for the within-class covariance matrix, and delta, the shrinkage penalty of class centroids towards the overall dataset centroid. For GBM, package **xgboost** fits a gradient boosting machine model. Four tuning parameters are allowed: (1) eta, the learning rate; (2) max.depth, the maximum tree depth; (3) subsample, the fraction of samples per tree; and (4) nrounds, the number of boosting trees to build.

For all six methods, k-fold cross-validation is implemented to tune classification parameters where the number of folds is set by argument nfold.

Value

Returns an object of class tunecpfa with the following elements:

opt.model	List containing optimal model for tuned classification methods for each component model that was fit.
opt.param	Data frame containing optimal parameters for tuned classification methods.
kcv.error	Data frame containing KCV misclassification error for optimal parameters for tuned classification methods.
est.time	Data frame containing times for fitting the component model and for tuning classification methods.
model	Character designating the component model that was used, including: model = "parafac" for the Parafac model, model = "parafac2" for the Parafac2 model, or model = "pca" for the PCA model.
method	Numeric indicating classification methods used. Value of '1' indicates 'PLR'; value of '2' indicates 'SVM'; value of '3' indicates 'RF'; value of '4' indicates 'NN'; value of '5' indicates 'RDA'; and value of '6' indicates 'GBM'.
x	Two-way matrix, or three-way or four-way data array or list used in argument x. If x was a three-way or four-way array, and if model was pca, returns the flattened two-way matrix.
y	Factor containing class labels used. Note that output y is recoded such that the input labels of y are converted to numeric integers from 0 through the number of levels, which are then applied as labels for output y.
Aweights	List containing estimated A weights for each component model that was fit. For PCA, contains the loadings.
Bweights	List containing estimated B weights for each component model that was fit. Null if model was pca.
Cweights	List containing estimated C weights for each Parafac or Parafac2 model that was fit. Null if input argument x was a three-way array or if model was pca.
Phi	If model = "parafac2", a list containing estimated Phi from the Parafac2 model. Phi is the common cross product matrix shared by all levels of the last mode (see help file for function parafac2 in package multiway for additional details). NULL if model = "parafac" or if model = "pca".
const	Constraints used in fitting the Parafac, Parafac2, or PCA model. When model was pca, contains the value used in input pcarot to indicate whether a rotation was applied to the solution.

<code>cmode</code>	Integer value of 1, 2, or 3 (or 4 if <code>x</code> is a four-way array) specifying mode whose component weights were predictors for classification.
<code>family</code>	Character value specifying whether classification was binary (<code>family = "binomial"</code>) or multiclass (<code>family = "multinomial"</code>).
<code>xdim</code>	Numeric value specifying number of levels for each mode of input <code>x</code> . If <code>model = "parafac2"</code> , the number of levels for the first mode is designated as NA because the number of levels can differ across levels of the last mode. If <code>model = "pca"</code> and if input <code>x</code> was a 3-way or 4-way array, <code>xdim</code> contains the number of levels of the matrix that is the unfolded version of the input array.
<code>lxdim</code>	Integer specifying the number of modes of the output <code>x</code> . Identical to the number of modes of input <code>x</code> , except when input <code>x</code> was a 3-way or 4-way array and when <code>model</code> was <code>pca</code> . In this case, <code>lxdim</code> is 2.
<code>train.weights</code>	List containing classification component weights for each fit Parafac or Parafac2 model, for possibly different numbers of components. The weights used to train classifiers.
<code>priorweights</code>	List containing three elements based on input <code>prior</code> : (1) <code>weight</code> , inverse probability weights per observation, used to balance classes for PLR, NN, and GBM; (2) <code>frac</code> , inverse probability weights per class, used to balance classes for SVM; and (3) <code>pricorrect</code> , uniform priors used to balance classes for RF and RDA.
<code>scenters</code>	List containing center of the scale for each Parafac or Parafac2 model that was fit. Note that, for each component, estimated classification weights are mean-centered before being passed to classification methods. Returns list of NULL values if argument <code>compscale = FALSE</code> .
<code>sscales</code>	List containing standard deviation of the scale for each Parafac or Parafac2 model that was fit. Note that, for each component, estimated classification weights are scaled to have a variance of 1 before being passed to classification methods. Returns list of NULL values if argument <code>compscale = FALSE</code> .
<code>pcacenter</code>	Numeric vector containing centers for each feature used in PCA. NULL if <code>model</code> is not <code>pca</code> .

Note

For fitting the Parafac model, if argument `cmode` is not NULL, input array `x` is reshaped with function `aperm` such that the `cmode` dimension of `x` is ordered last. Estimated mode A and B (and mode C for a four-way array) weights that are outputted as `Aweights` and `Bweights` (and `Cweights`) reflect this permutation. For example, if `x` is a four-way array and `cmode = 2`, the original input modes 1, 2, 3, and 4 will correspond to output modes 1, 3, 4, 2. Here, output A = input 1; B = 3, and C = 4 (i.e., the second mode specified by `cmode` has been moved to the D mode/last mode). For `model = "parafac2"`, classification mode is assumed to be the last mode (i.e., mode C for three-way array and mode D for four-way array). For PCA, if argument `cmode` is not NULL, and if `x` is a 3-way or 4-way array, the array is reshaped with `aperm` such that the `cmode` dimension of `x` is ordered first. Then, the array is unfolded into a two-way matrix. If `x` is already input as a two-way matrix, the matrix is reshaped if `cmode` is 2, such that the matrix is transposed. Note that for PCA, `Aweights` contains the PCA model loadings.

In addition, note that the following combination of arguments will give an error: `nfac = 1`, `family = "multinomial"`, `method = "PLR"`. The issue arises from providing `glmnet::cv.glmnet` input `x`

with a matrix that has a single column. The issue is resolved for family = "binomial" because a column of 0s is appended to the single column, but this solution does not appear to work for the multiclass case. As such, this combination of arguments is not currently allowed. This issue will be resolved in a future update.

Applications of this function to real datasets can be explored at the following repository: <https://github.com/matthewasisgress/multiway-classification/>.

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Examples

```
##### Parafac example with 3-way array and binary response #####
## Not run:
# set seed and simulate a three-way array connected to a binary response
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),                # for A weights
                distG = list(dname = "gamma", shape = 2,
                             scale = 4))                # for G weights

# define target correlation matrix for columns of C mode weights matrix
cormat <- matrix(c(1, .6, .6, .6, 1, .6, .6, .6, 1), nrow = 3, ncol = 3)

# simulate a three-way array connected to a response
data <- simcpfa(arraydim = c(11, 12, 100), model = "parafac", nfac = 3,
               nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.6, 3),
               meanpred = rep(2, 3), modes = 3, corrpred = cormat,
               technical = techlist, smethod = "eigende")

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
ntree <- c(100, 200)
nodesize <- c(1, 2)
size <- c(1, 2)
decay <- c(0, 1)
rda.alpha <- c(0.1, 0.6)
delta <- c(0.1, 2)
eta <- c(0.3, 0.7)
max.depth <- c(1, 2)
subsample <- c(0.75)
nrounds <- c(100)
method <- c("PLR", "SVM", "RF", "NN", "RDA", "GBM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost, ntree = ntree,
                  nodesize = nodesize, size = size, decay = decay,
                  rda.alpha = rda.alpha, delta = delta, eta = eta,
                  max.depth = max.depth, subsample = subsample,
                  nrounds = nrounds)

model <- "parafac"
nfolds <- 3
```

```
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X, y = data$y, model = model,
                      nfac = 3, nfolds = nfolds, method = method,
                      family = family, parameters = parameters,
                      parallel = FALSE, const = const, nstart = nstart)

# print tuning object
tune.object

## End(Not run)
```

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